

Origins of Hidden Sector Dark Matter

Gilly Elor
290E 10/26/2011

With Clifford Cheung, Lawrence Hall and Piyush Kumar

Cosmology [arXiv:1010.0022](#)
Collider Signals [arXiv:1010.0024](#)

I. Cosmology

Evidence for Dark Matter

Lots of experimental evidence for the existence of dark matter particles

- Galactic Rotation Curves
- Velocity Dispersions of Galaxies
- Gravitational Lensing
- CMB
- Structure Formation
- ...

Relic abundance measured:

$$\Omega_{DM} h^2 \sim 0.11$$

Production Mechanism?

Candidate which gives correct relic abundance?

Production by “Freeze-Out”

Interactions with Standard Model particles keeps the Dark Matter in thermal equilibrium with the early universe bath as long as the interaction rate exceeds the expansion rate.

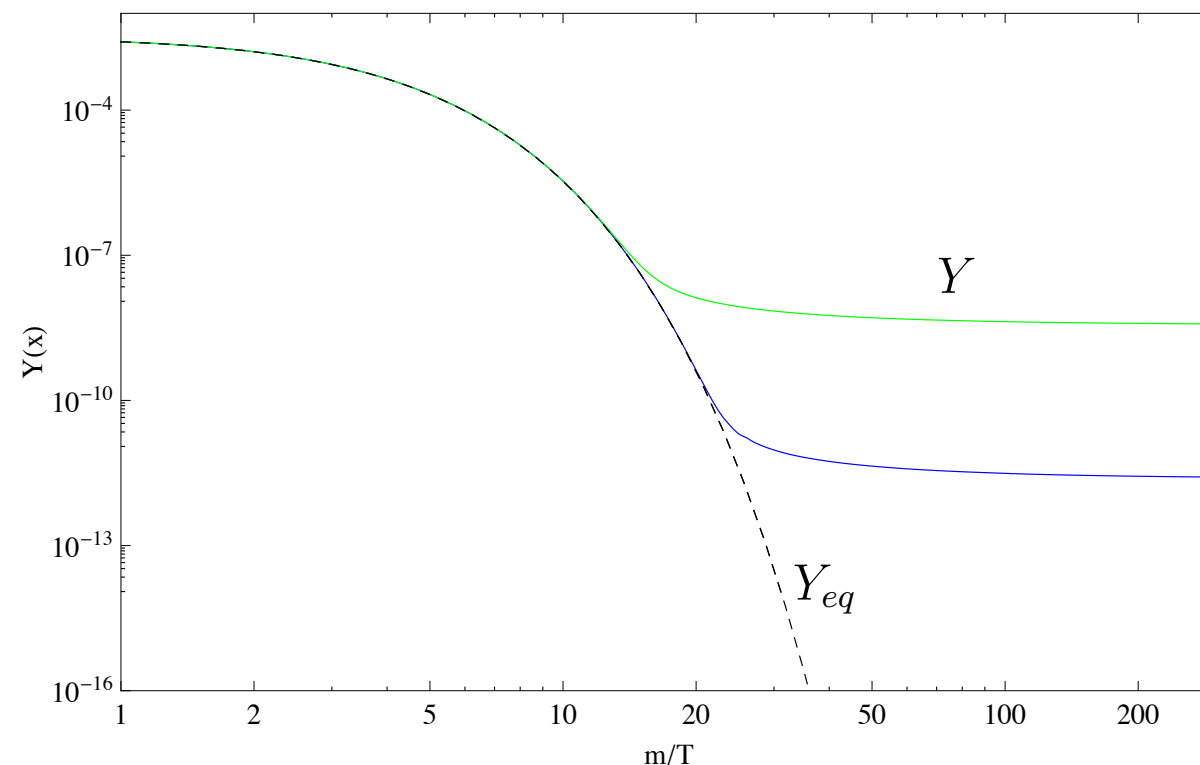
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The evolution of the number density is given by the Boltzmann equation:

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Convention is to re-write in terms of co-moving number density (or Yield): $Y = n/s$ $x = m/T$

$$\frac{dY}{dx} = -\frac{s\langle\sigma v\rangle}{Hx} (Y^2 - Y_{\text{eq}}^2)$$



Visible
Sector+DM
Bath T

Boltz suppression
because for a massive
particle is becomes hard
to produce a particle
anti-particle from the
bath once the
Temperature falls below
the mass

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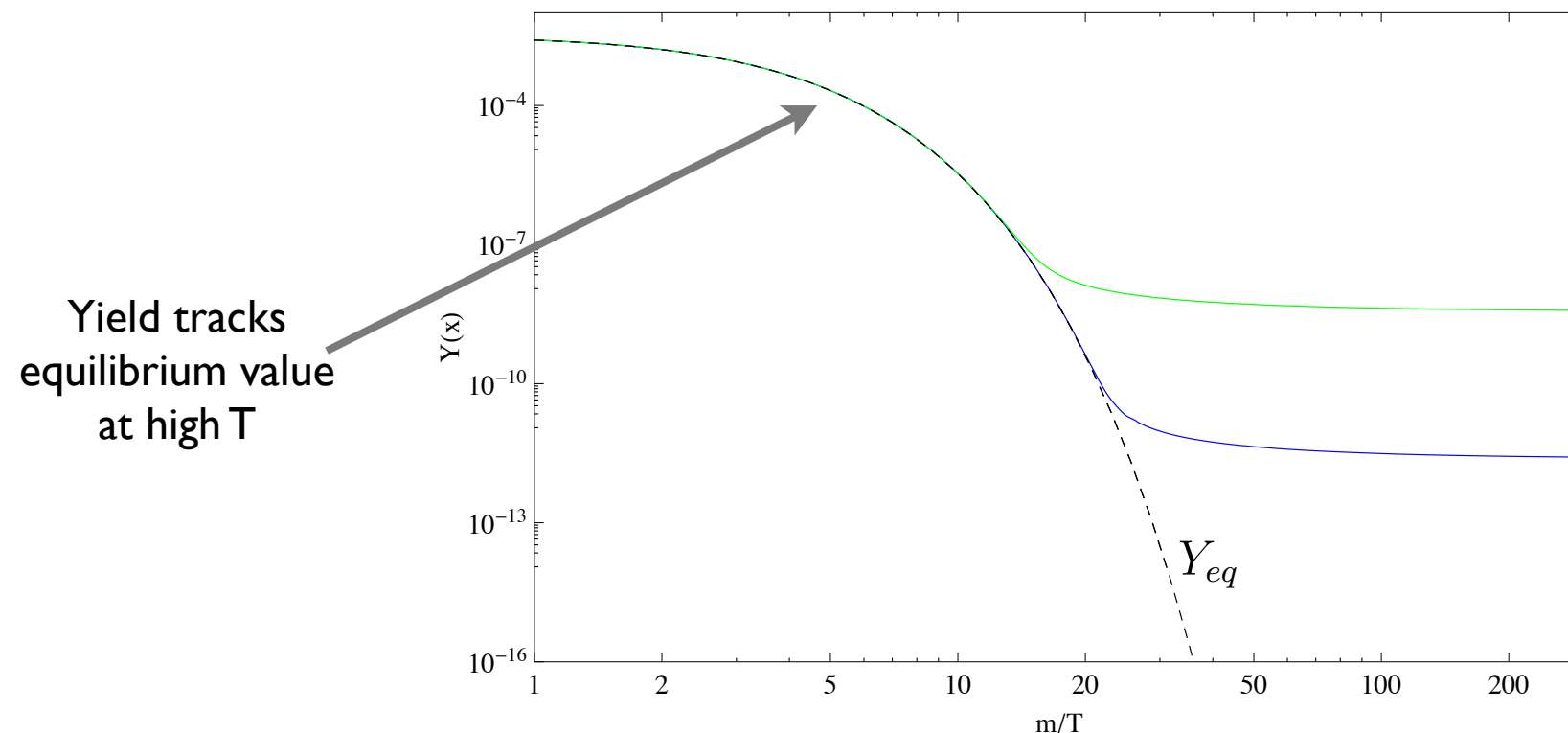
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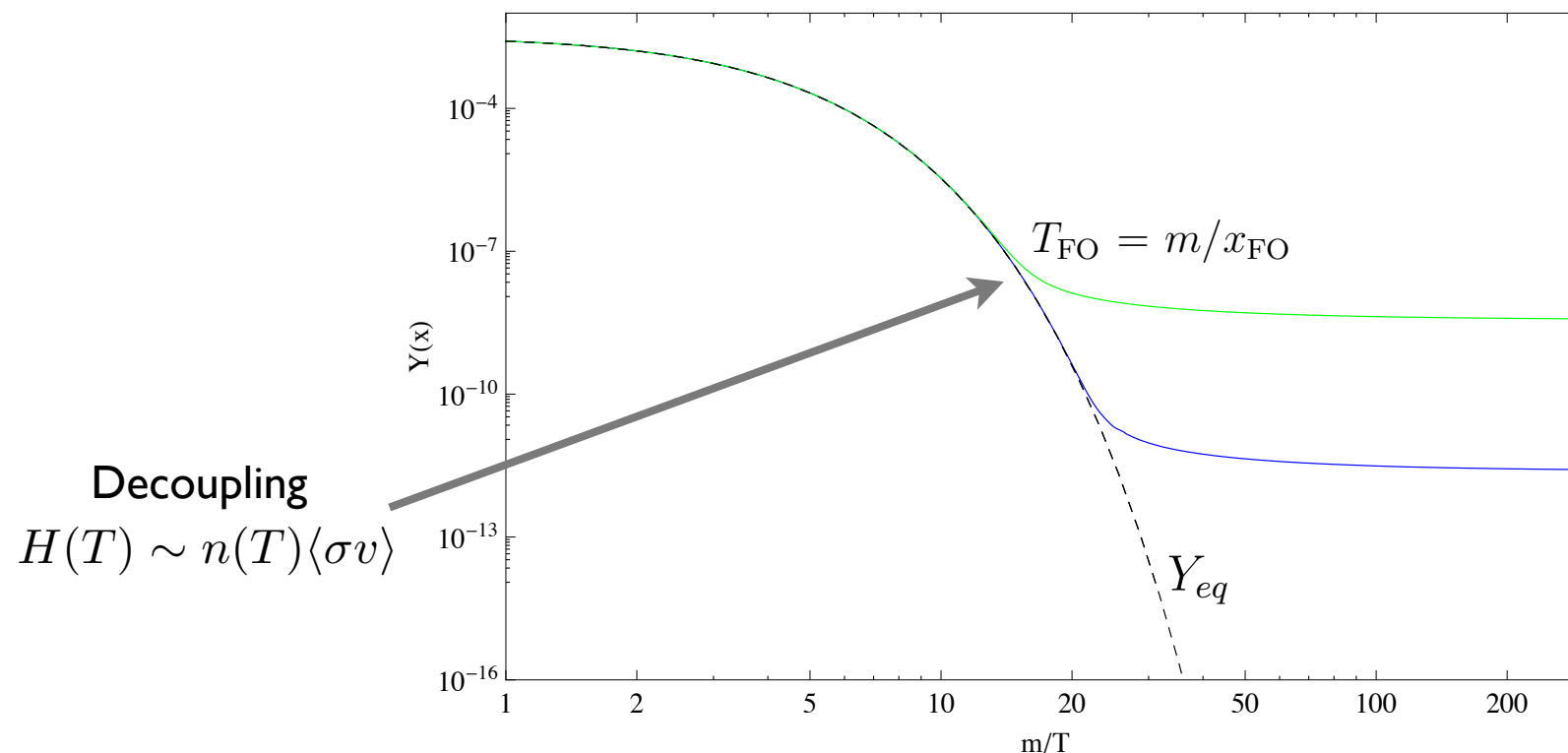
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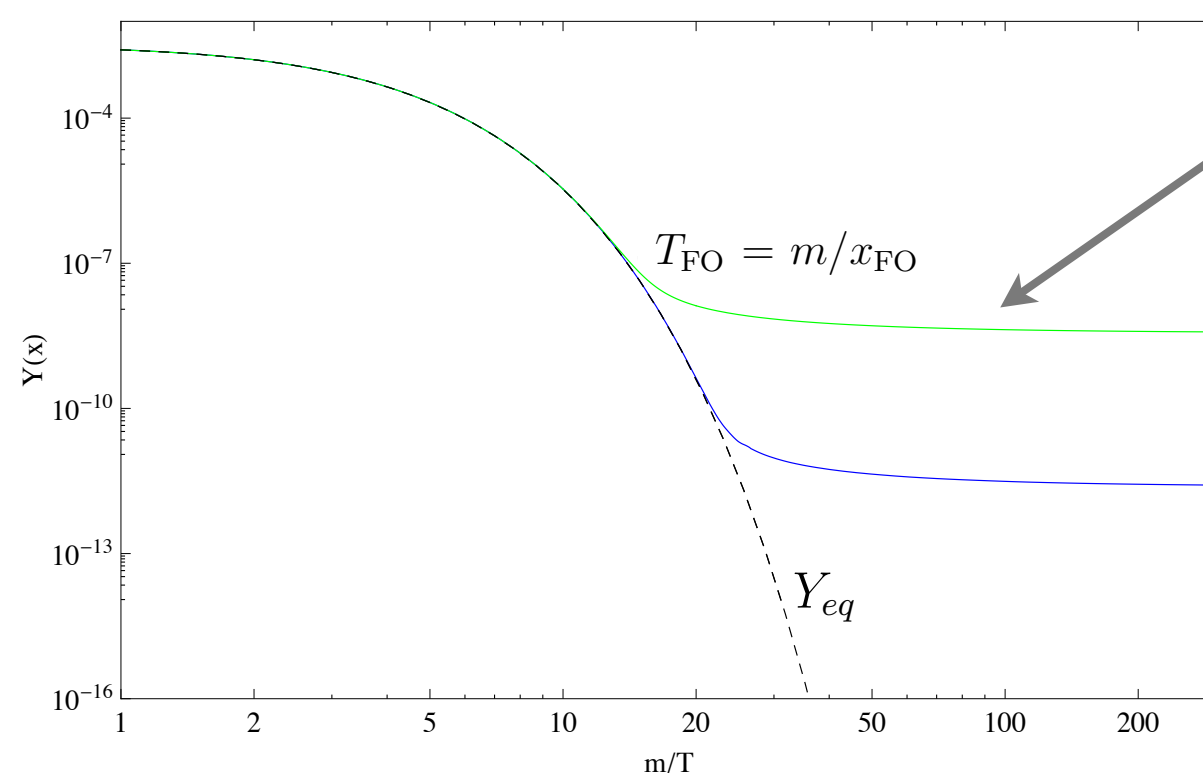
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$$H > Y(T)s(T)\langle\sigma v\rangle \Rightarrow \frac{dY}{dx} \sim 0$$

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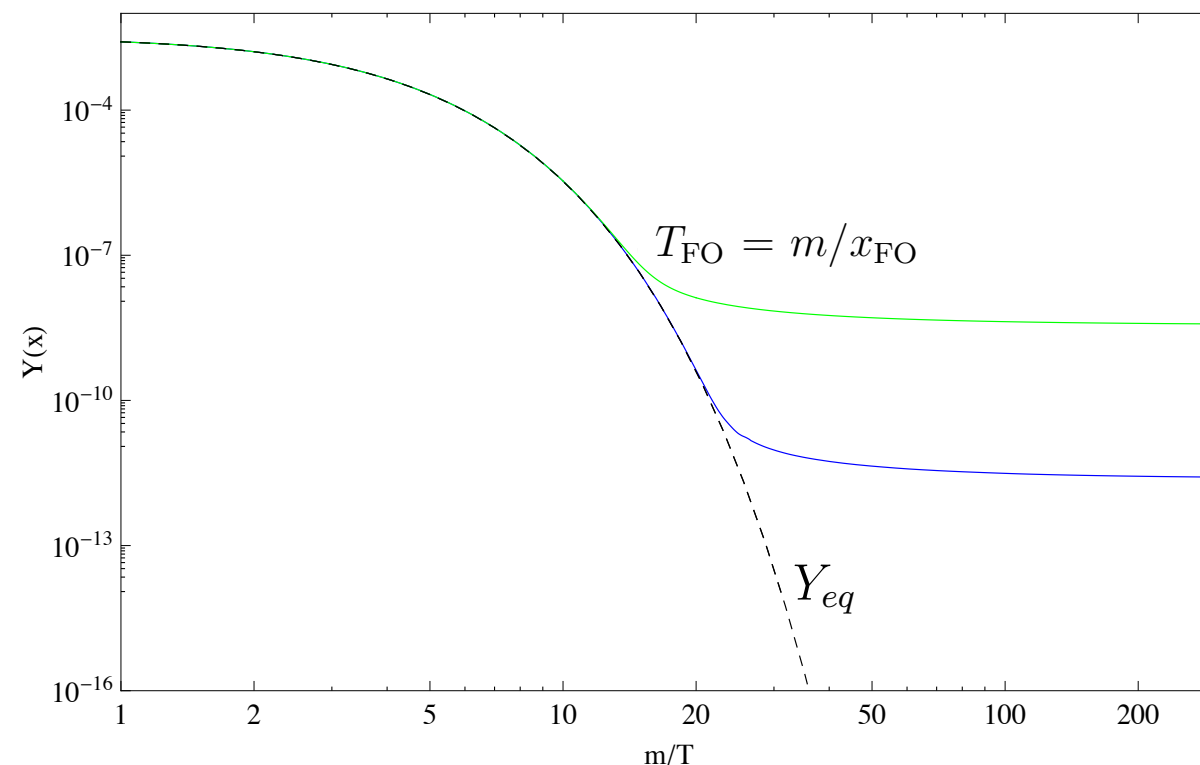
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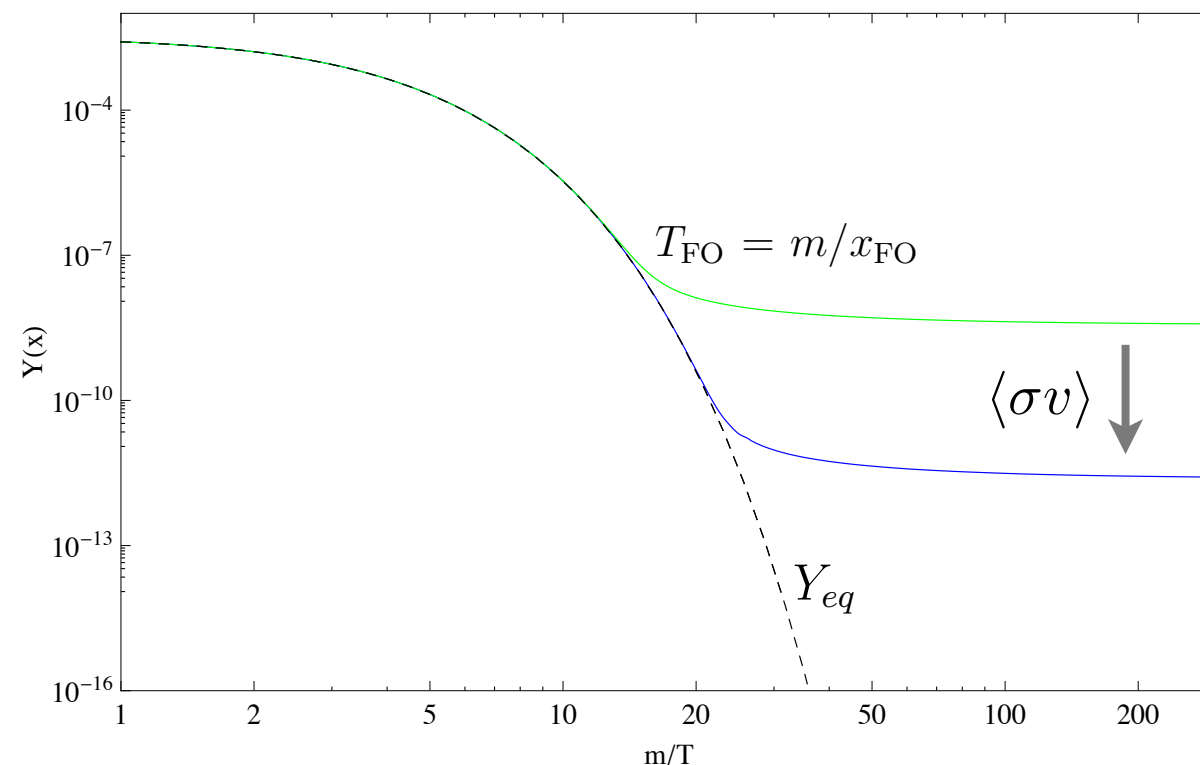
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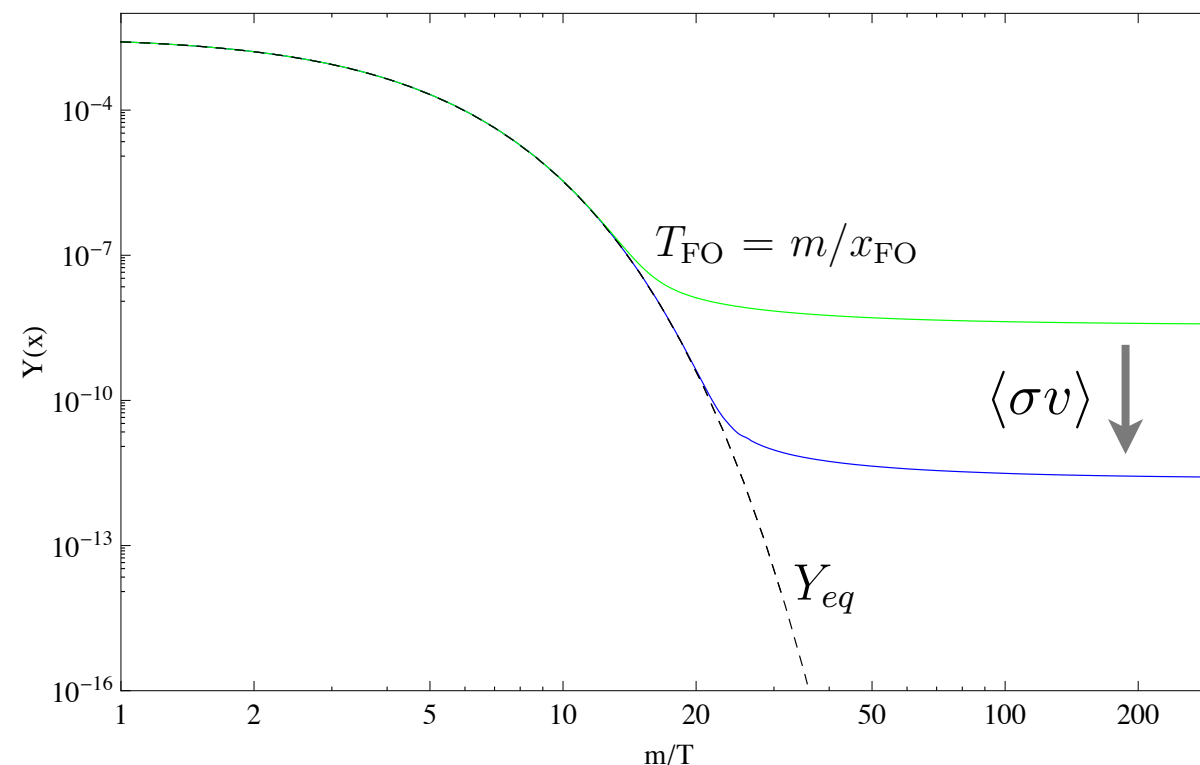
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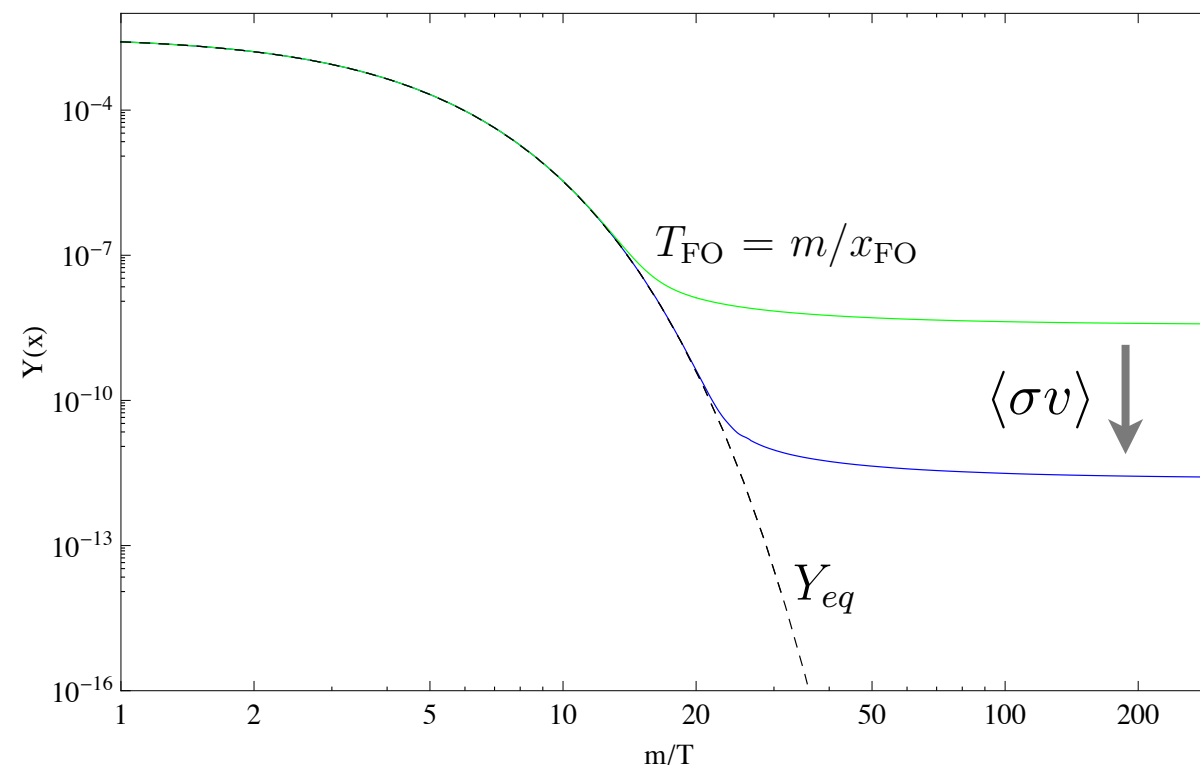
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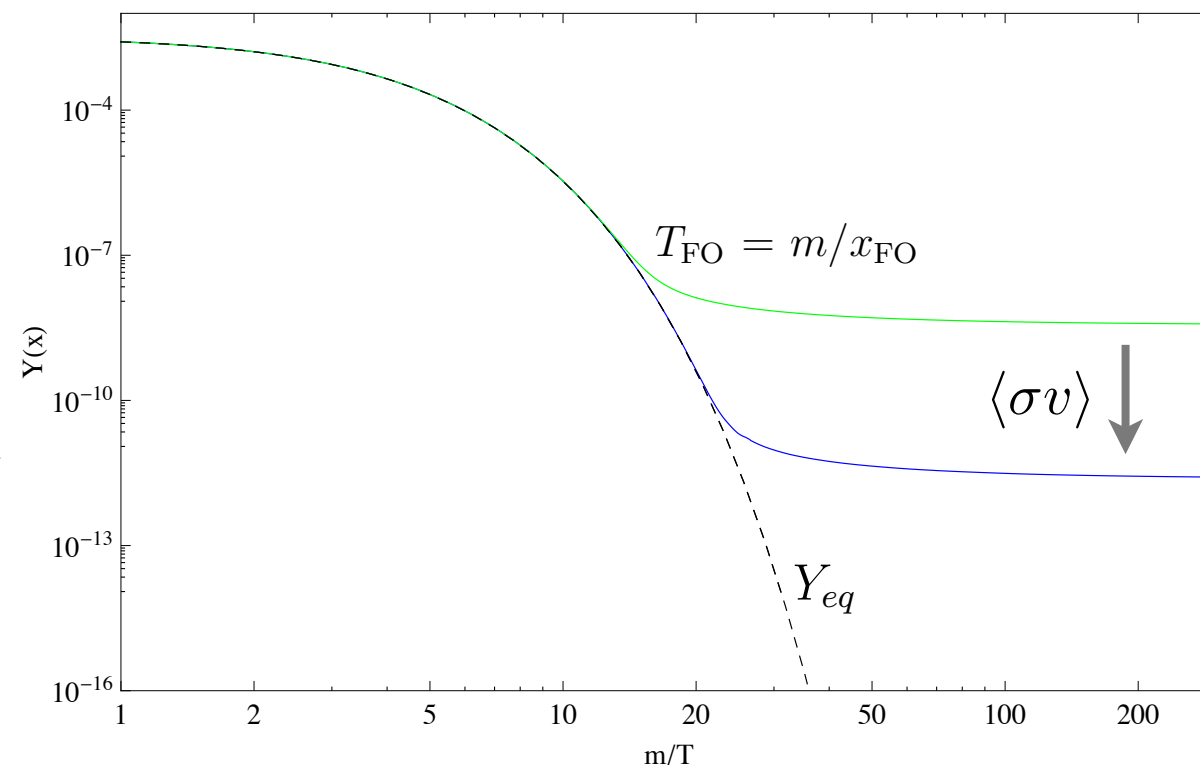
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→ $\langle\sigma v\rangle_0 \simeq 3 \times 10^{-26} \text{ cm}^3/\text{s}$



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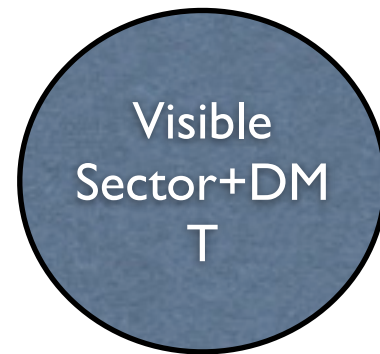
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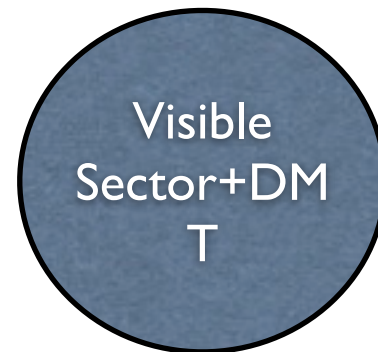


What if Dark Matter is initially decoupled from the thermal bath?

[L. Hall, K. Jedamzik, J. March-Russel, S. West arXiv:0911.1120]

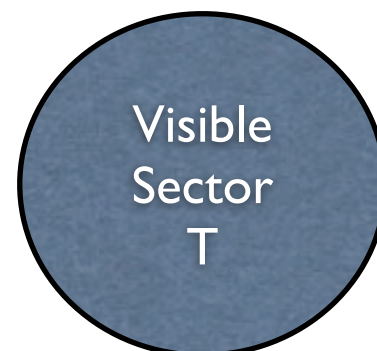
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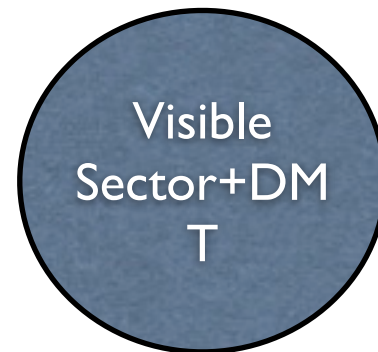
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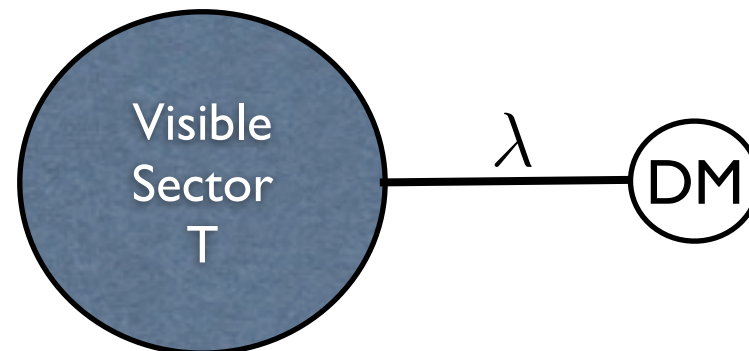


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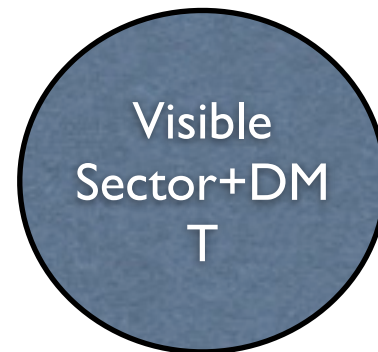
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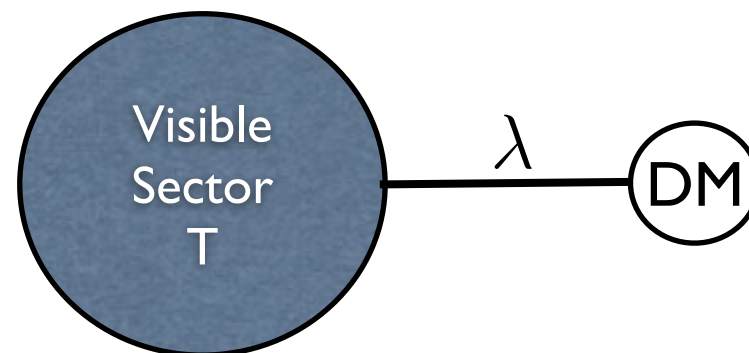


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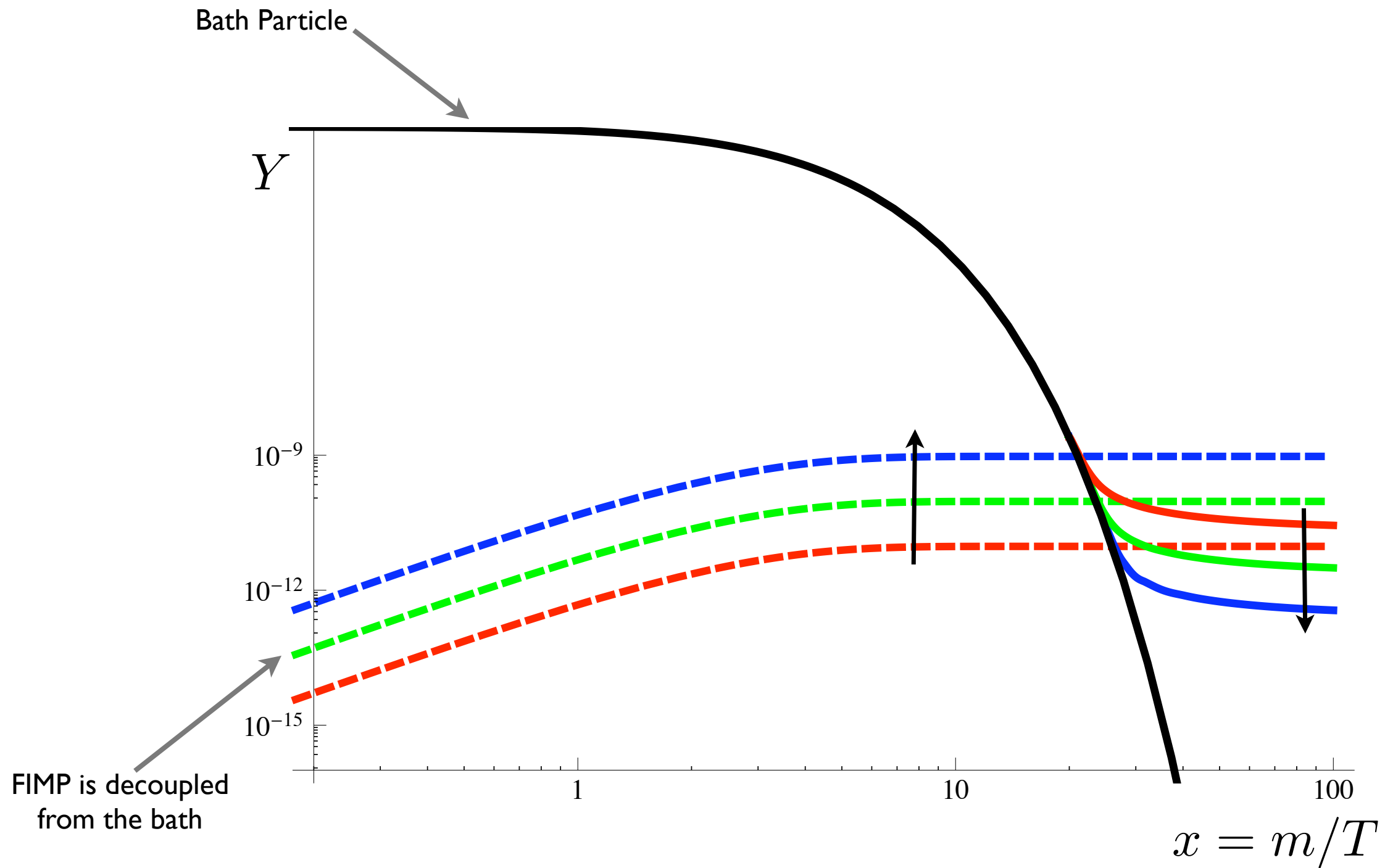
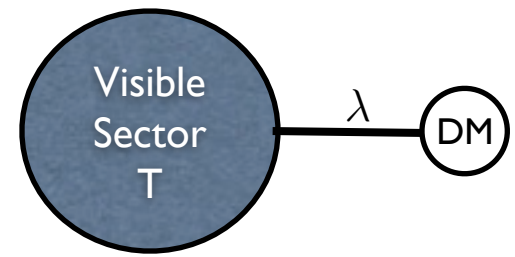
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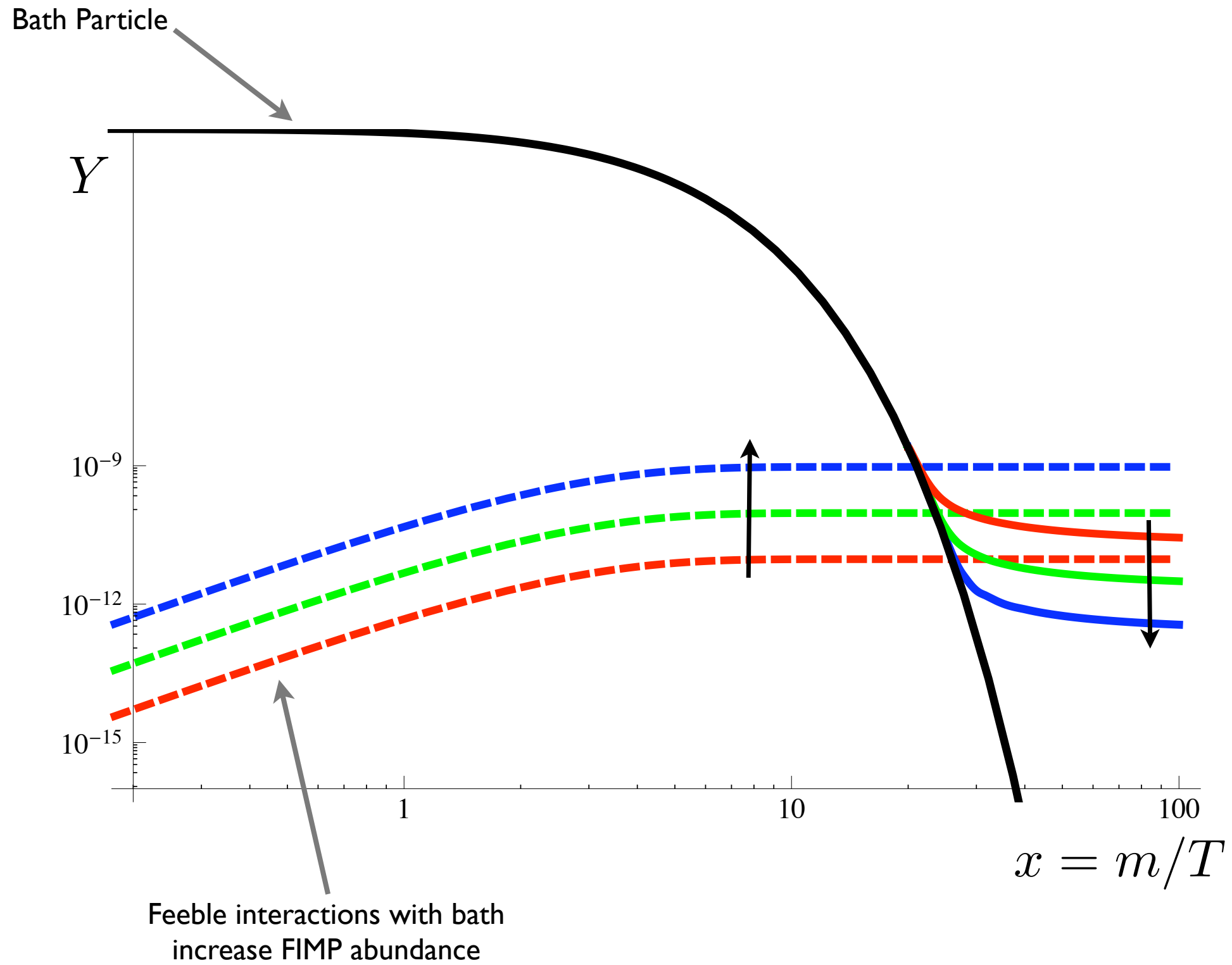
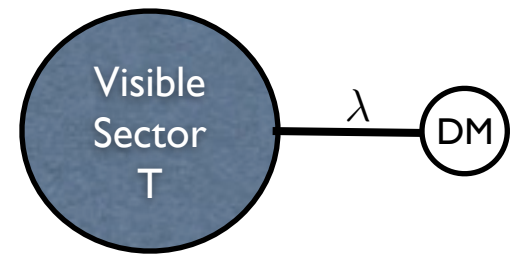
Feeble interaction allows for a new production mechanism:

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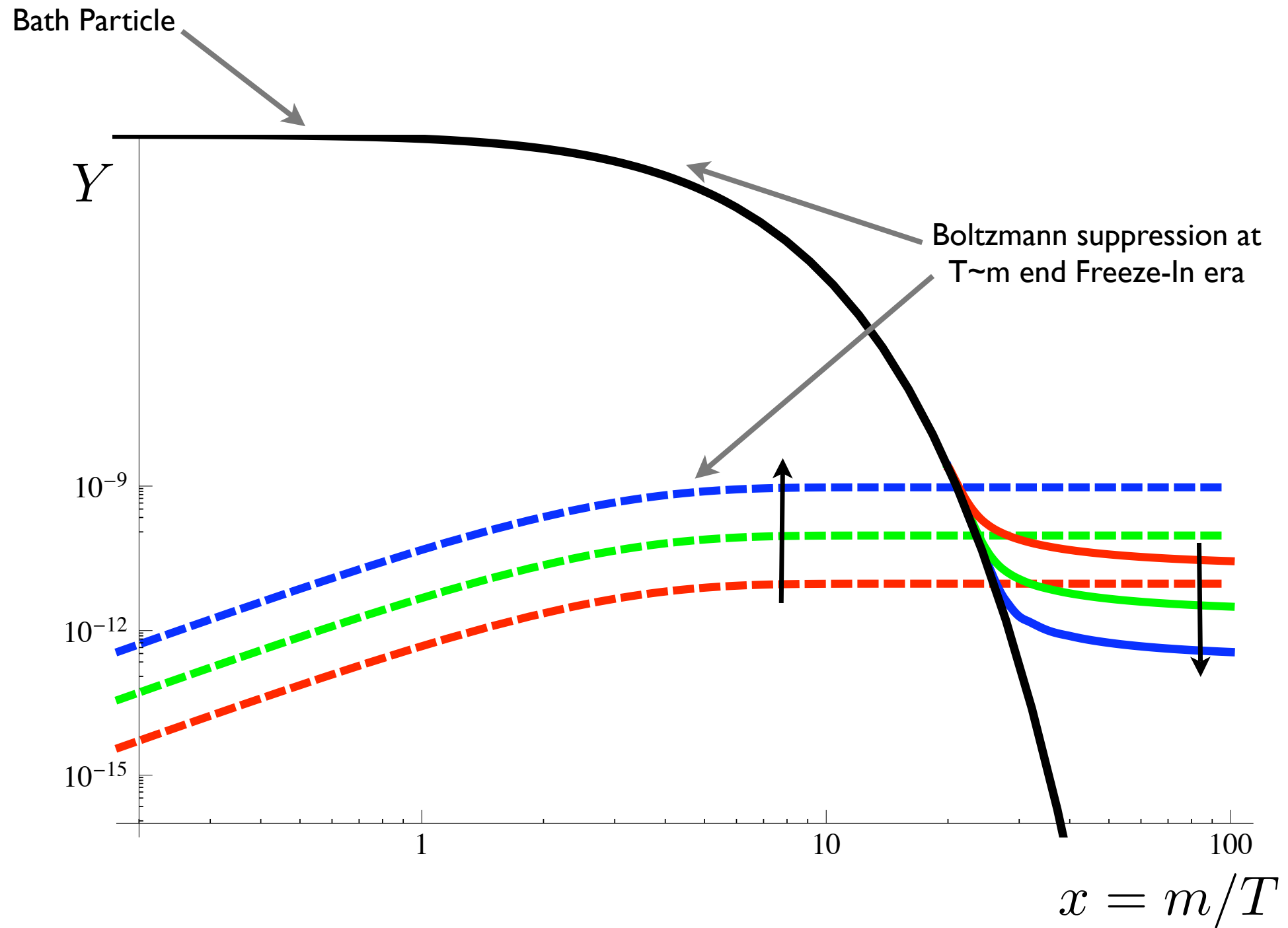
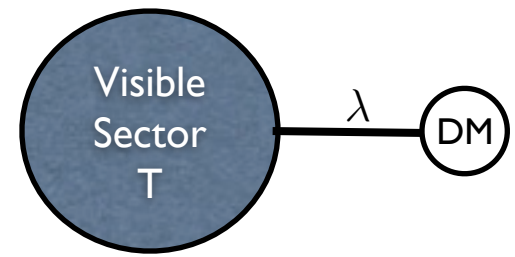
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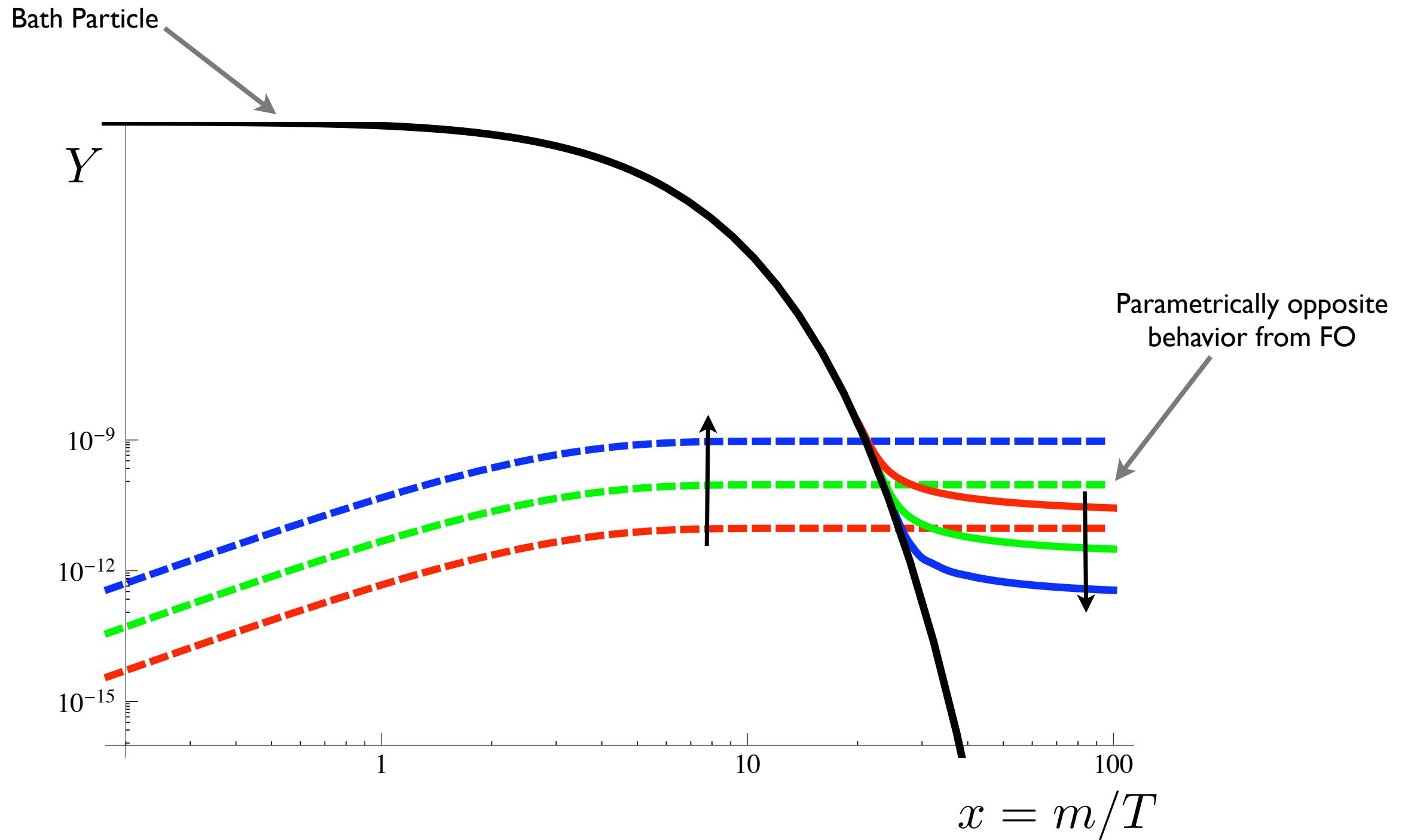
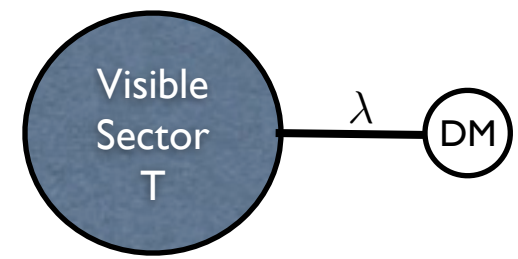
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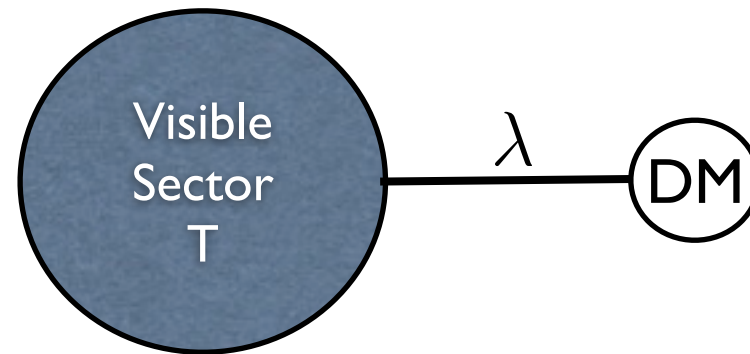
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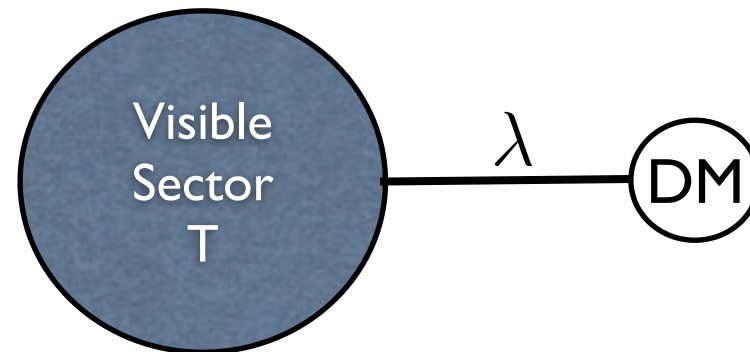
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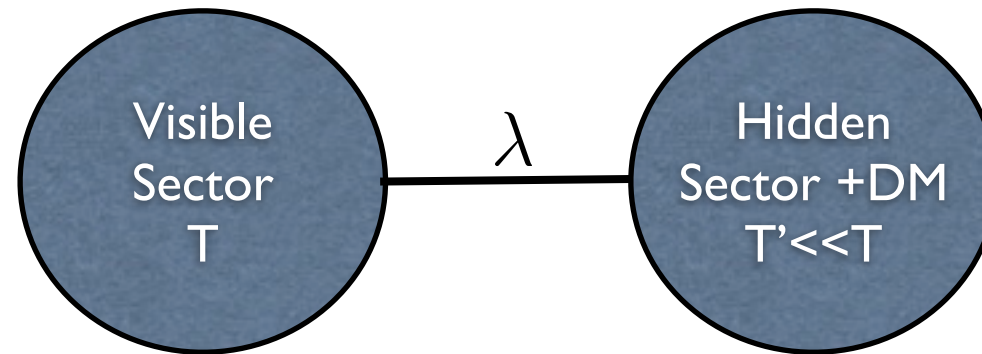


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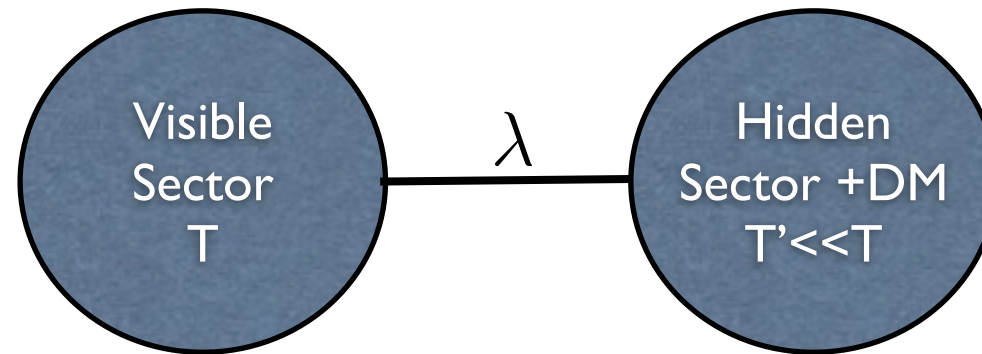
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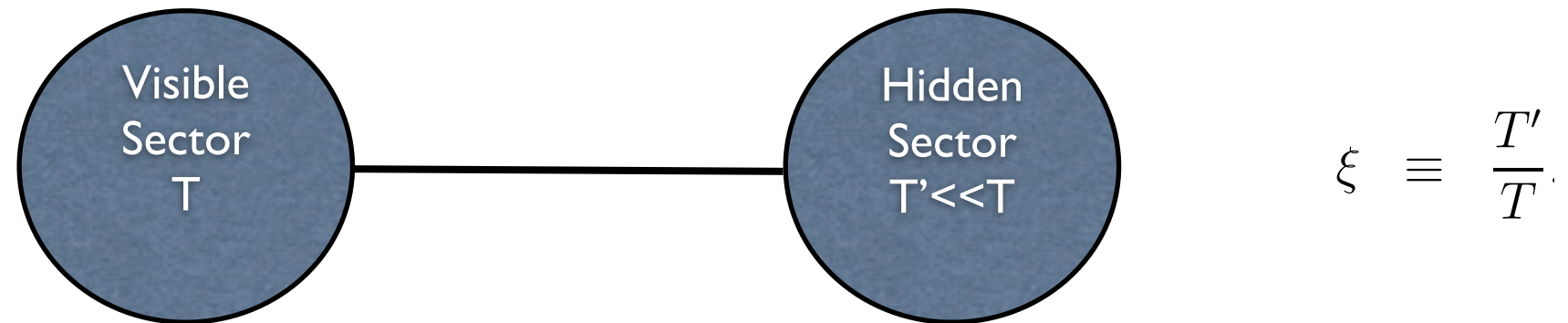
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What are the possible production mechanisms of
“Hidden Sector Dark Matter”

Cosmology arXiv:1010.0022

Hidden Sector Dark Matter

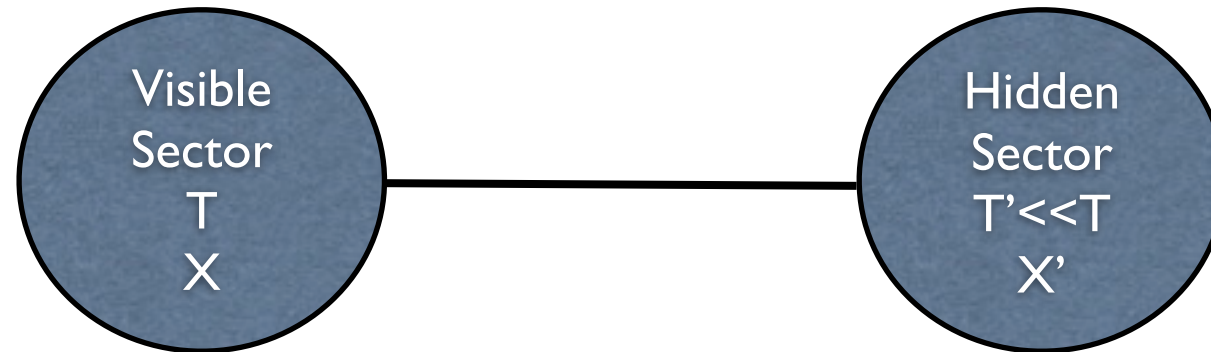
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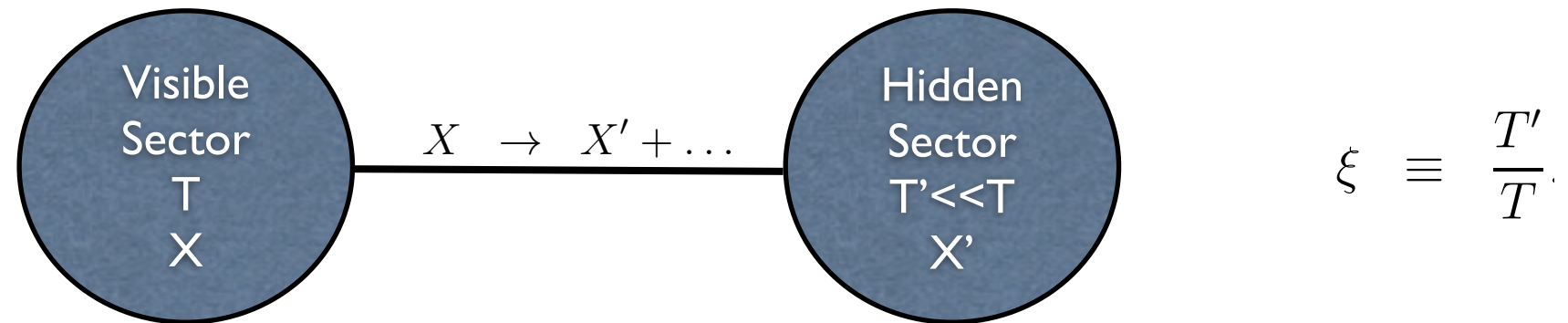


$$\xi \equiv \frac{T'}{T}$$

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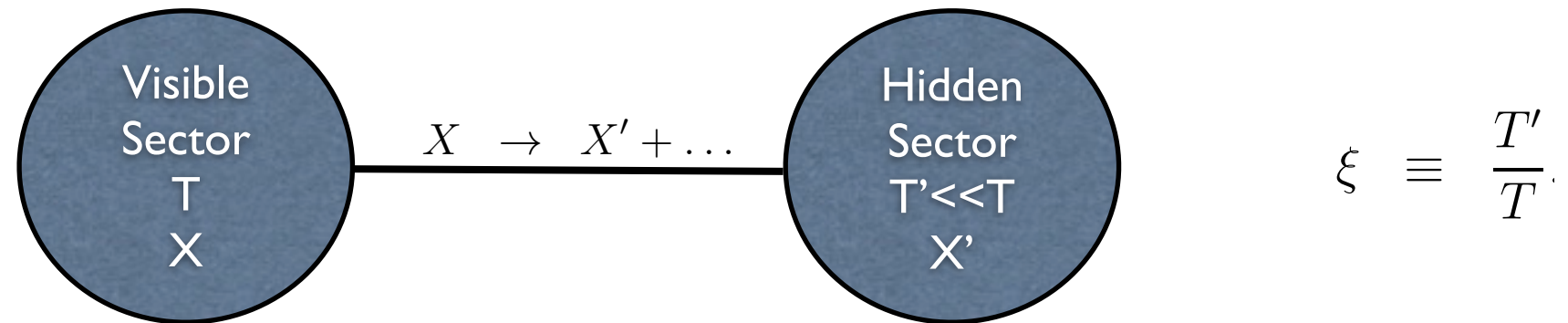
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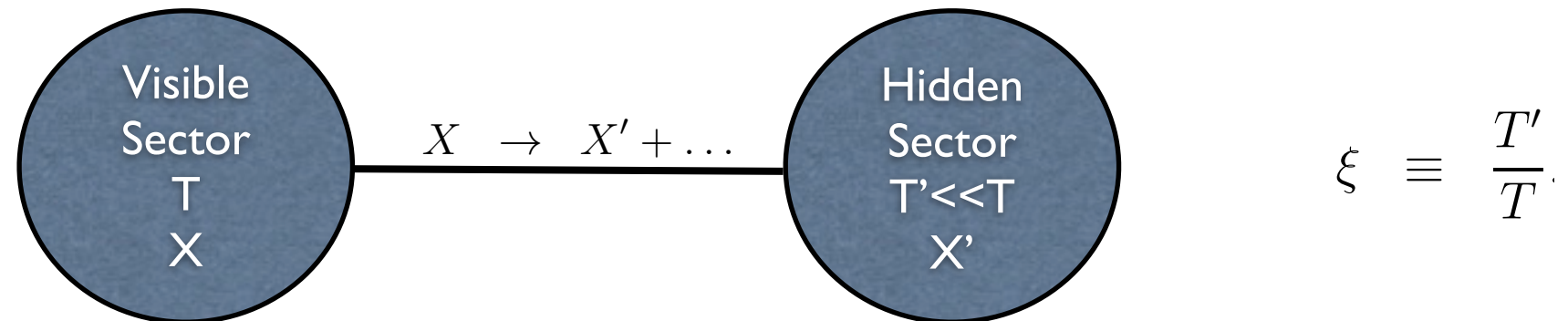


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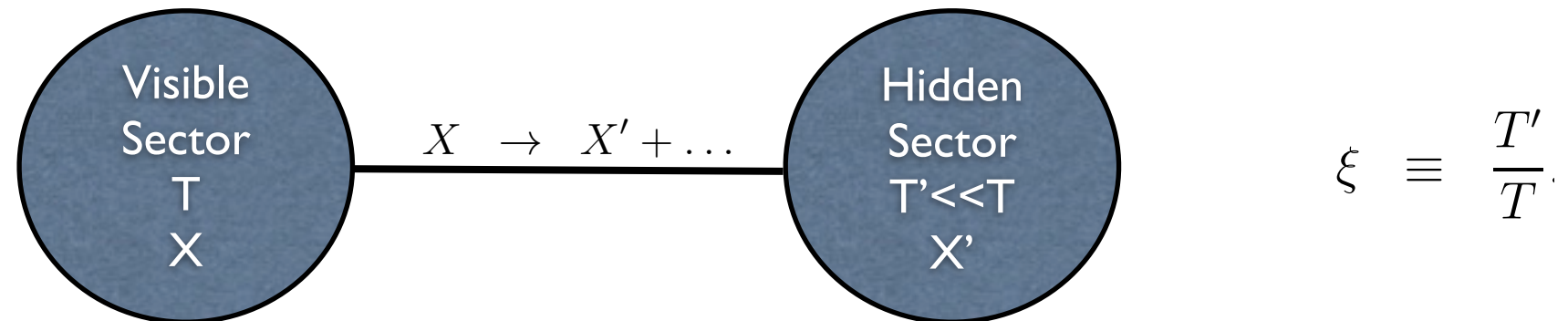
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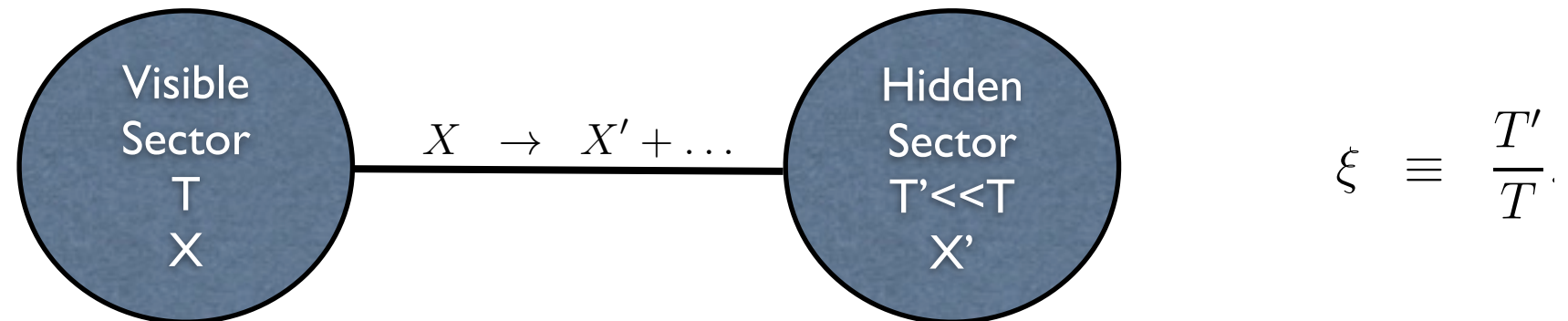
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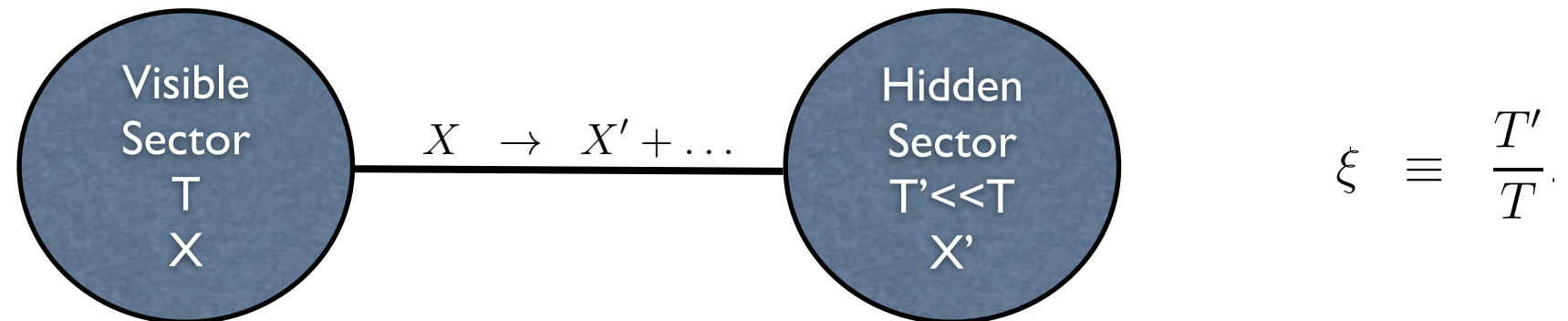
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- There exists a stabilizing symmetry. Take X/X' to be the lightest particle in the visible/hidden sector charged under the stabilizing symmetry. $m > m'$
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- Coupled Boltzmann equations:

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Decay rate of X to X'
 \sim free parameter

Hidden Sector Dark Matter

A General Set Up:



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- Seven dimensional parameter space:

$$\{m, m', \langle\sigma v\rangle, \langle\sigma v\rangle', \xi, \tau, \epsilon\}$$

Two-Sector Cosmology

- Identify reconstructable Dark Matter production mechanisms.

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Not entirely independent

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Initial condition: $\xi_{\text{inf}} = T'_{\text{inf}}/T_{\text{inf}}$

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$$\xi^4(T) = \xi_{\text{UV}}^4 + \xi_{\text{IR}}^4(T)$$

UV scattering

The free parameter

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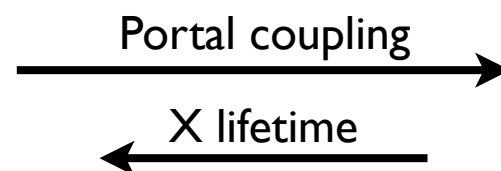
UV scattering

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Calculable

Two-Sector Cosmology

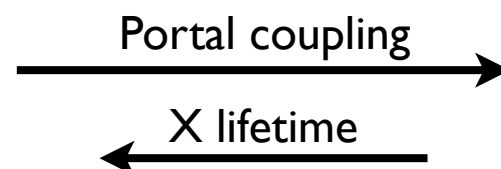
General behavior can be understood in terms of size of portal coupling



Two-Sector Cosmology

General behavior can be understood in terms of size of portal coupling

Multi-Component: X is stable,
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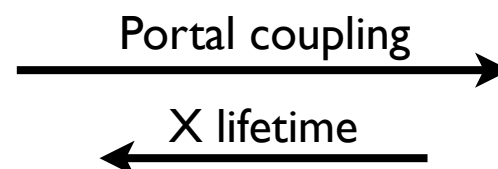
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Freeze-Out and Decay: X Freezes
out and late decays to X'



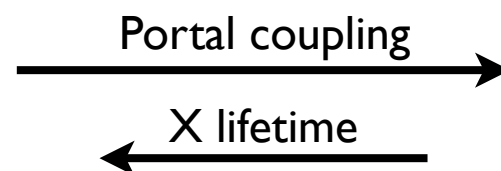
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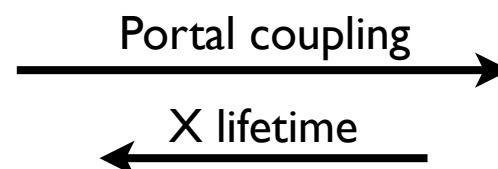
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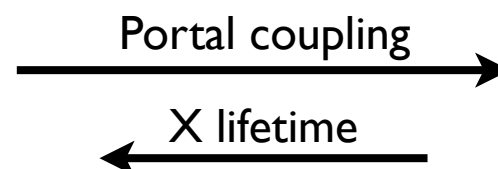
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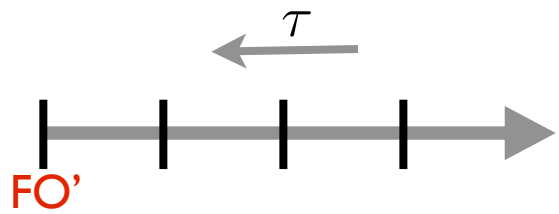
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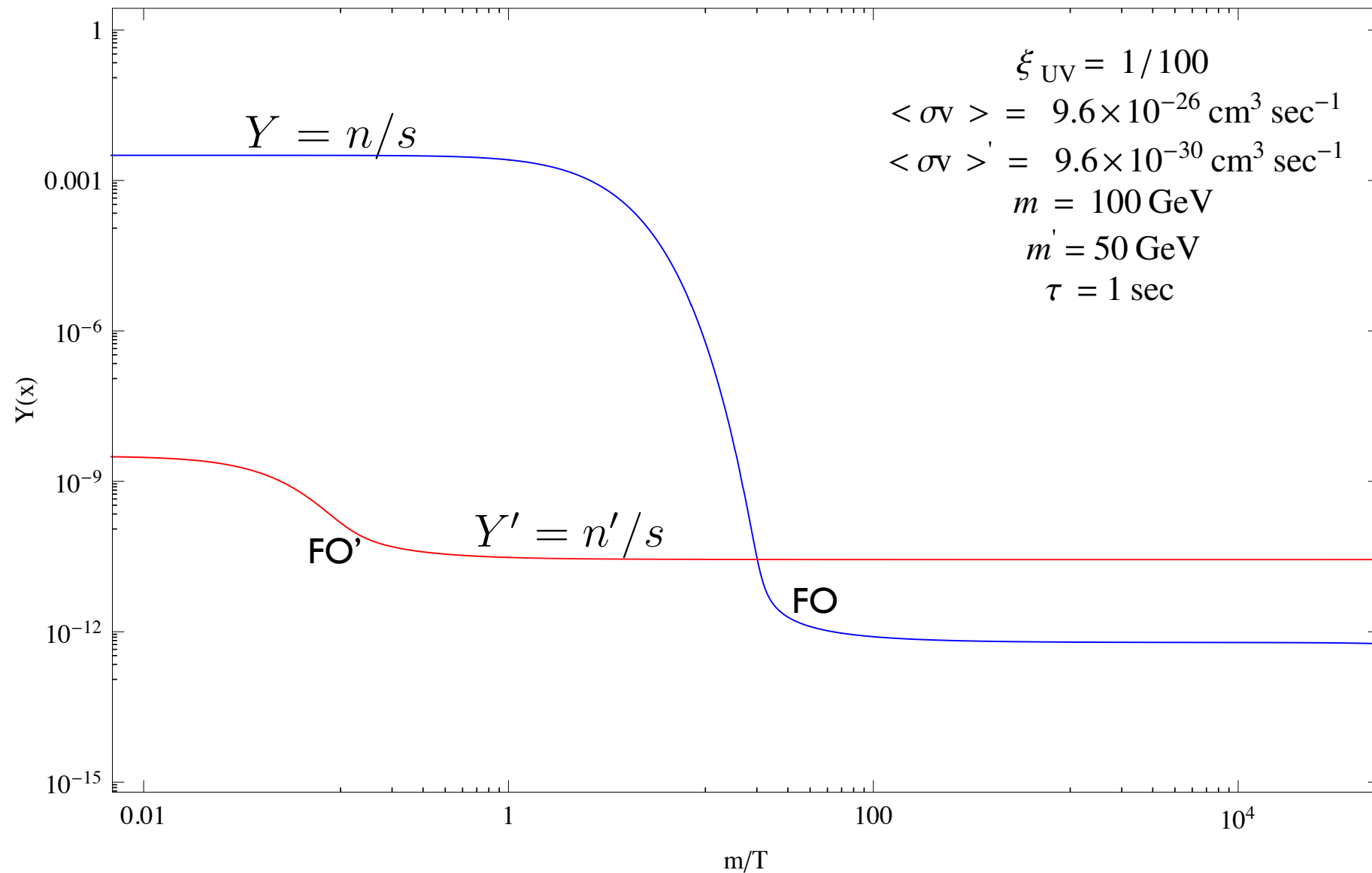


We see this numerically by solving the Boltzmann equations...

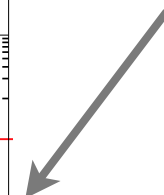


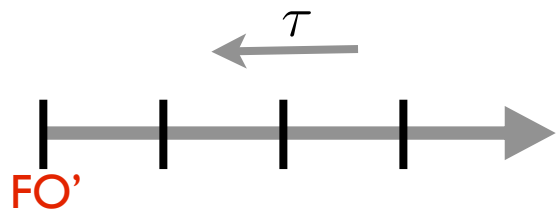
Hidden Sector Freeze-Out

J.L Feng, H.Tu, H.B.Yu hep-ph/0404198



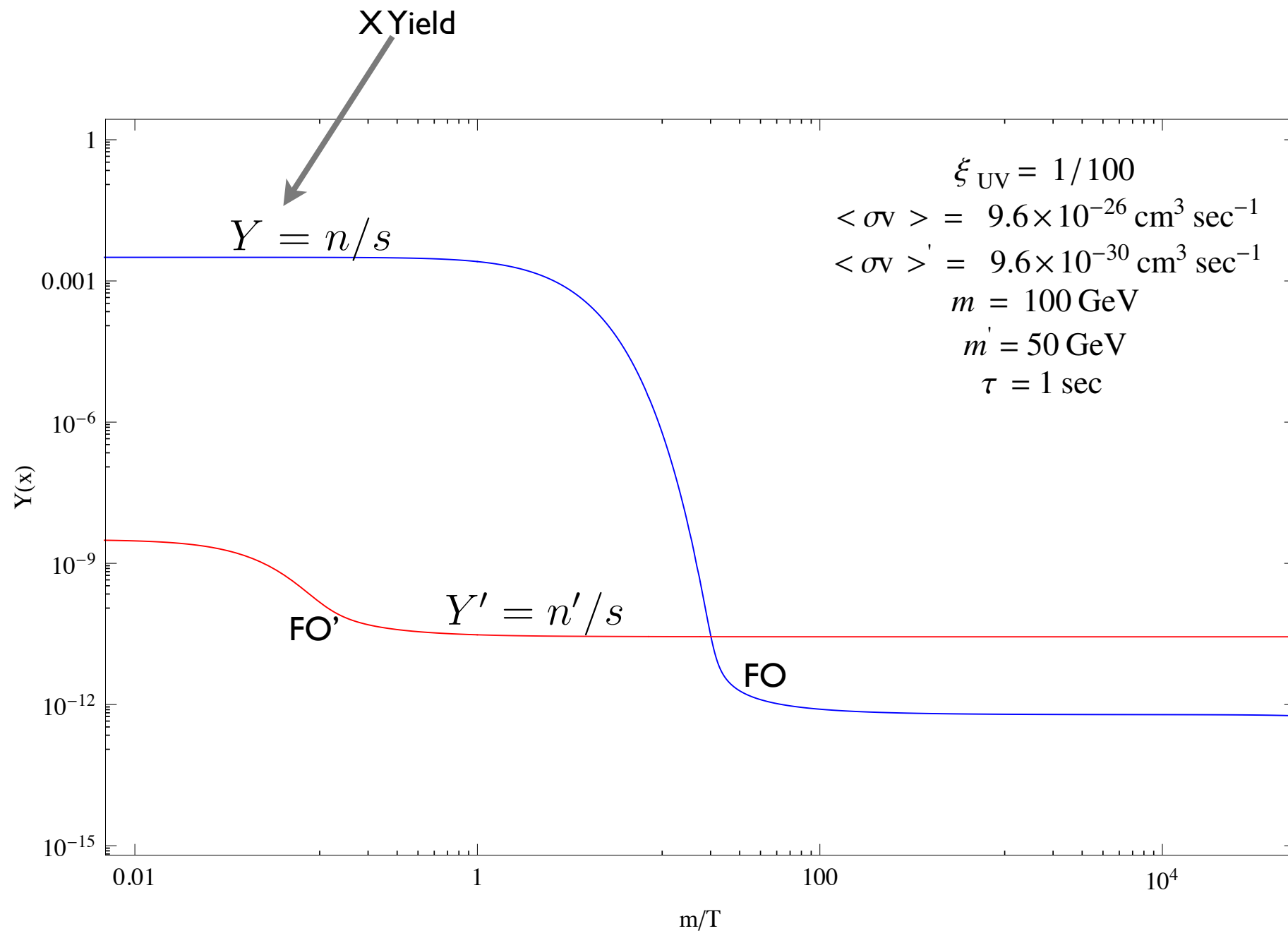
X is very long lived,
sectors effectively
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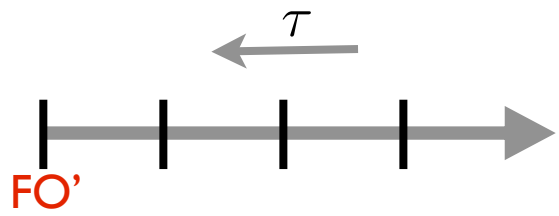


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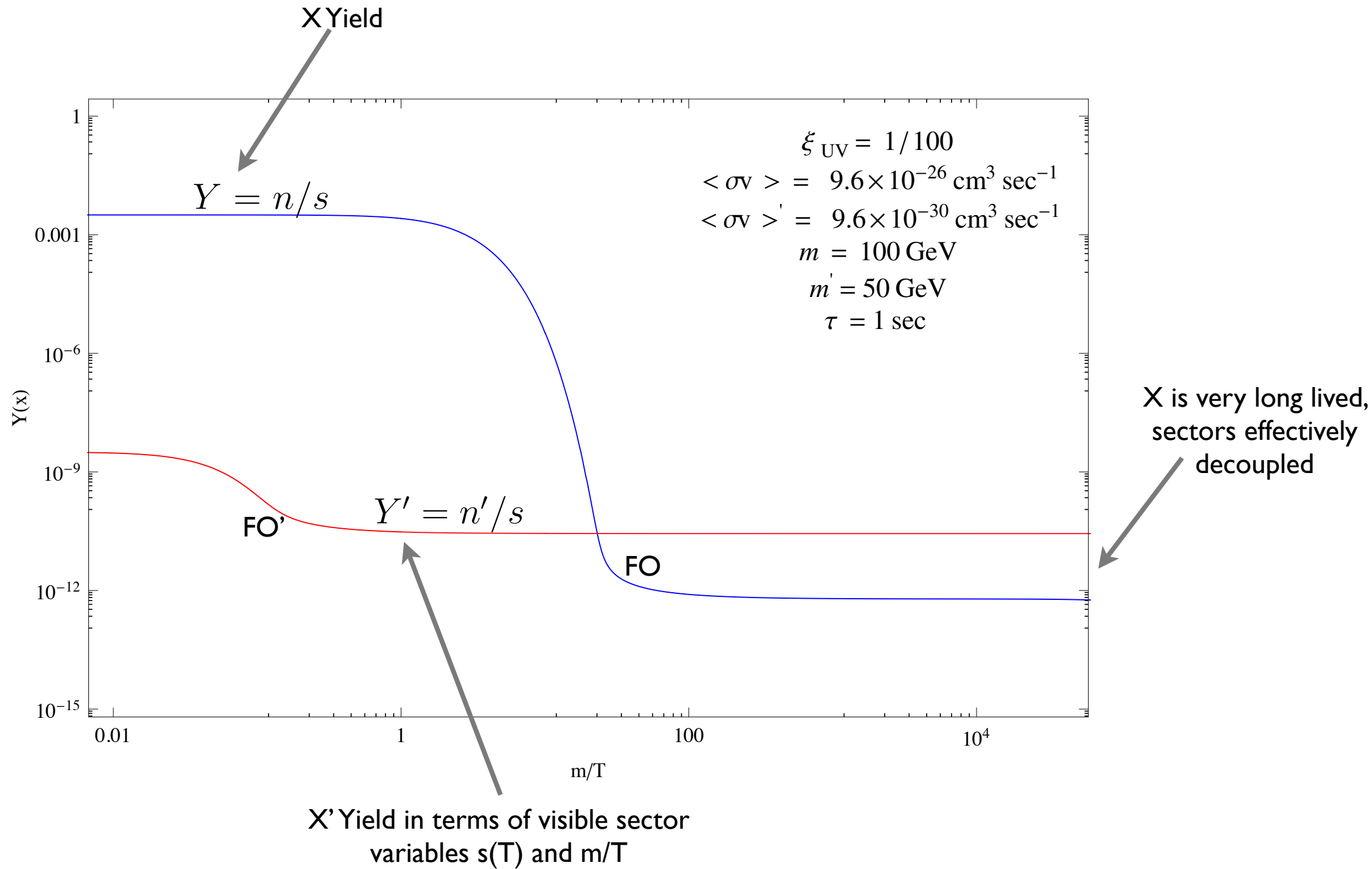


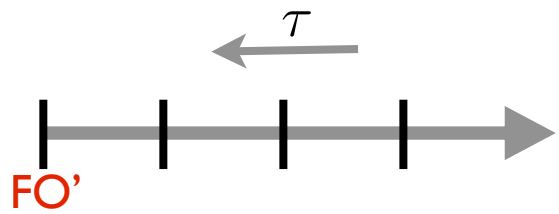
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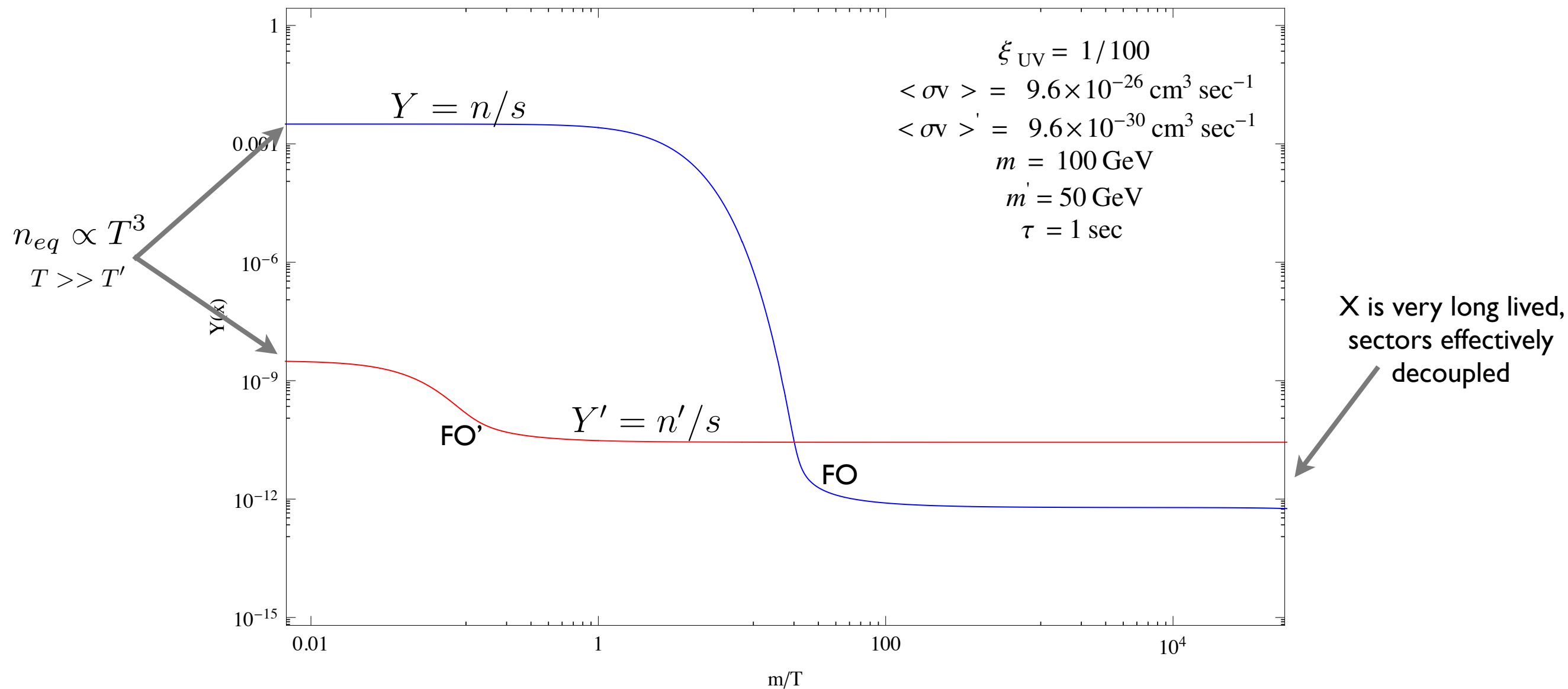
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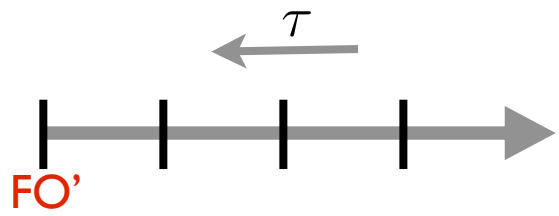




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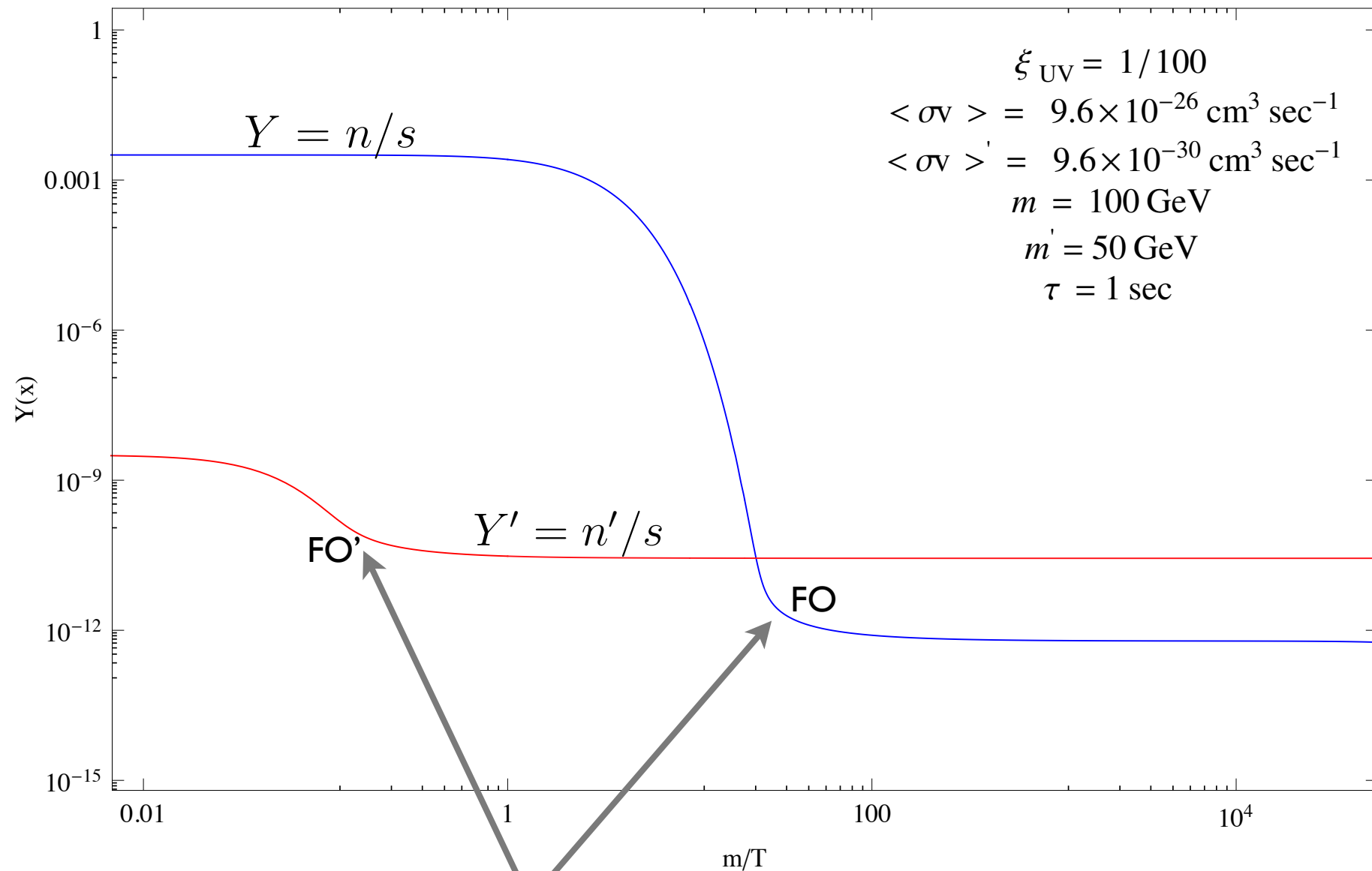
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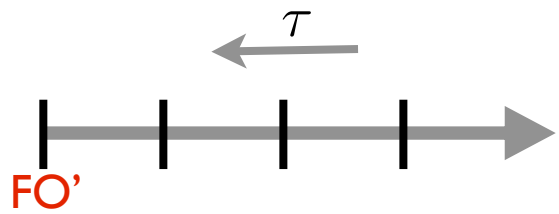
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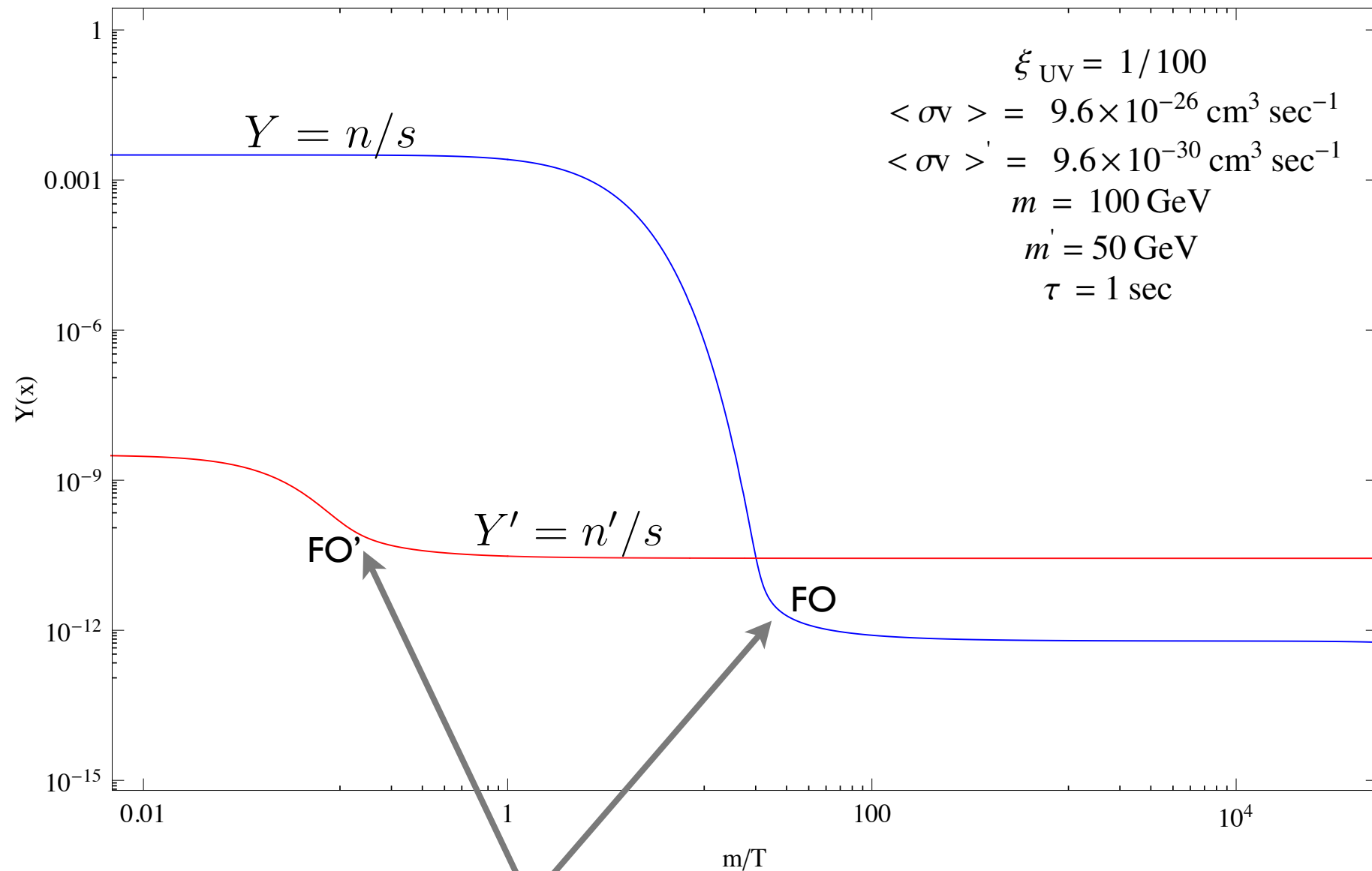
$$\frac{T_{FO'}}{T_{FO}} = \frac{1}{\xi_{FO'}} \frac{m'}{m}$$

Focus on the case where FO' occurs before FO



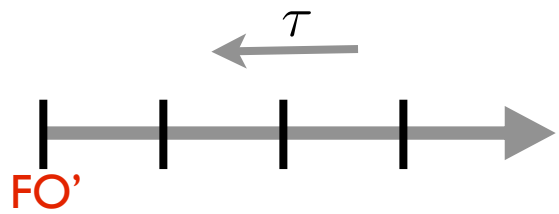
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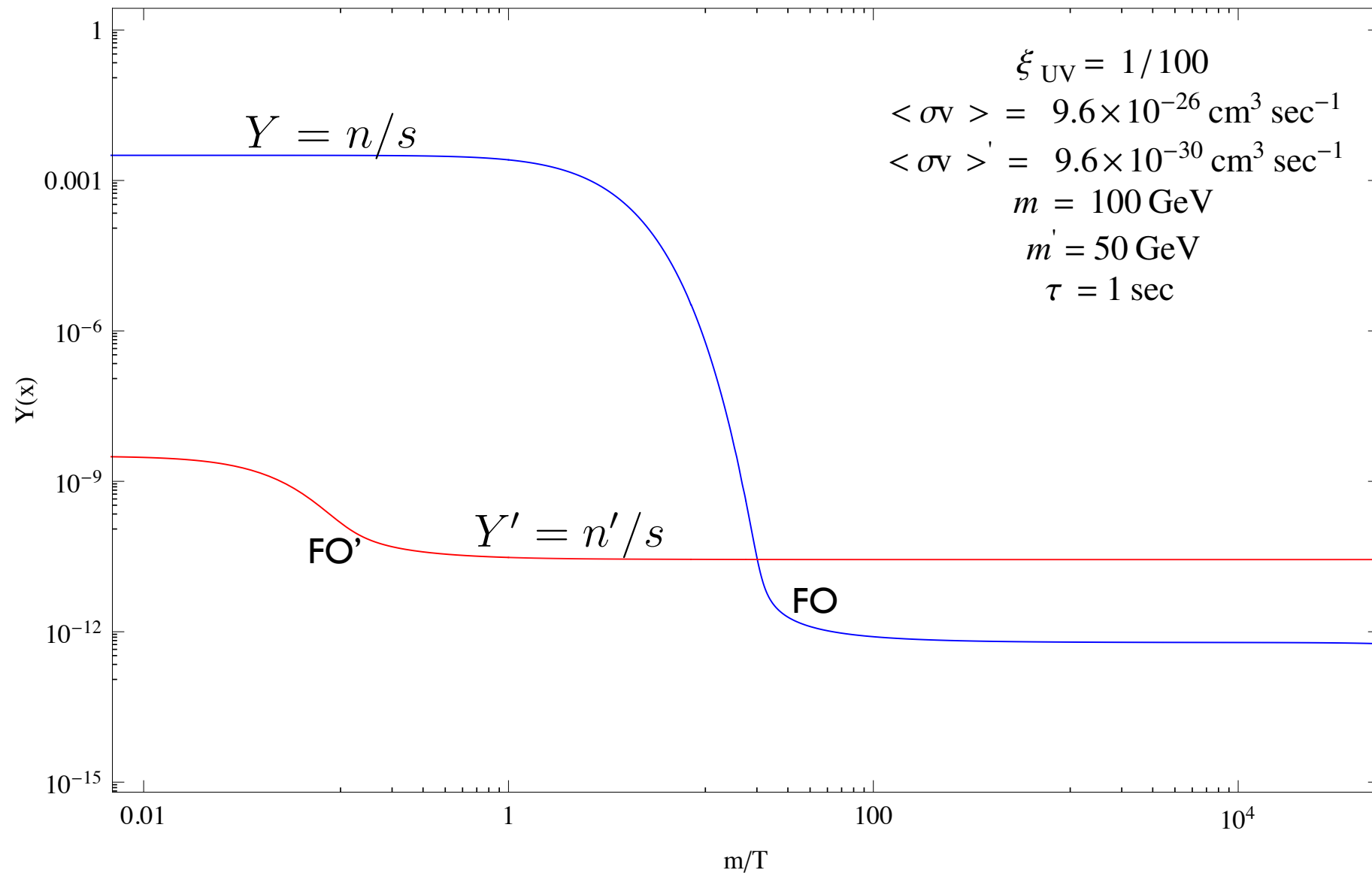
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$\langle \sigma v \rangle' \ll \langle \sigma v \rangle$ Hidden sector interactions not too strong so that FO' dominates over FO



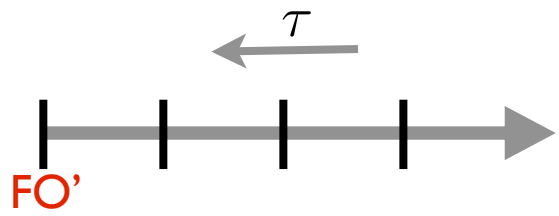
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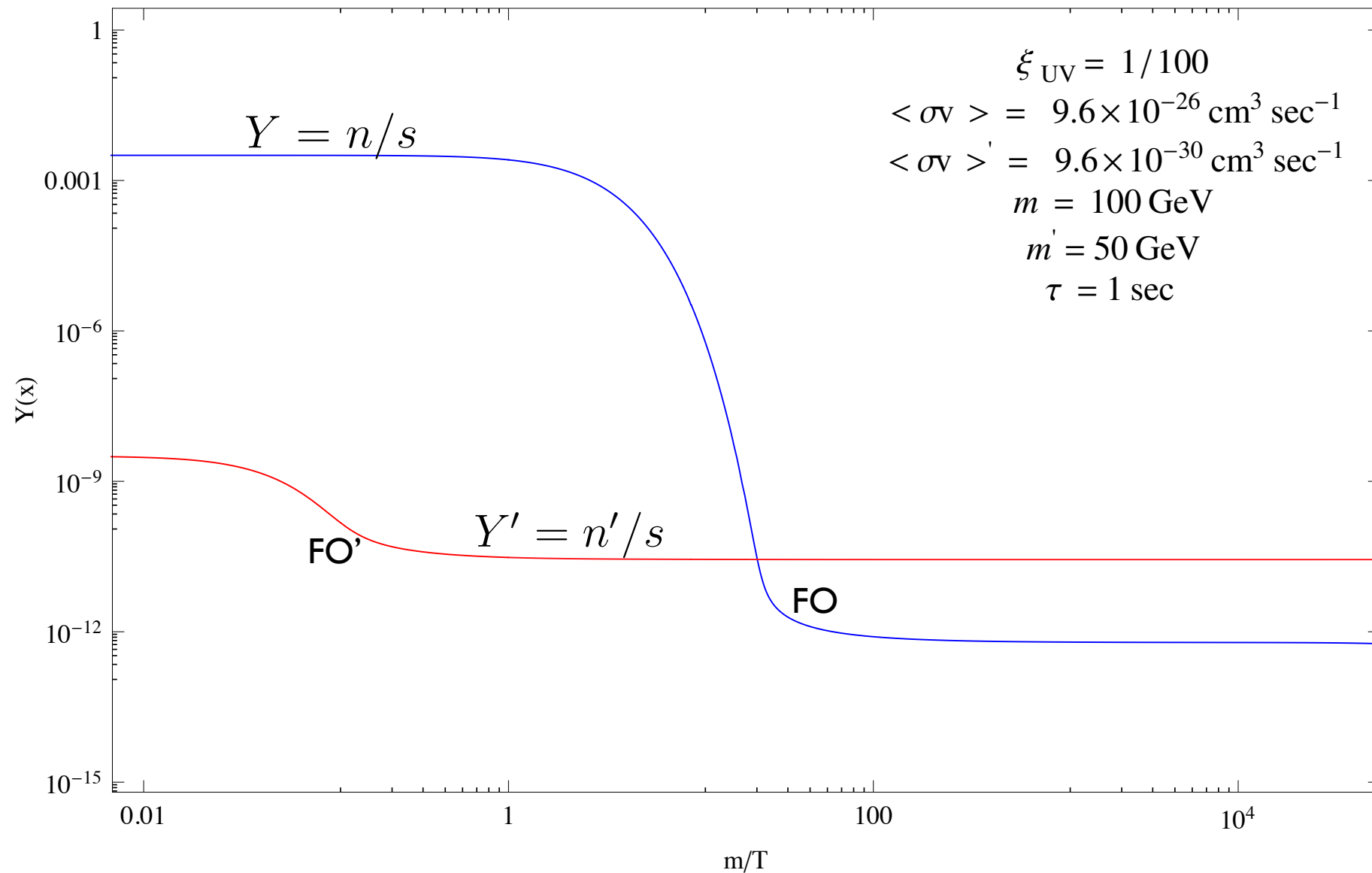
“Freeze out with hidden sector variables”:

$$Y'_{FO'} \propto \frac{\xi_{FO'}}{m' \langle \sigma v \rangle'}$$



Hidden Sector Freeze-Out

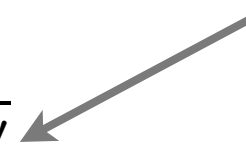
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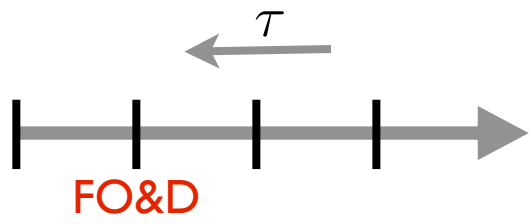


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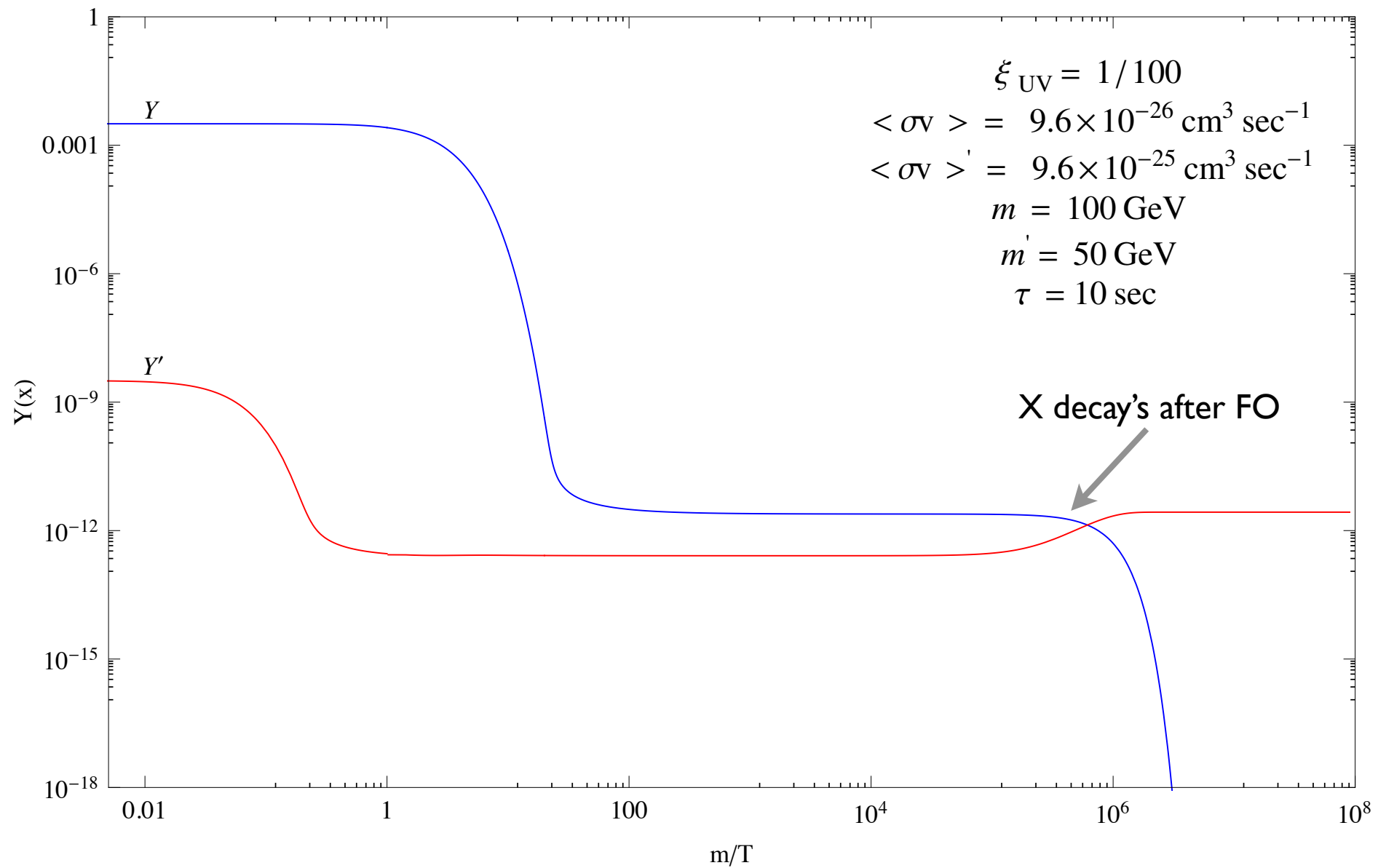
Not reconstructable

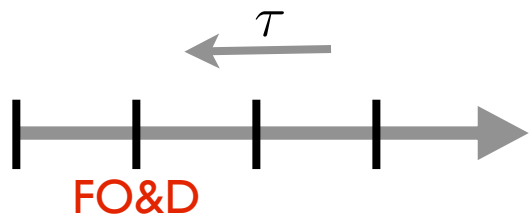




Freeze-Out and Decay

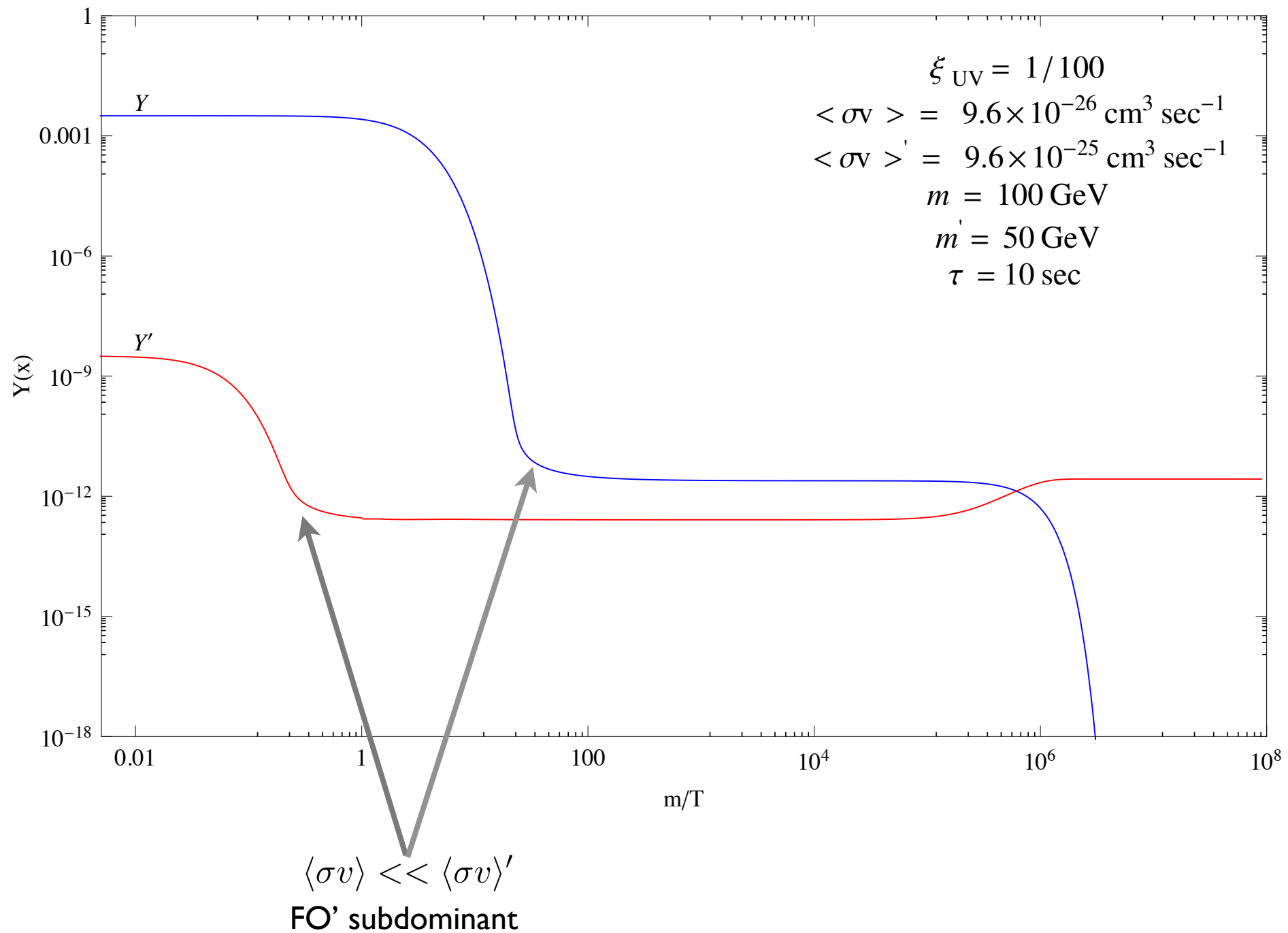
(Same mechanism but different setup from SuperWIMPs)

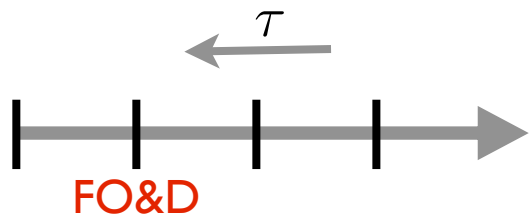




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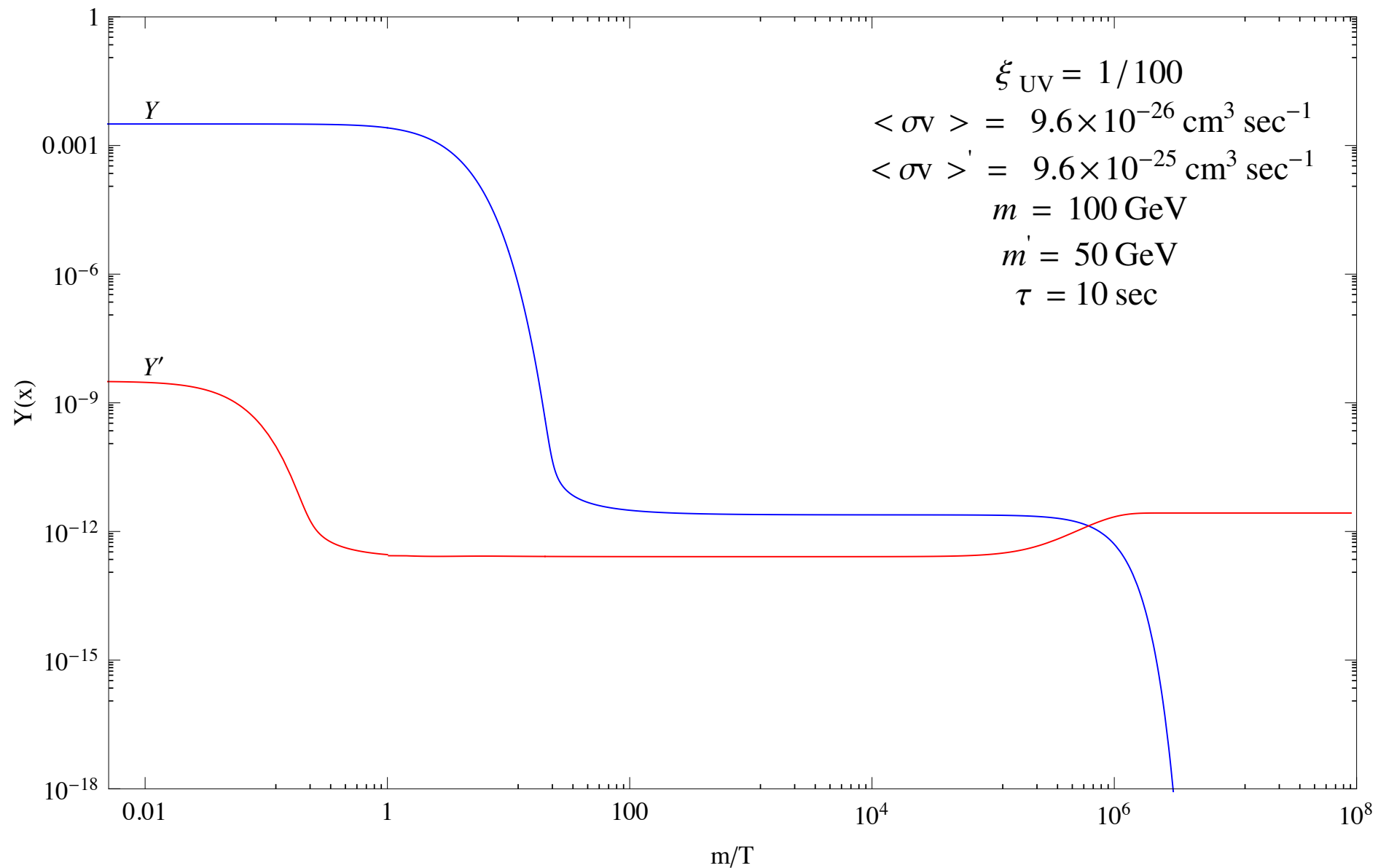
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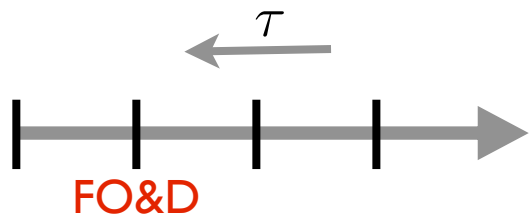


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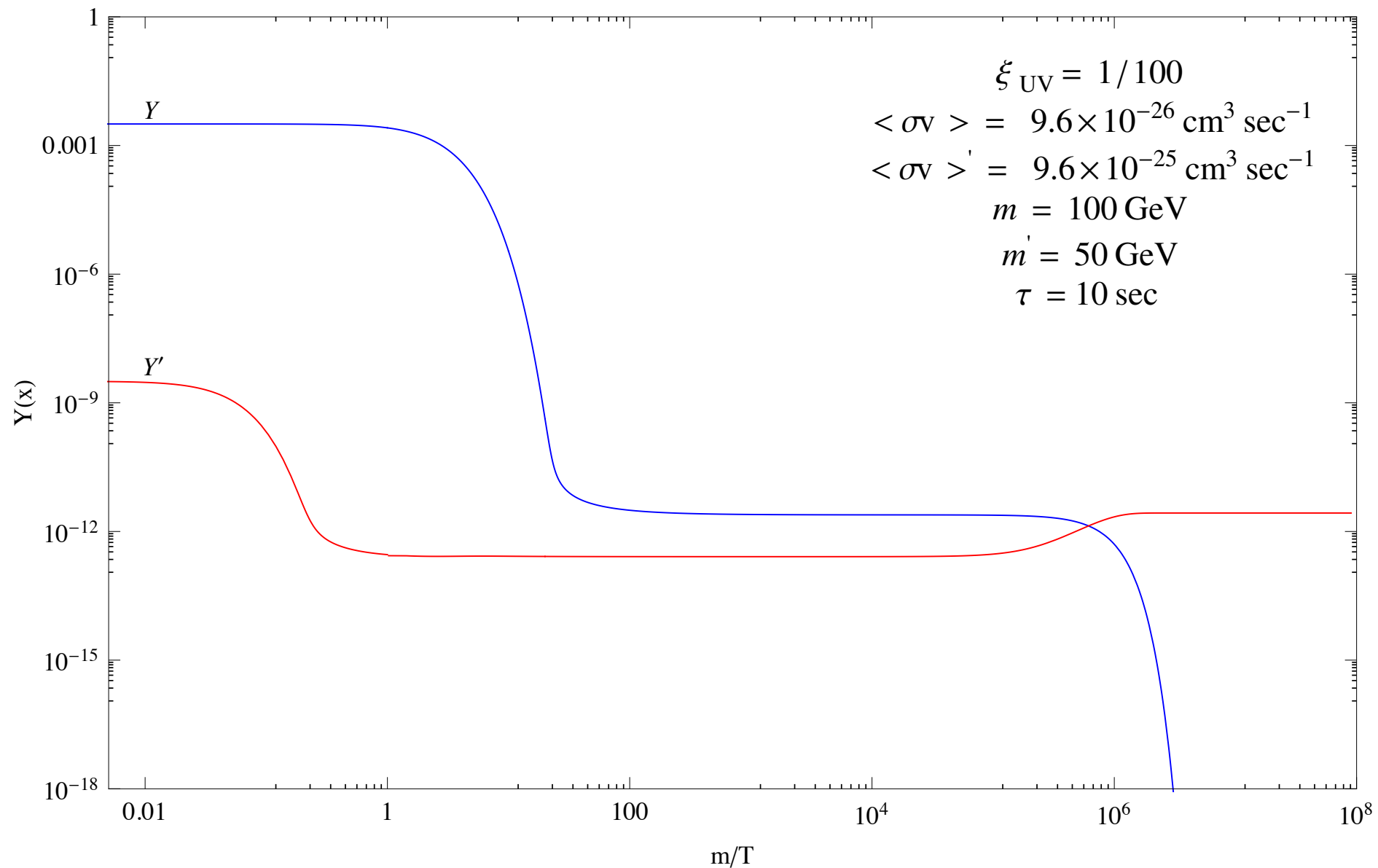


Every X decay yields exactly one X': $Y'_{\text{FO\&D}} = Y_{\text{FO}}$

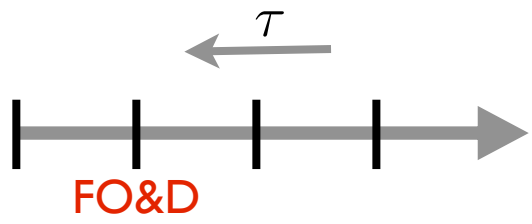


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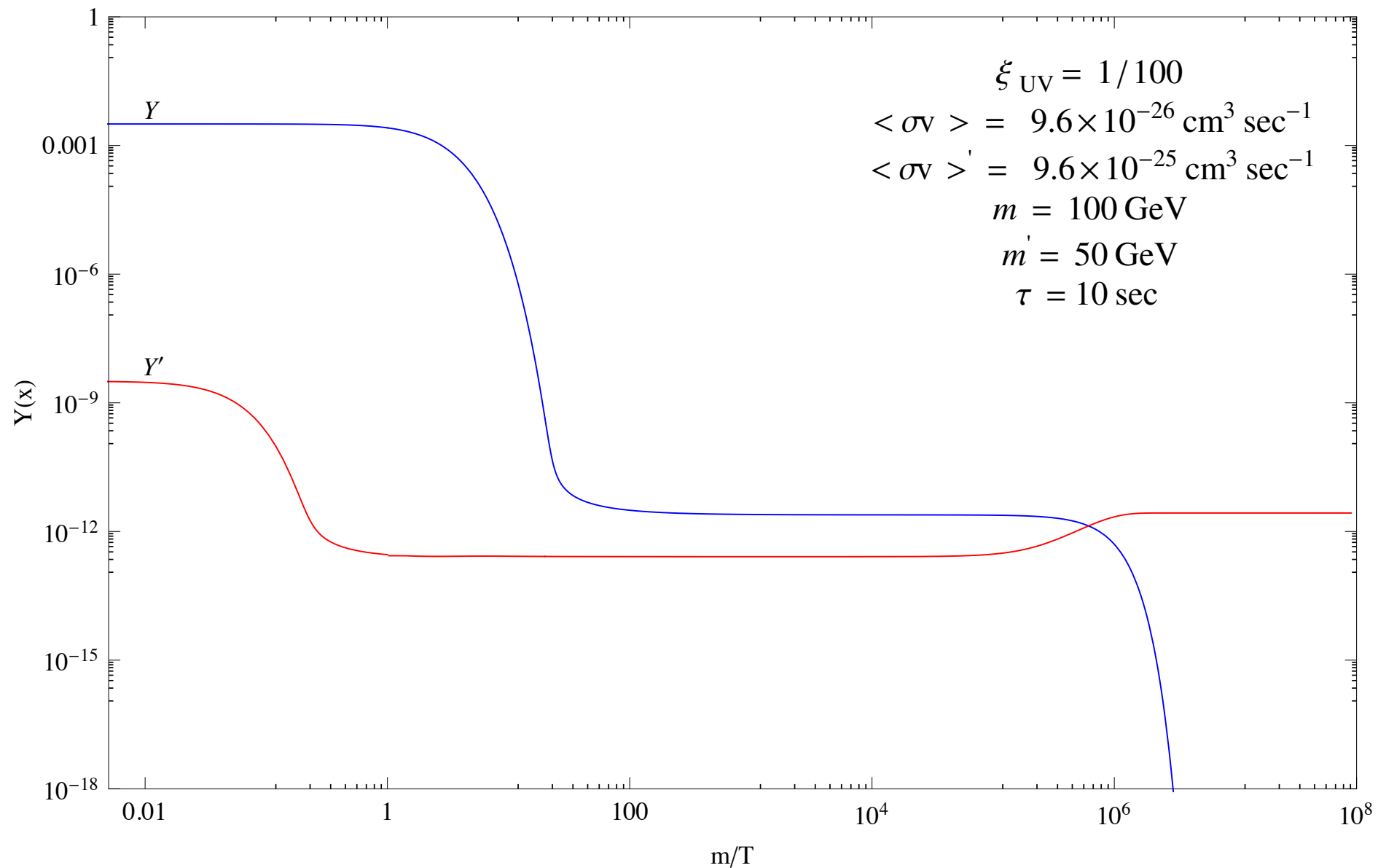


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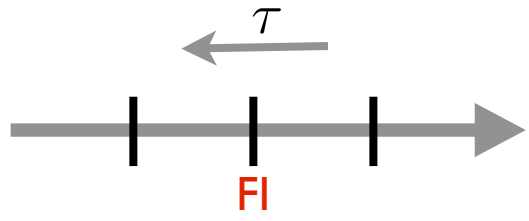
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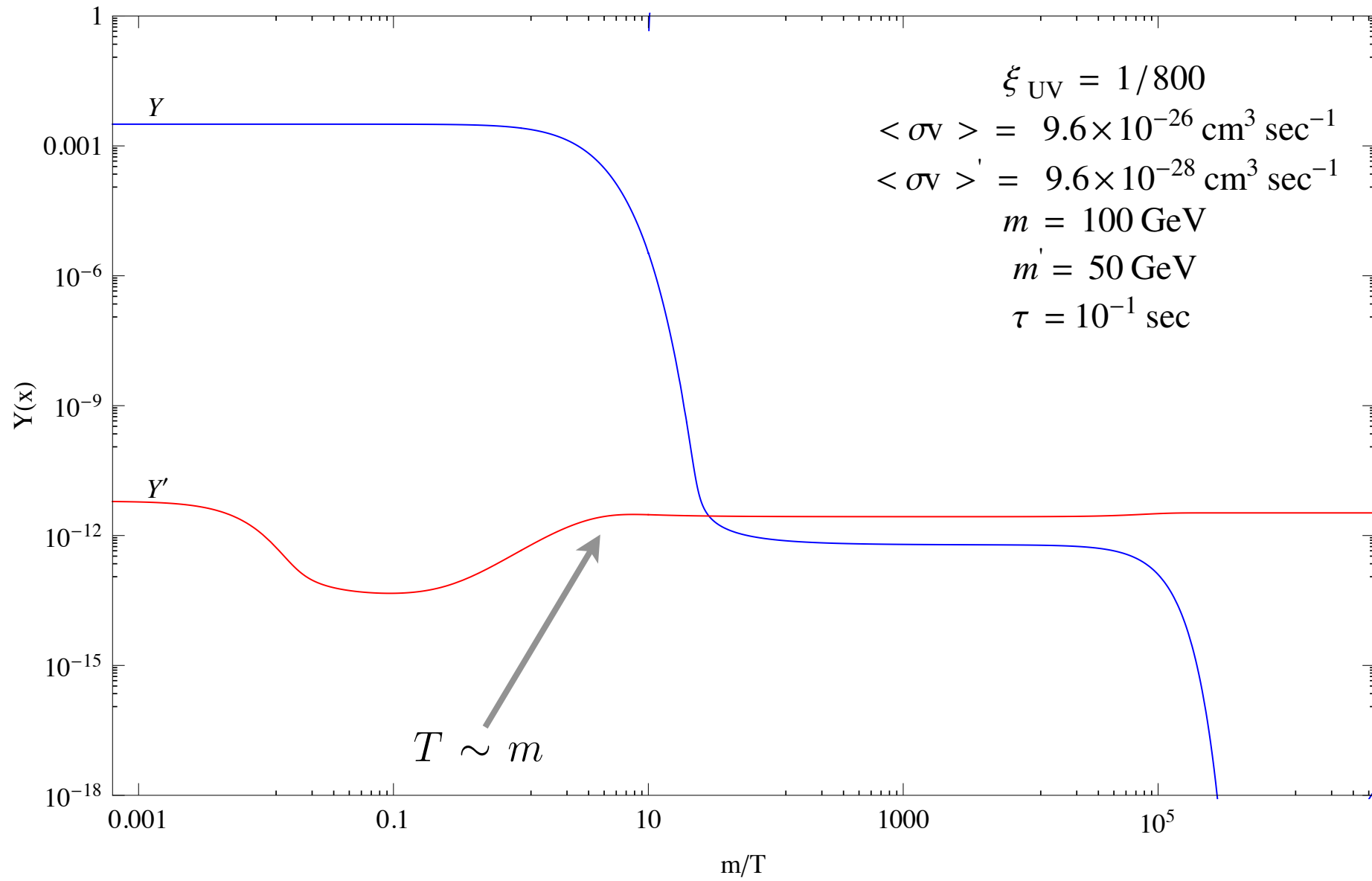


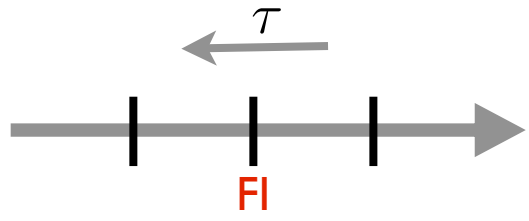
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Reconstructable by measuring: $m, m', \langle \sigma v \rangle$

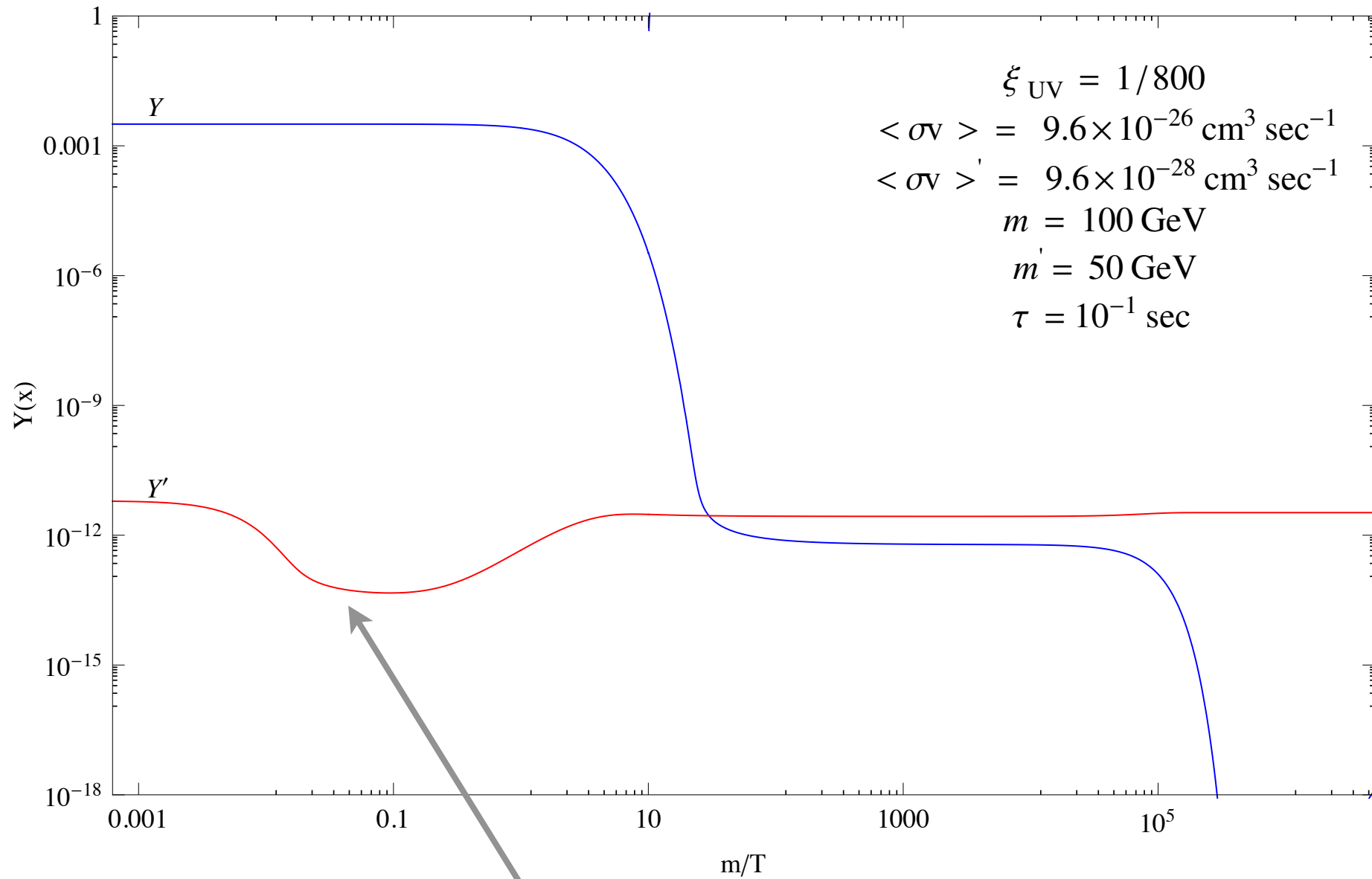


Freeze-In

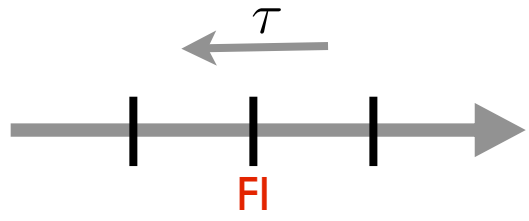




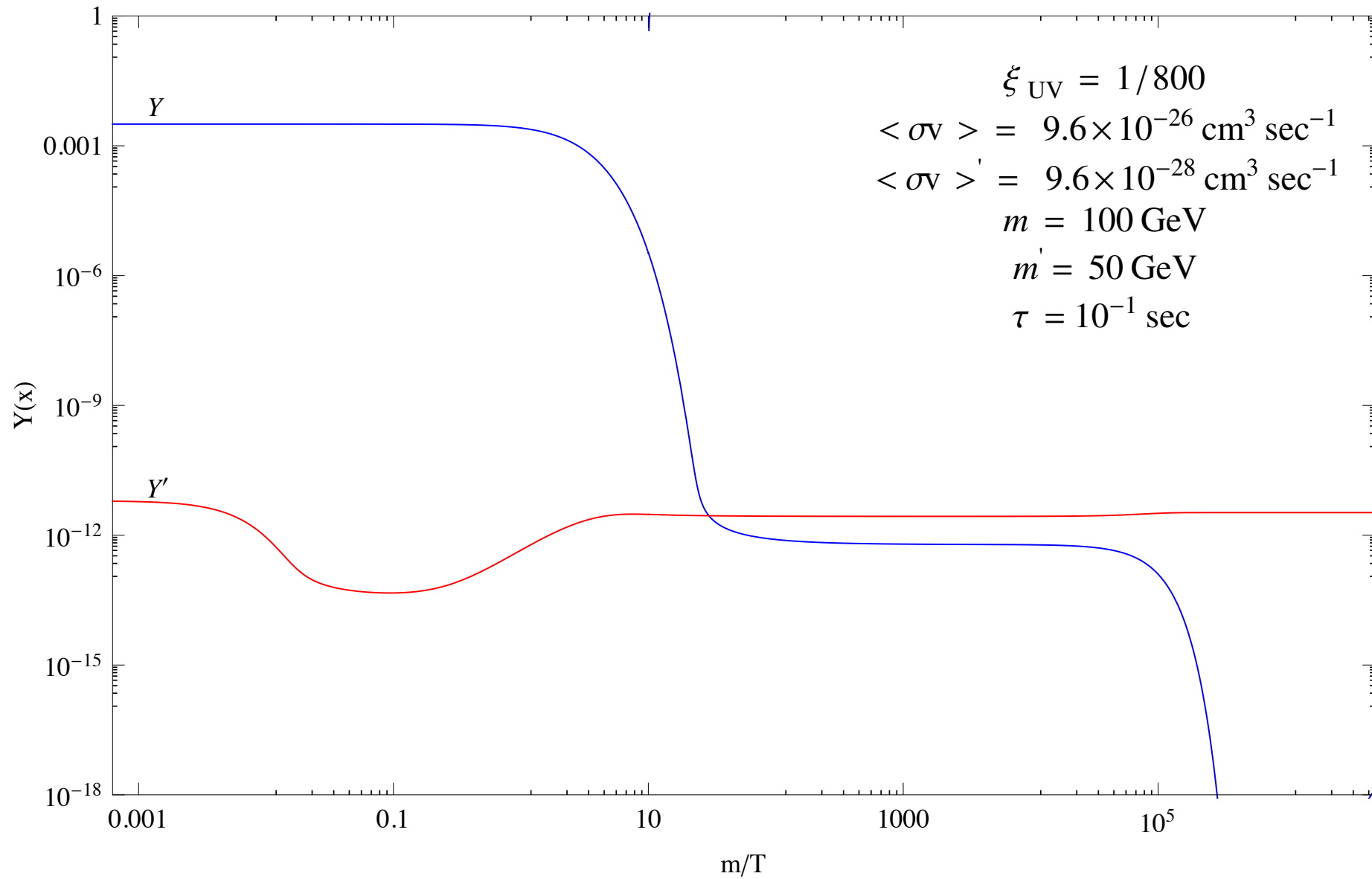
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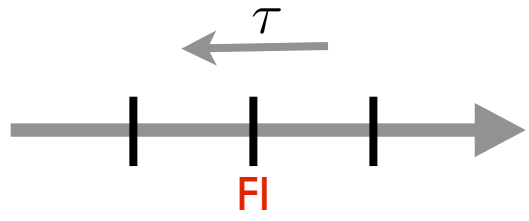
Note for FI to be effective it
must occur after FO'



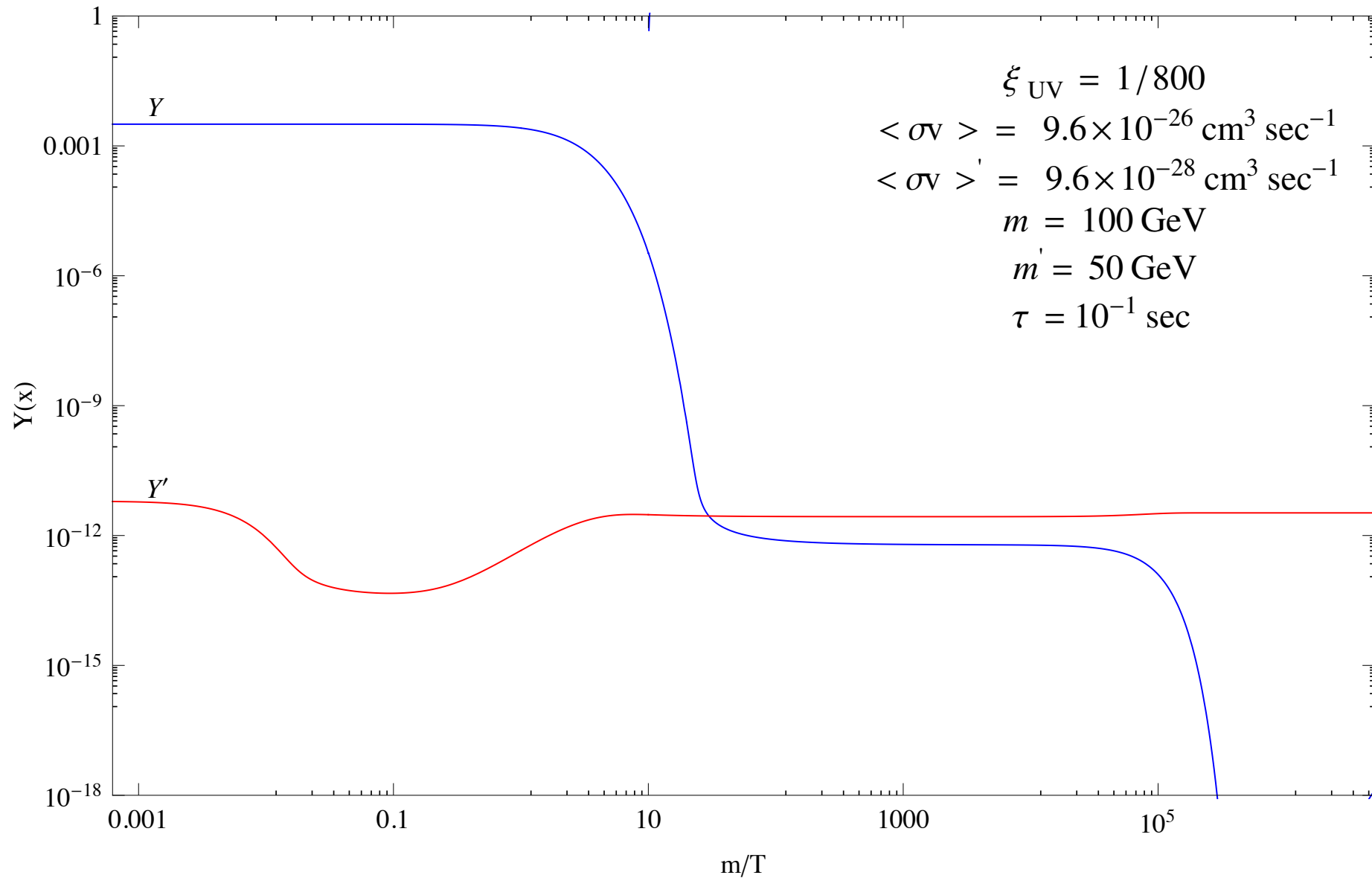
Freeze-In



Decay term dominates the Boltzmann equations: $Y'_{FI} \propto \frac{1}{\tau m^2} \rightarrow \Omega \propto \frac{m'}{m^2 \tau}$



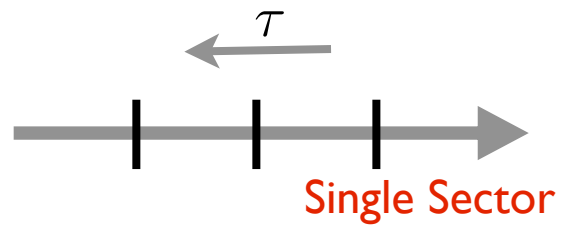
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$$\Omega_{DM} h^2 \sim 0.11 \rightarrow \tau \simeq (4 \times 10^{-2} \text{ s}) \left(\frac{m'}{m} \right) \left(\frac{100 \text{ GeV}}{m} \right) \left(\frac{228.5}{g_*} \right)^{3/2} \quad \text{Reconstructable}$$

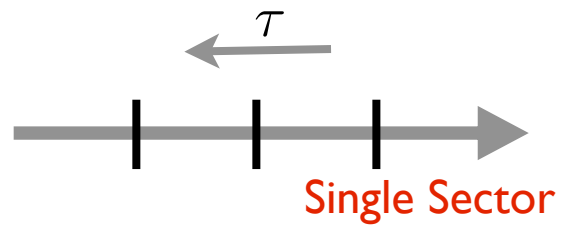
$L_{FI} \sim 10^6 \text{ meters}$ X decays could be seen in detectors.



Sector Equilibration

Connector operator couples the sectors so strongly that they come into thermal equilibrium.

$$\xi = T'/T \approx 1$$

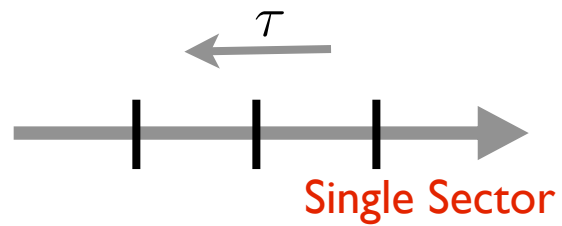


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What is the minimum possible lifetime that corresponds to equilibration?



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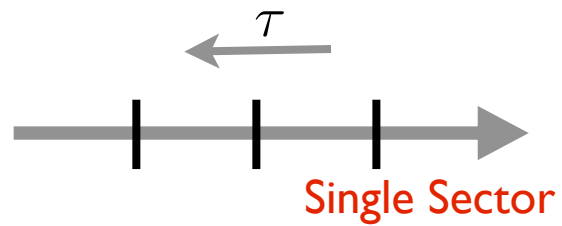
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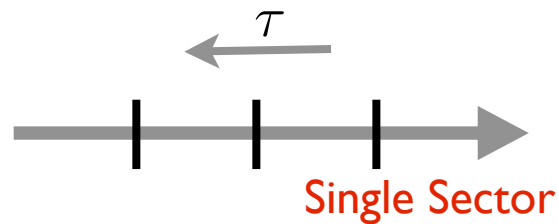
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From the change in hidden sector energy density due to FI:

$$Y'_{FI}(T) \propto \Gamma t \propto \frac{\Gamma M_{Pl}}{T^2} \quad \Rightarrow \quad \begin{cases} \xi_{IR}^4(T) = A \frac{M_{Pl} \Gamma}{T^2} & (T > m) \\ \xi_{IR}(T) \simeq \xi_{IR}(m) & (T < m). \end{cases} \quad \text{Since FI is exponentially switched off}$$



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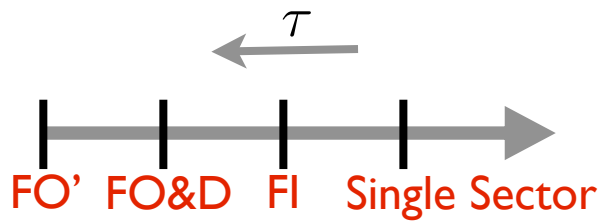
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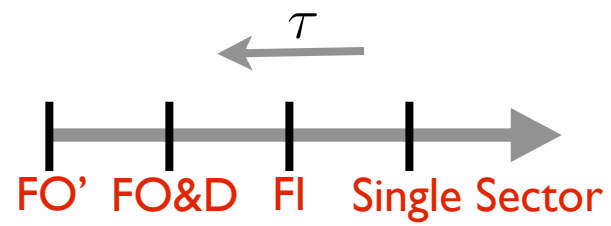
Freeze-In decays are strong enough to equilibrate the two sectors if:

$$\xi_{IR}(T \simeq m) = 1$$

$$\Rightarrow \tau_{\min} \simeq 10^{-13} \text{ s} \left(\frac{100 \text{ GeV}}{m} \right)^2 \left(\frac{100}{g'_*(T \simeq m)/g_X} \right)$$



Complete?

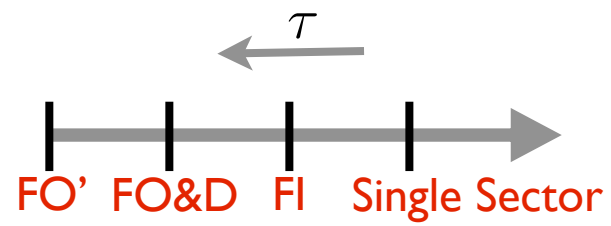


Complete?

Could there be other effects due to the presence of multiple source terms in the Boltzmann equations?

$$x \frac{d}{dx} Y' \simeq -\frac{Y'^2}{Y'_{\text{crit}}} + \frac{\Gamma Y}{H}$$

$$Y'_{\text{crit}} \equiv \frac{H}{\langle \sigma v \rangle' s}$$

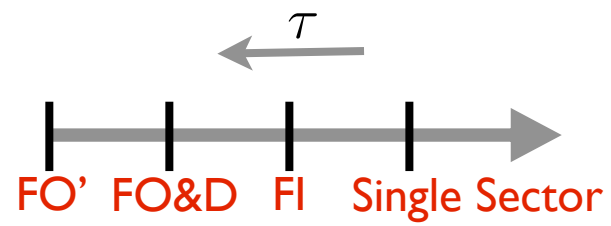


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X' source term
driving FI or FO&D



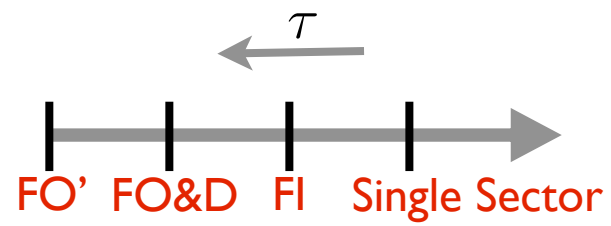
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\nearrow X' annihilations \nwarrow X' source term driving FI or FO&D

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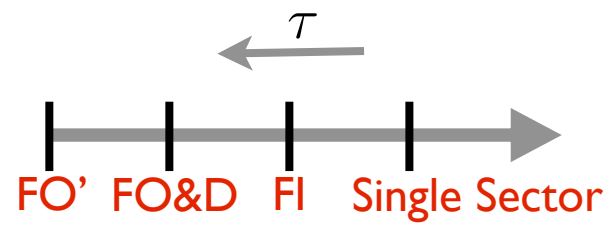
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X' annihilations

Ignored in FI and FO&D analysis

X' source term
driving FI or FO&D



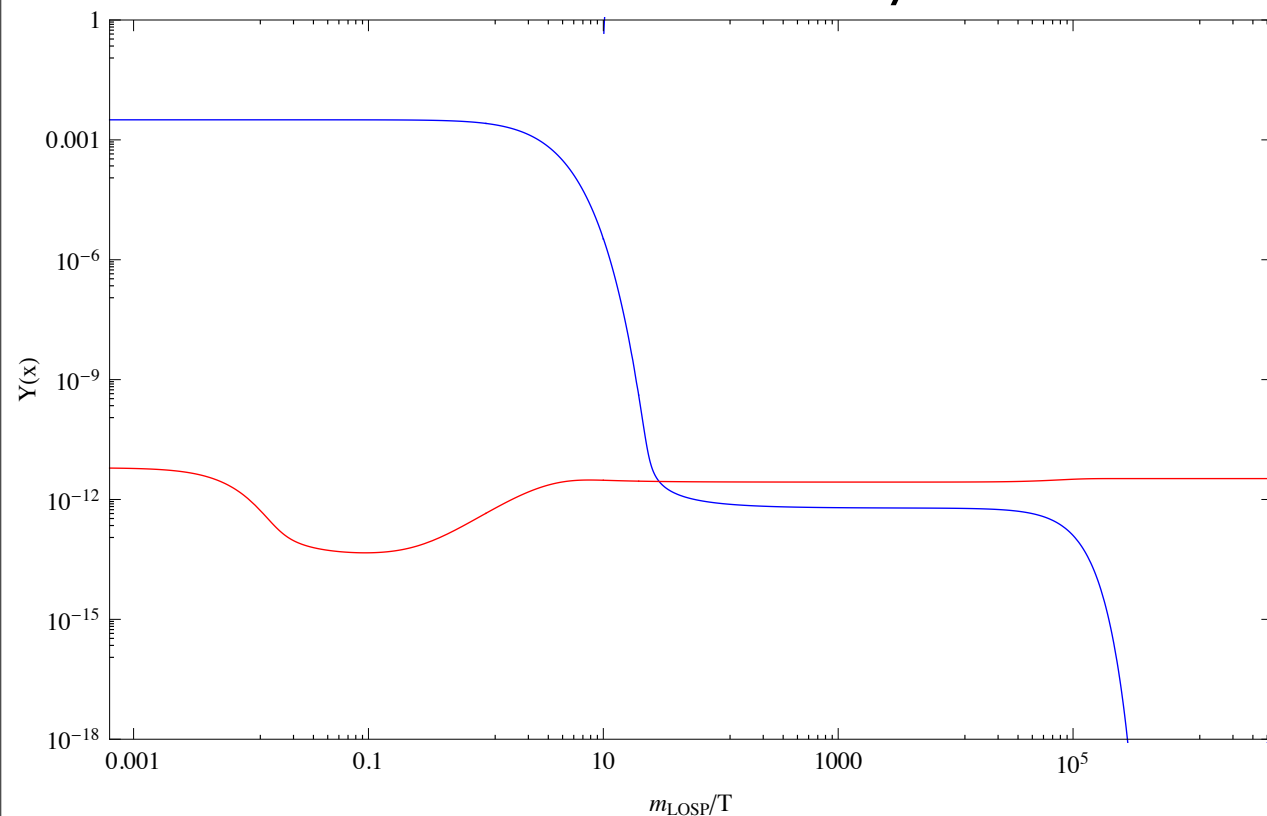
Complete?

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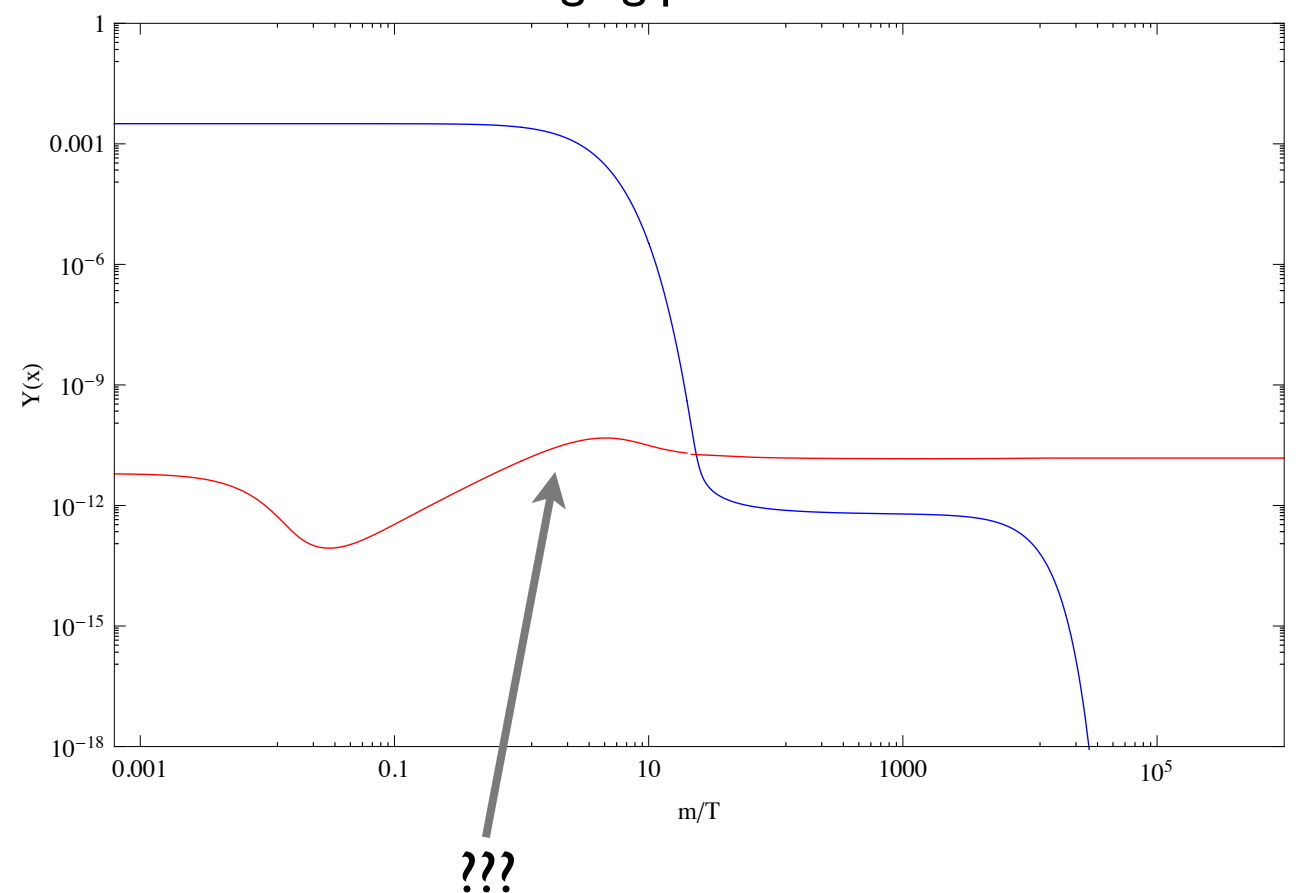
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Ignored in FI and FO&D analysis
X' source term
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Final abundance dominated by Freeze-In



Changing parameters...



Re-Annihilations

$$x \frac{d}{dx} Y' \simeq -\frac{Y'^2}{Y'_{\text{crit}}} + \frac{\Gamma Y}{H}$$

Multiple source terms can result in a modification of the FI and FO&D abundance

Recall X' is in thermal equilibrium as long as $Y' > \frac{H}{s\langle\sigma v\rangle'} = Y'_{\text{crit}}$

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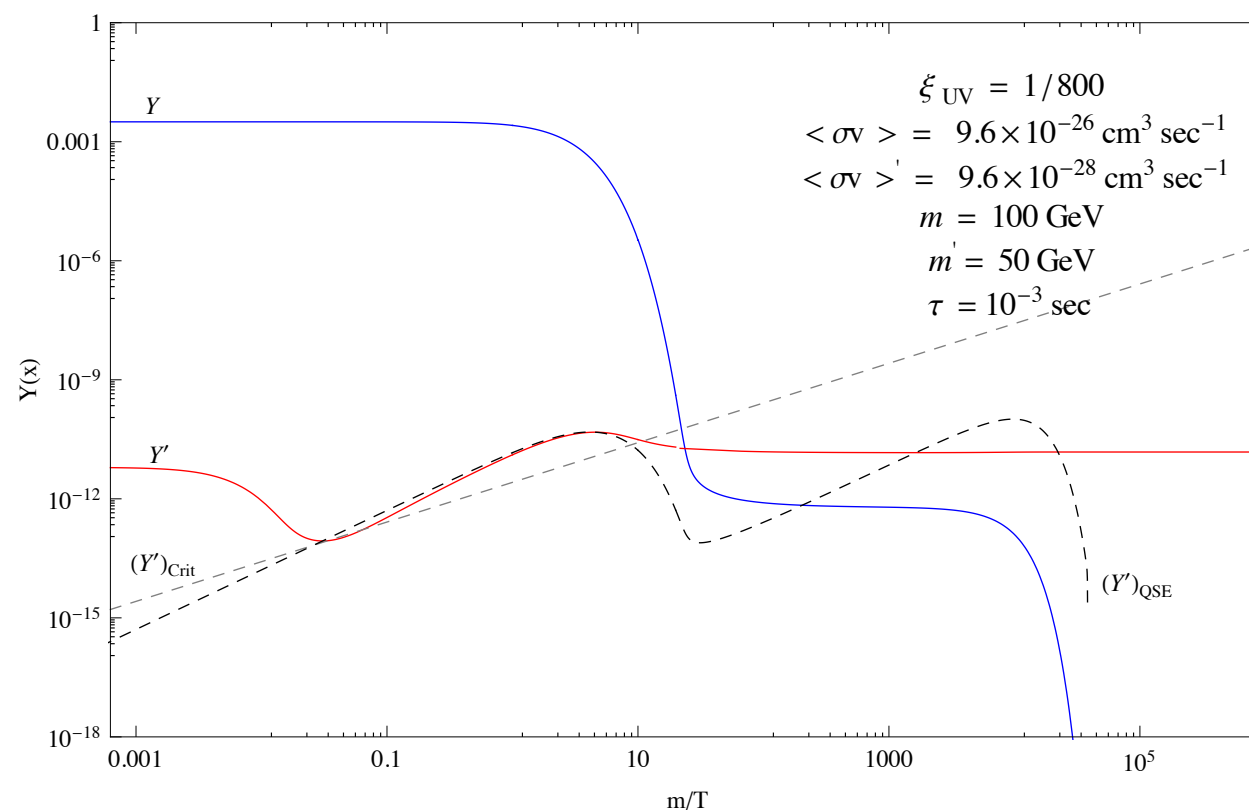
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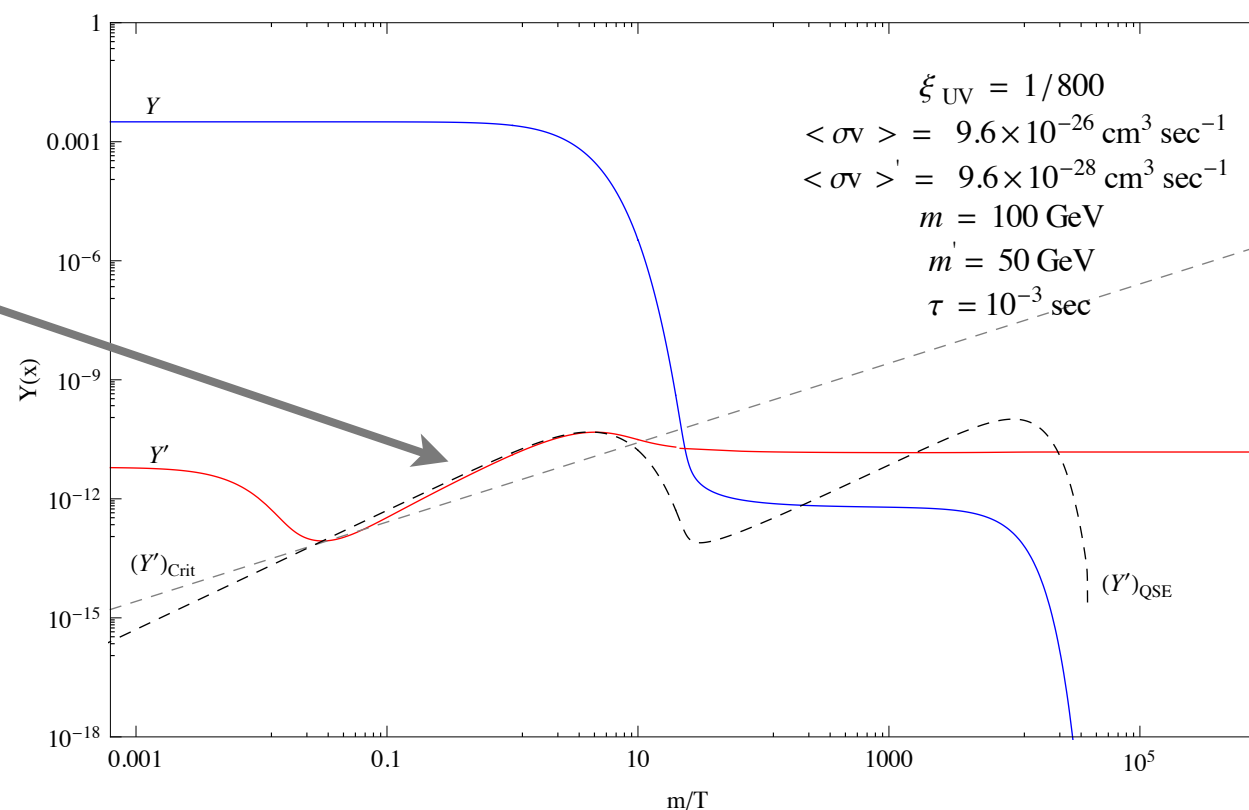
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QSE will be maintained as long as $Y'_{\text{QSE}} > Y'_{\text{crit}}$



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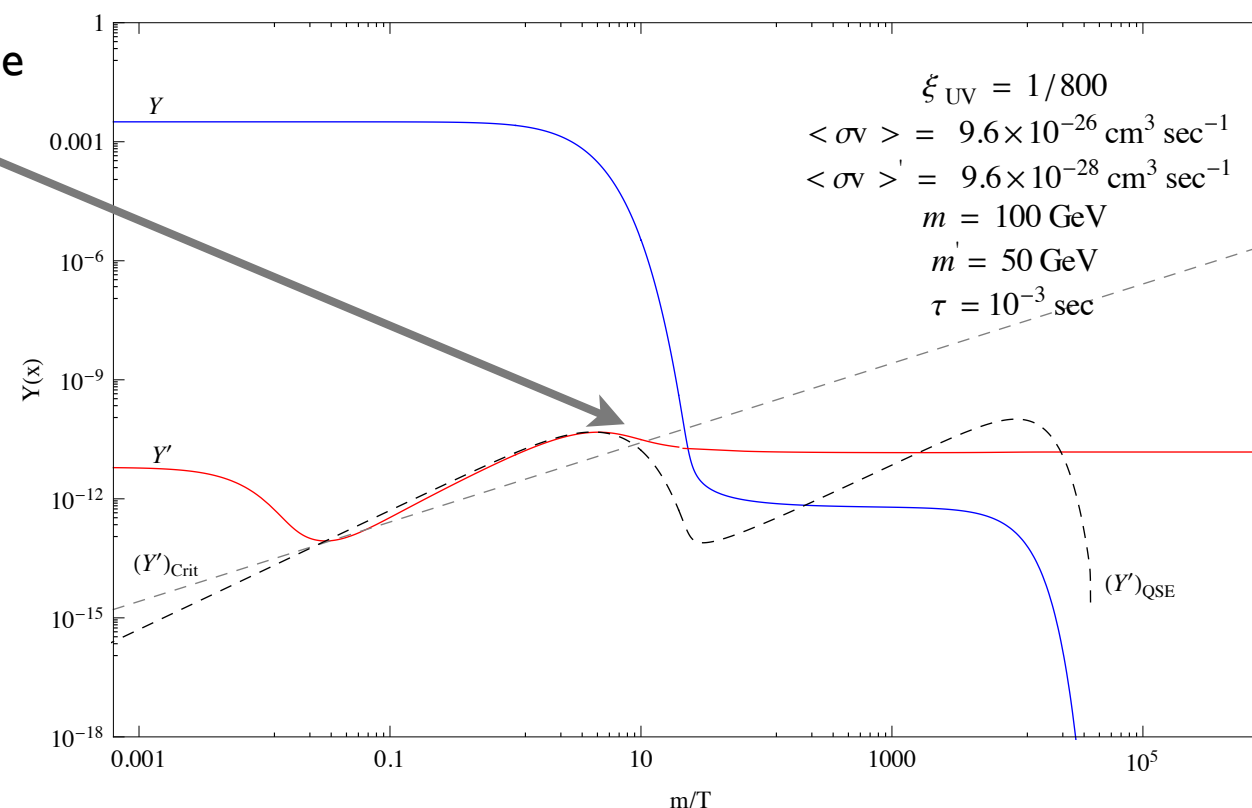
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Ends when Y' falls below the critical yield at T_r

$$Y'_{\text{QSE}}(T_r) = Y'_{\text{crit}}(T_r)$$



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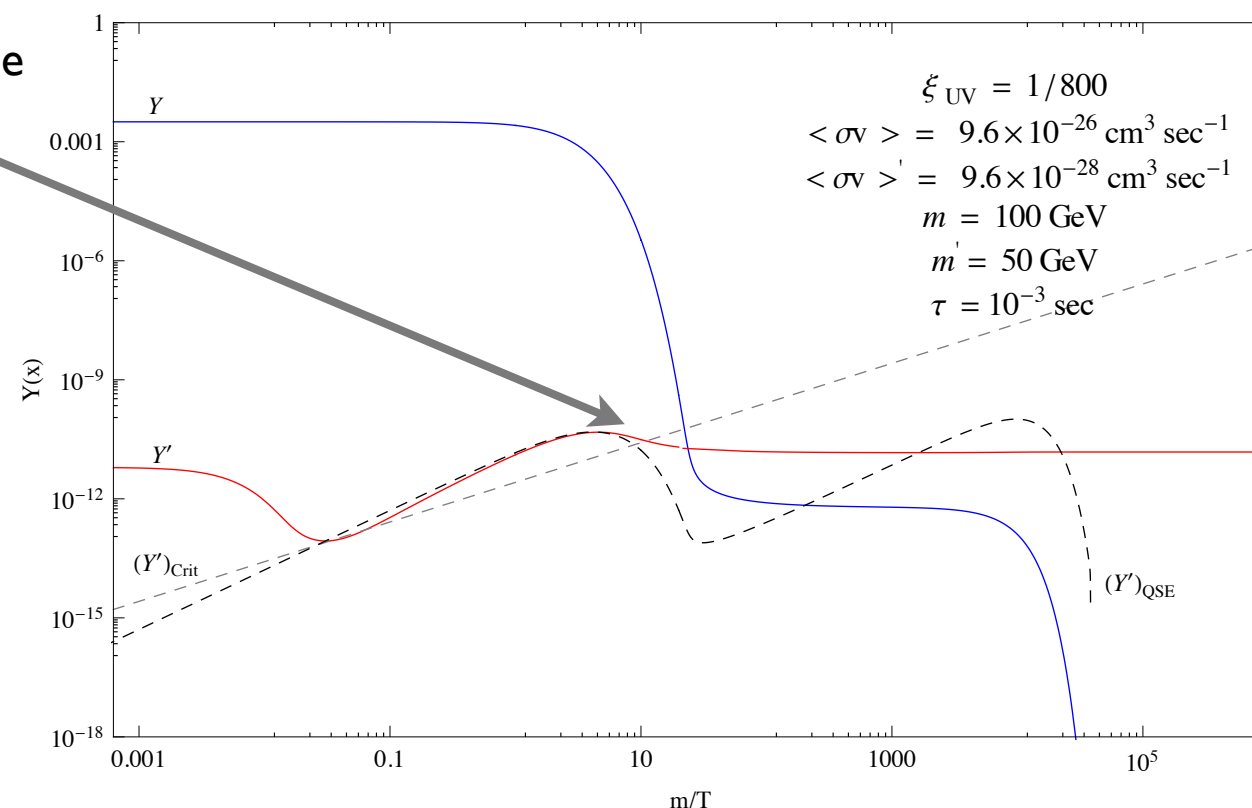
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Resulting in a modified (smaller) FI yield which we call FI_r

$$Y'_{FI_r} = Y'_{\text{crit}}(T_{FI_r})$$

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Of course these *Re-Annihilations* will start at a lower abundance (a second FO')

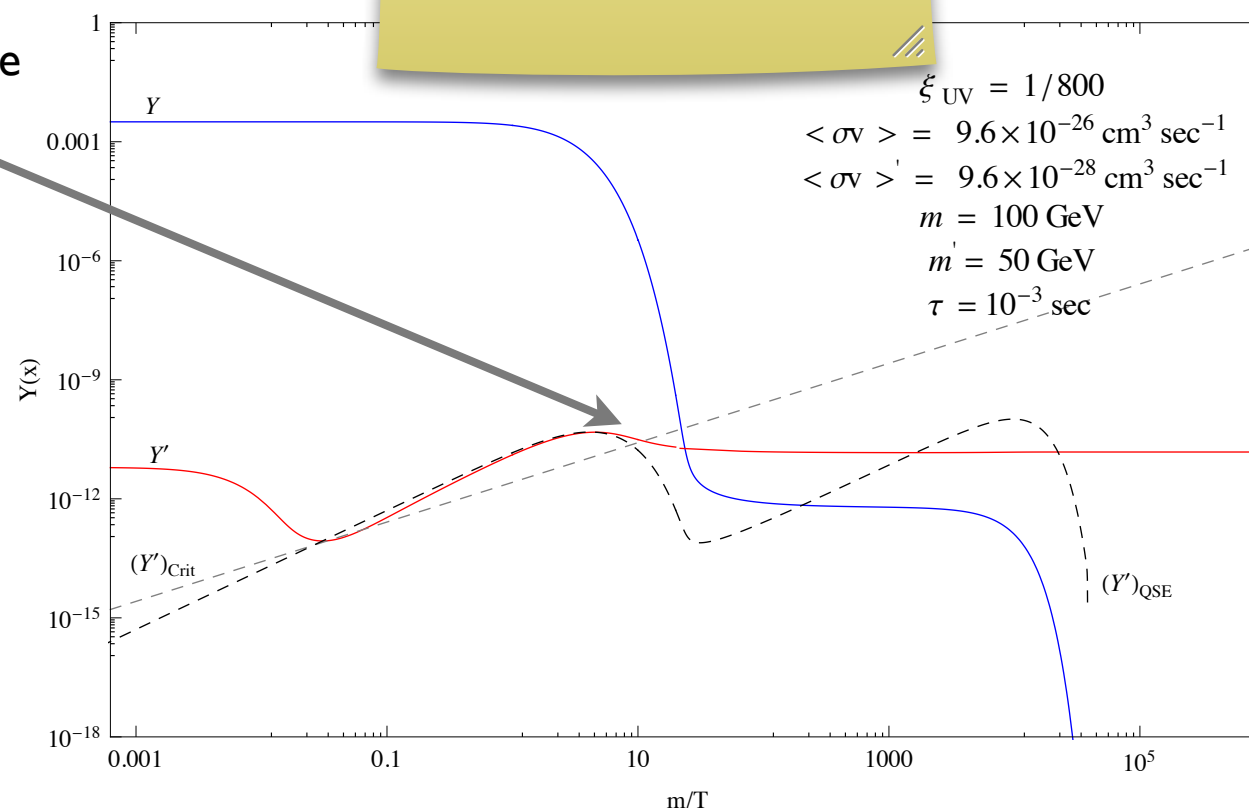
We call this competing behavior between decays and annihilations *Quasi-Static Equilibrium (QSE)*

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$$Y'_{\text{QSE}} = \frac{\Gamma Y}{H} Y'_{\text{crit}} = \frac{\Gamma Y}{\langle\sigma v\rangle' s}$$

Ends when Y' falls below the critical yield at T_r

$$Y'_{\text{QSE}}(T_r) = Y'_{\text{crit}}(T_r)$$



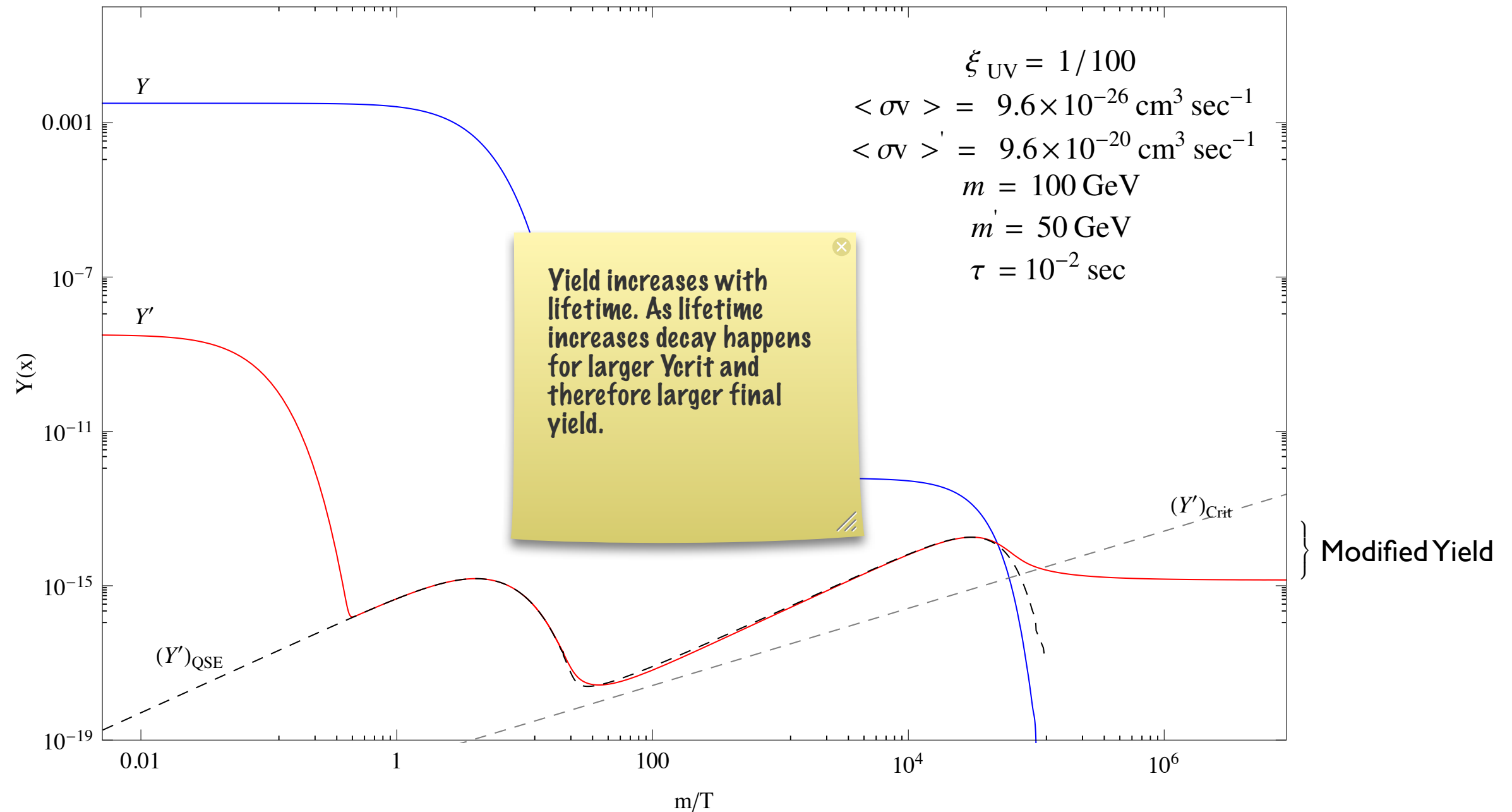
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$$Y'_{FI_r} = Y'_{\text{crit}}(T_{FI_r})$$

$$Y'_{FI_r} = C_{FO} \frac{1}{M_{Pl} \langle\sigma v\rangle'} \frac{1}{T_{FI_r}} \propto \frac{1}{m \langle\sigma v\rangle'}$$

Not Reconstructable

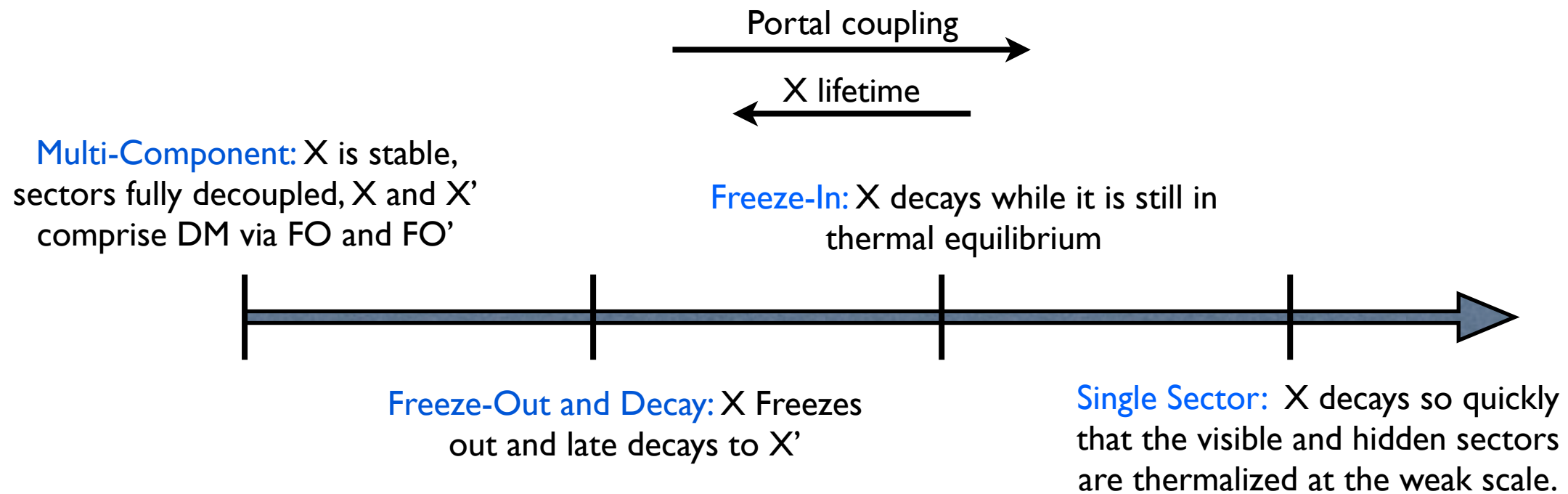
Freeze-Out and Decay with Re-Annihilation (FO&Dr)



$$Y'_{\text{FO\&Dr}} = Y'_{\text{crit}}(T_{\text{FO\&Dr}}) \quad \longrightarrow \quad Y'_{\text{FO\&Dr}} = C_{\text{FO}} \frac{1}{M_{\text{Pl}} \langle \sigma v \rangle'} \frac{1}{T_{\text{FO\&Dr}}} \propto \frac{\sqrt{\tau}}{\langle \sigma v \rangle'}$$

Not Reconstructable

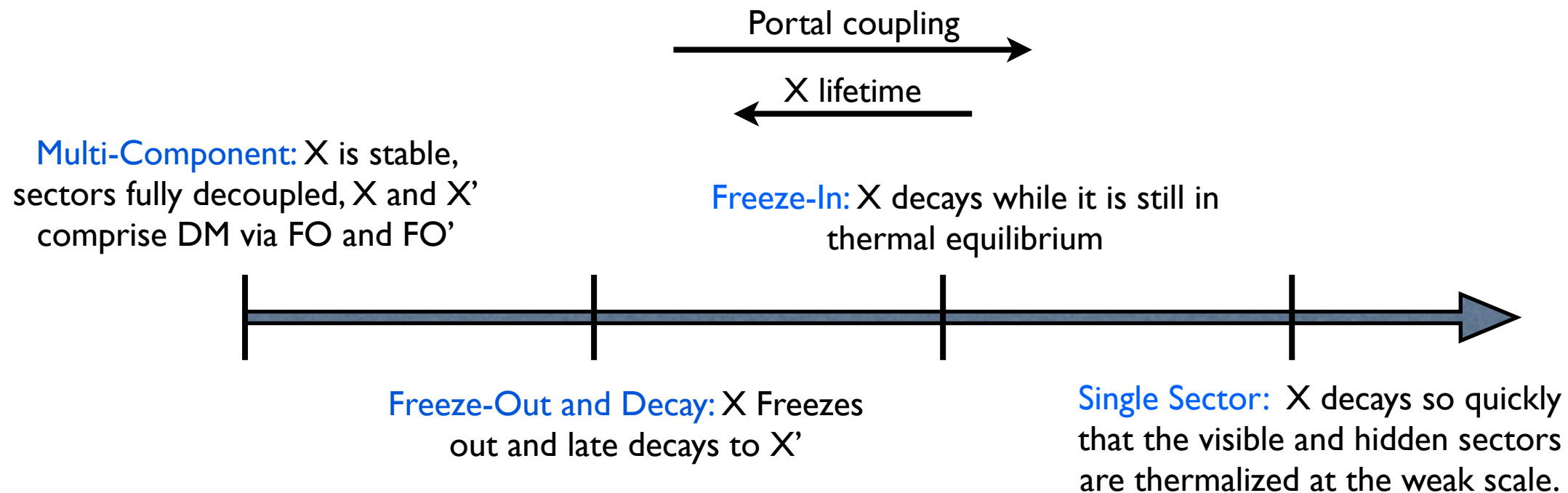
Summary



FO&D and FI are in principle reconstructable as long as yield is not modified by re-annihilations.

$$\left\{ \begin{array}{l} Y'_{\text{FO\&D}} \propto \frac{1}{m \langle \sigma v \rangle} \\ Y'_{\text{FI}} \propto \frac{1}{\tau m^2} \\ Y'_{\text{FO}'} \propto \frac{\xi_{\text{FO}'}}{m' \langle \sigma v \rangle'} \\ Y'_{\text{FI}_r} \propto \frac{1}{m \langle \sigma v \rangle'} \\ Y'_{\text{FO\&D}_r} \propto \frac{\sqrt{\tau}}{\langle \sigma v \rangle'} \end{array} \right.$$

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Next: what does parameter space look like?

$$\{m, m', \langle \sigma v \rangle, \langle \sigma v \rangle', \xi, \tau, \epsilon\}$$

Cosmological Phase Diagrams

$$\langle\sigma v\rangle = \langle\sigma v\rangle_0 = 3 \times 10^{-26} \text{ cm}^3/\text{s}$$

$$m = 100 \text{ GeV}, m' = 50 \text{ GeV}$$

$$\xi_{UV} = 0.01$$

$$Y'_{\text{FO\&D}} \propto \frac{1}{m\langle\sigma v\rangle}$$

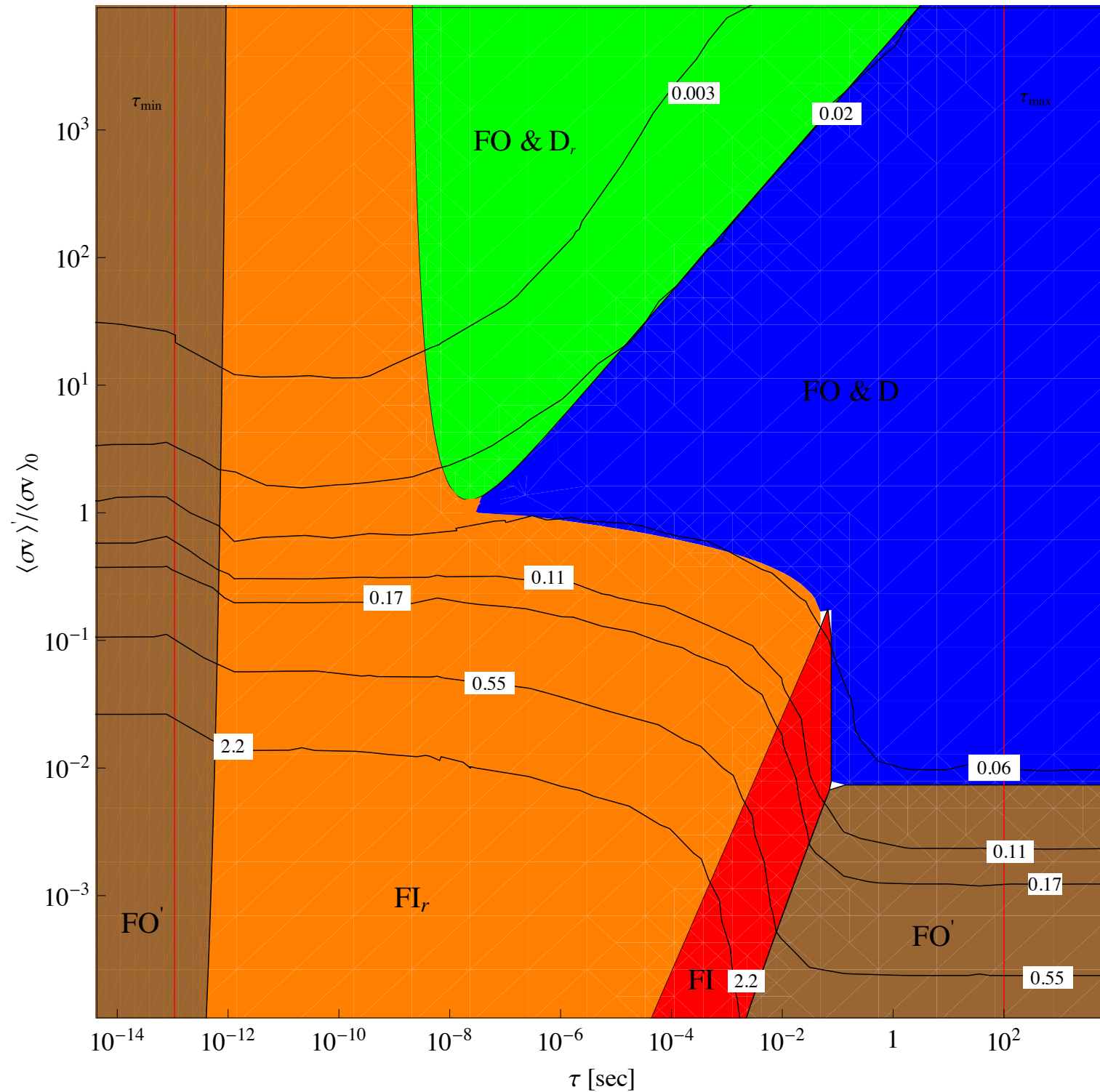
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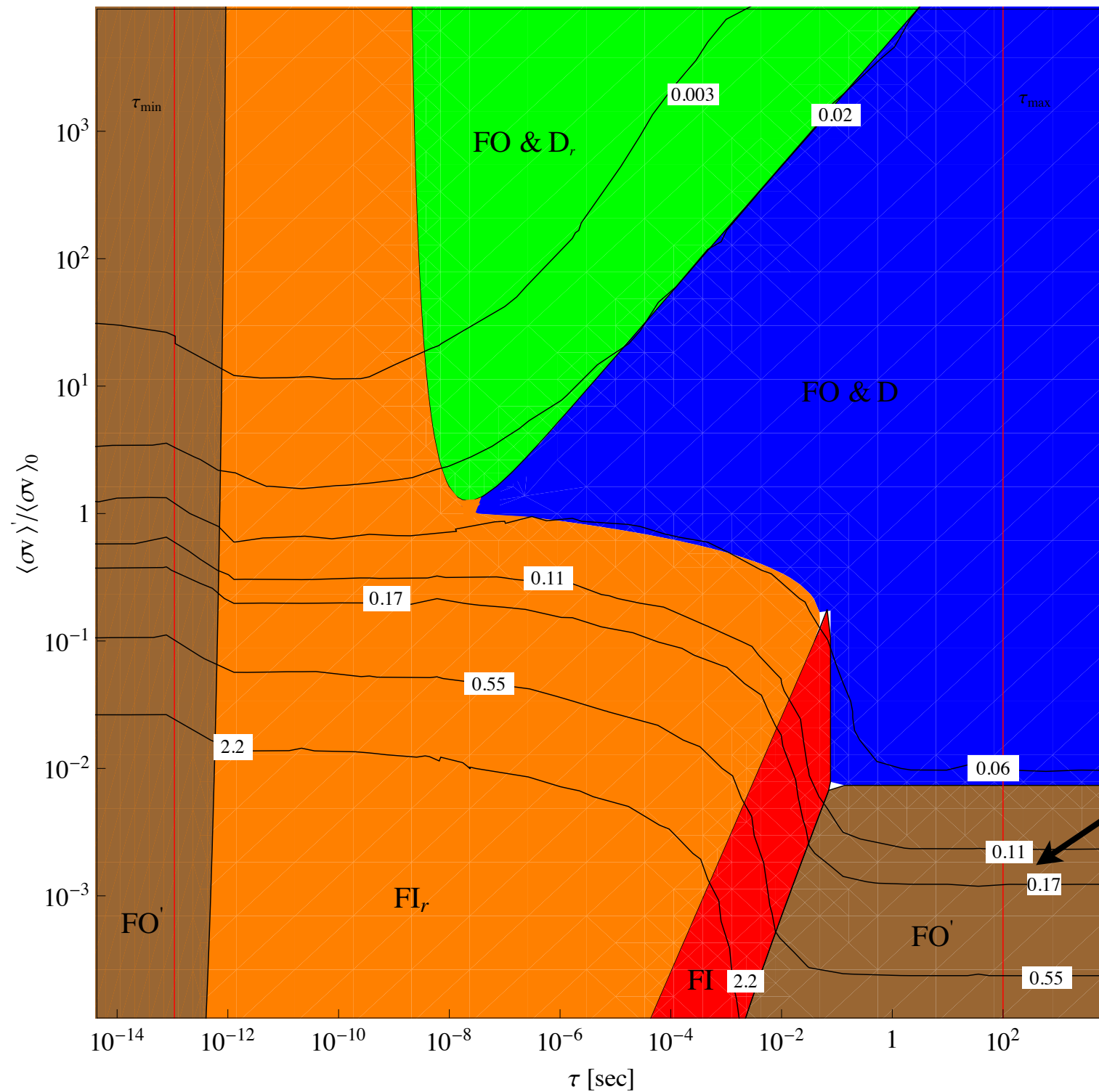
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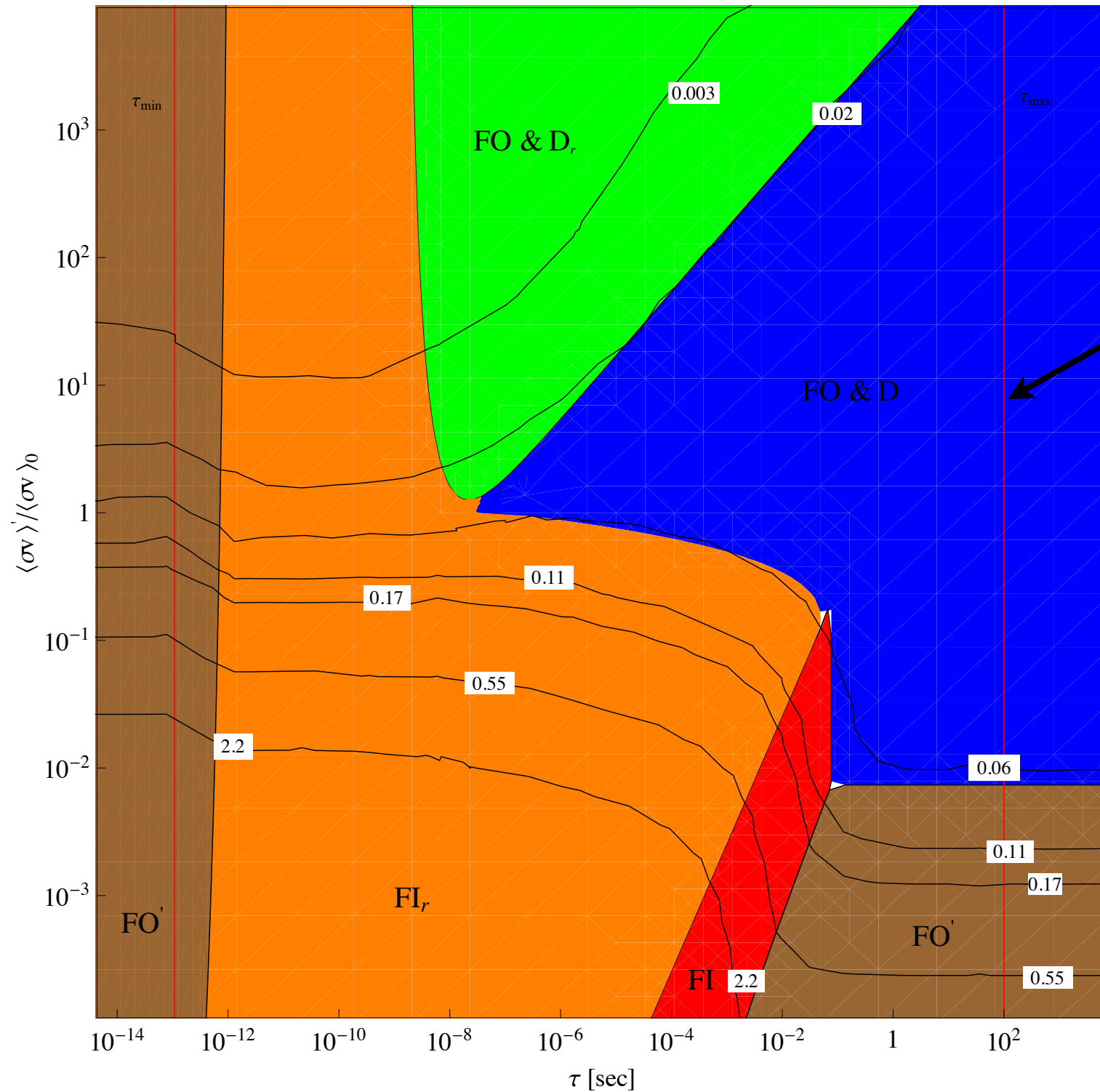
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BBN bound

[M. Kawasaki, K. Kohri,
T. Moroi, A. Yotsuyanagi
arXiv:0804.3745]

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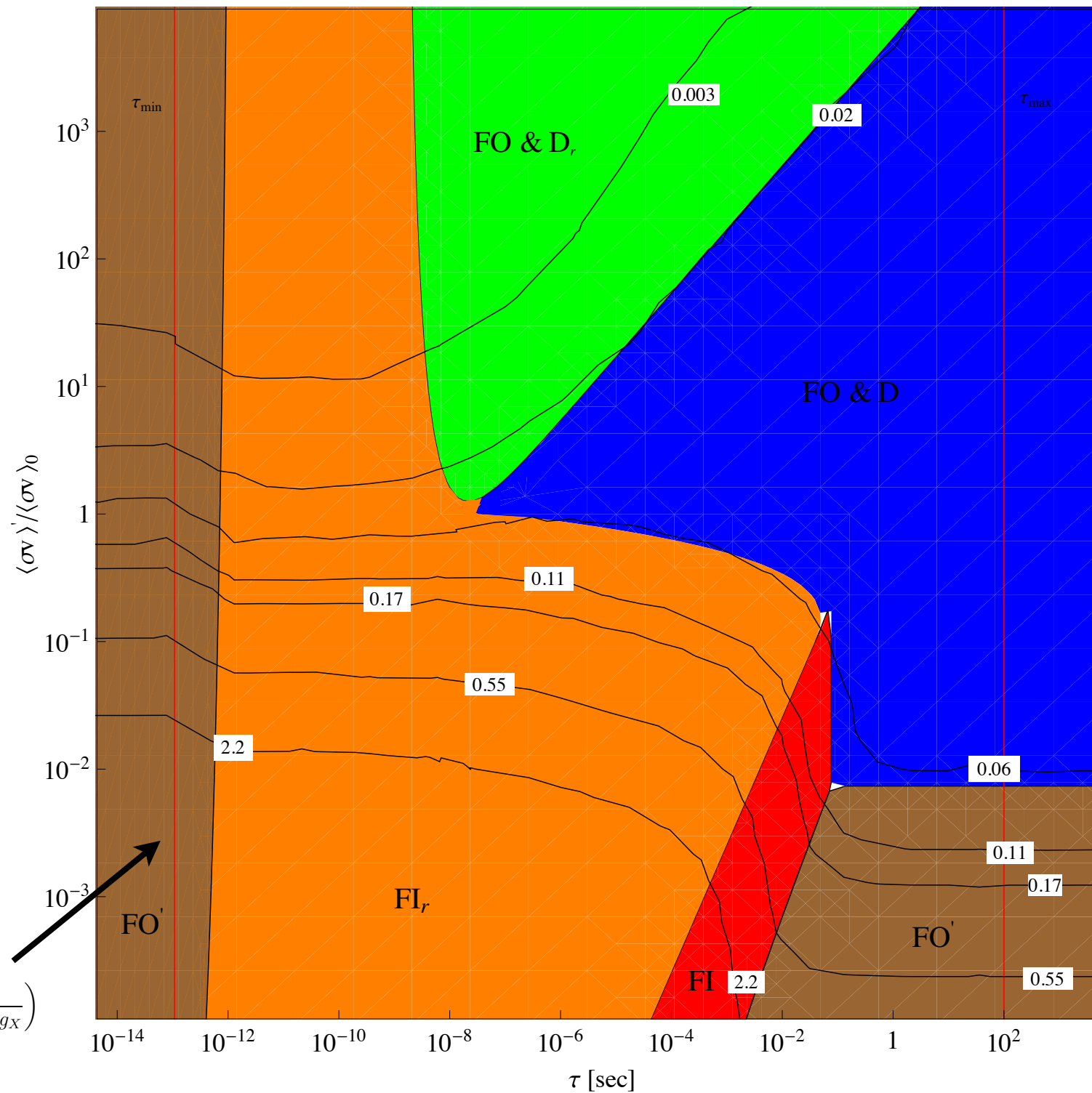
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$$\xi_{\text{FO}'}^4(\tau) \sim \xi_{UV}^4 + \frac{\#}{\tau^2}$$

Thermalization bound

$$\tau_{\min} \simeq 10^{-13} \text{ s} \left(\frac{100 \text{ GeV}}{m} \right)^2 \left(\frac{100}{g'_*(T \simeq m)/g_X} \right)$$



Cosmological Phase Diagram

Talk about contours and regions.

$$Y'_{\text{FO\&D}} \propto \frac{1}{m \langle \sigma v \rangle}$$

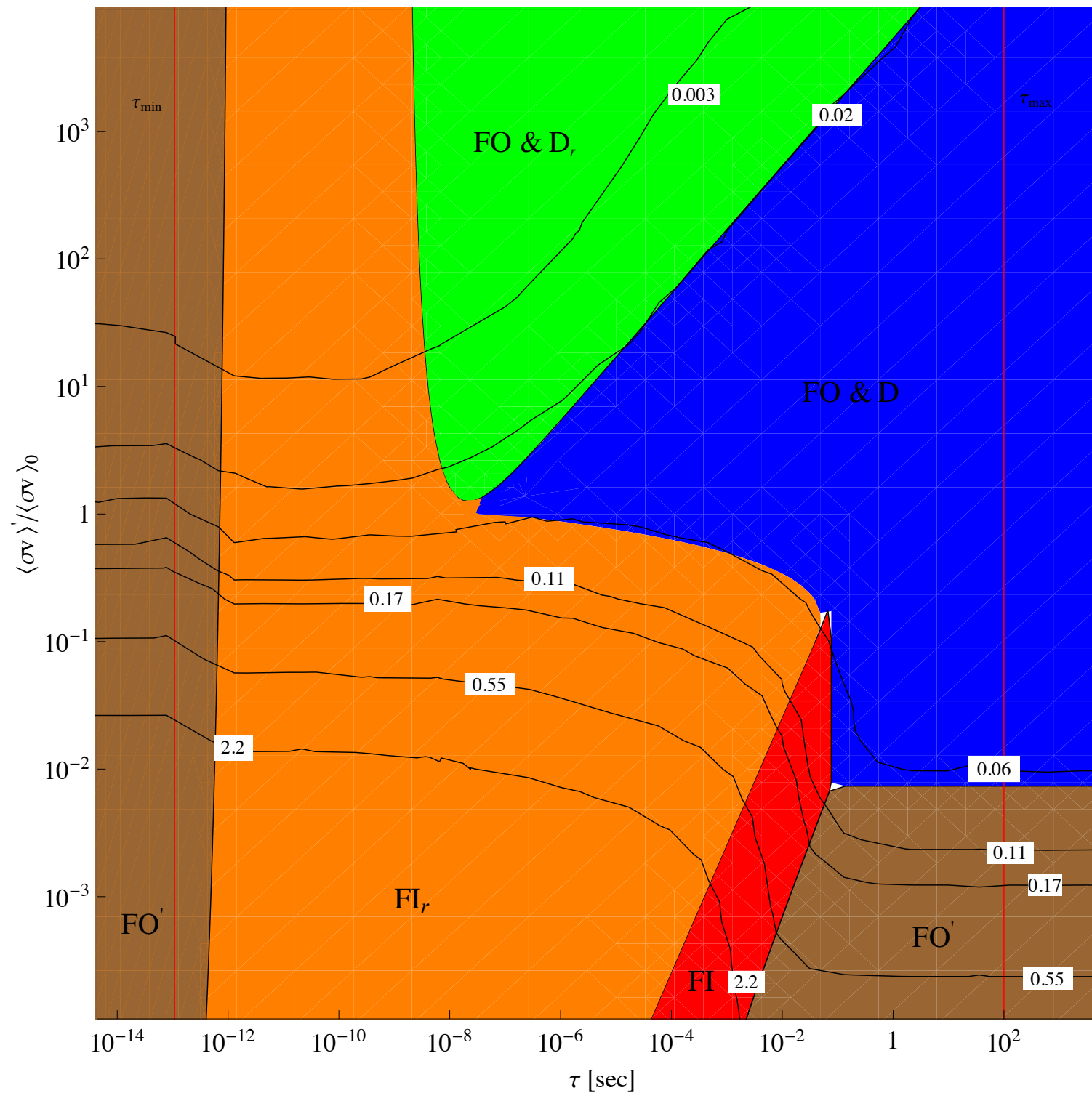
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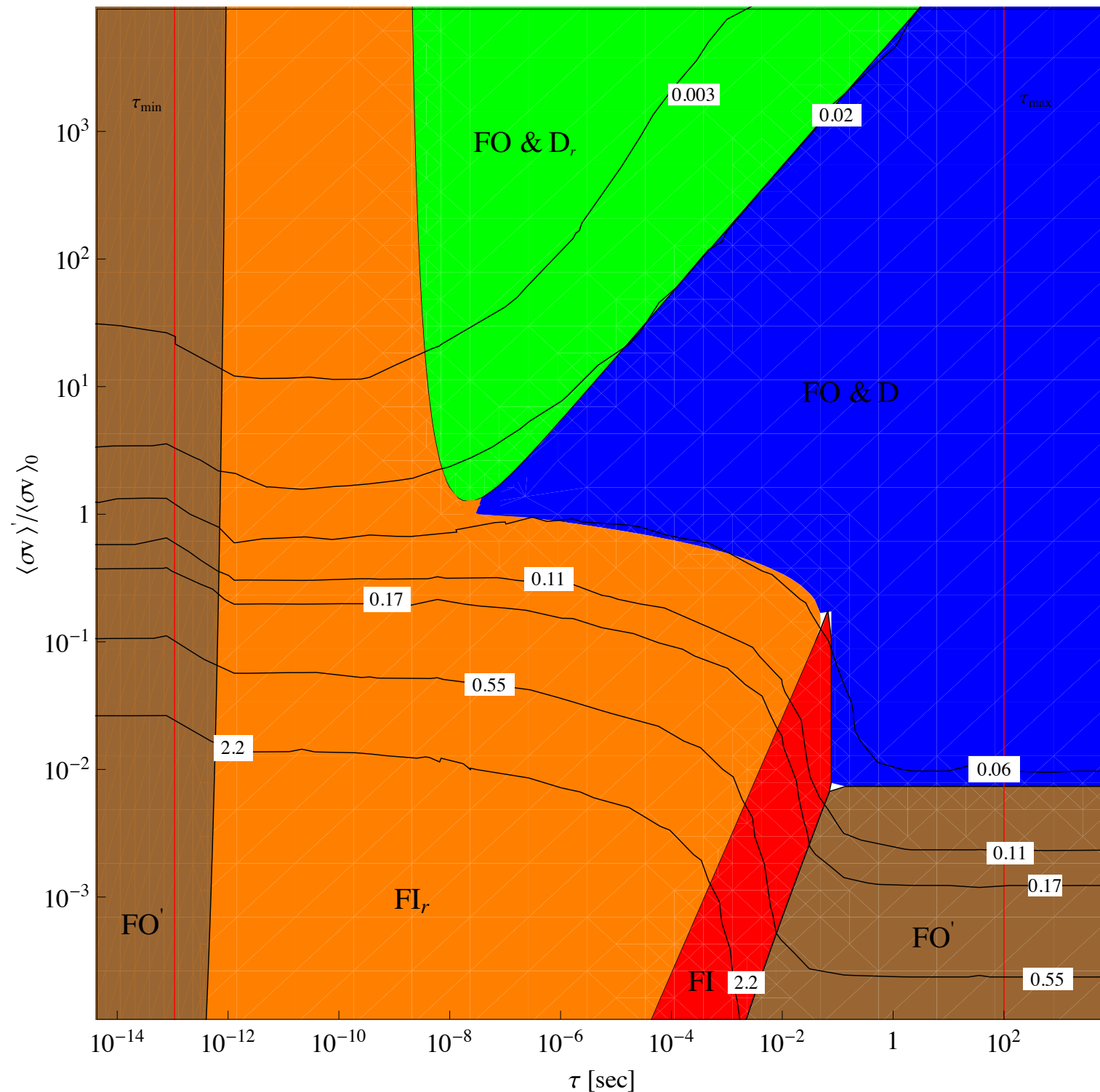
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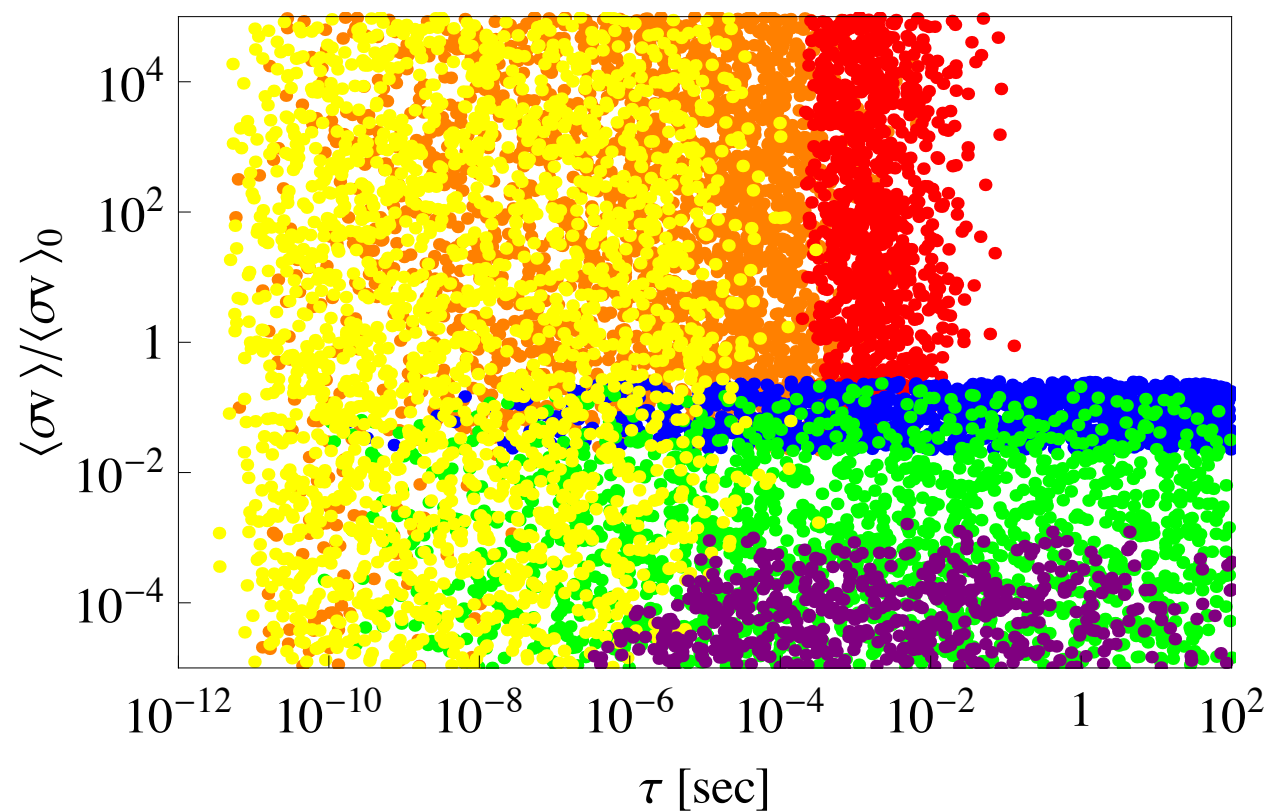


Still need to enforce Dark Matter constraint...

Getting the Right Relic Abundance

$$\Omega_{DM} h^2 \sim 0.11$$

Production mechanisms map to distinct window in parameter space:



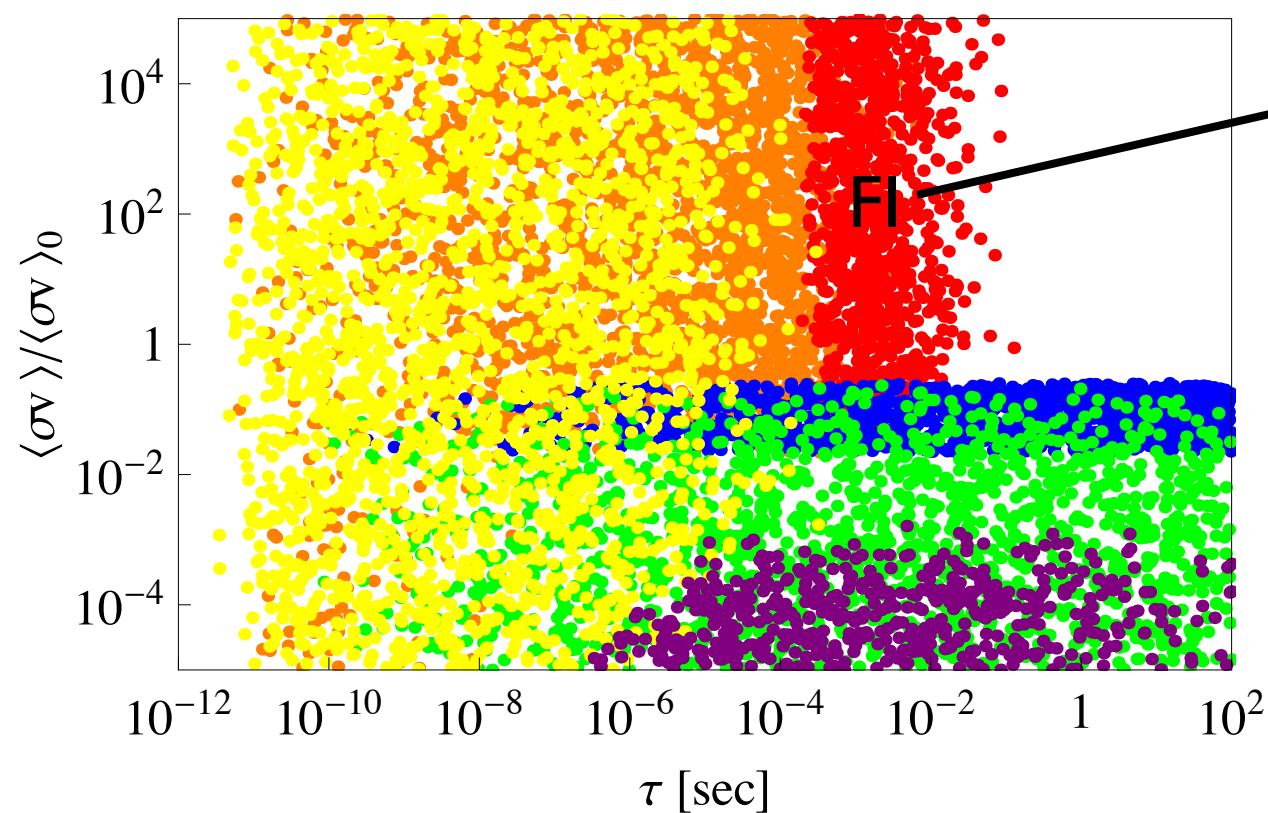
$$10 \text{ GeV} < m < 1 \text{ TeV}$$

$$1/20 < m'/m < 1/2$$

Getting the Right Relic Abundance

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Production mechanisms map to distinct window in parameter space:



$$\tau \simeq (4 \times 10^{-2} \text{ s}) \left(\frac{m'}{m} \right) \left(\frac{100 \text{ GeV}}{m} \right) \left(\frac{228.5}{g_\star} \right)^{3/2}$$

$$L_{\text{FI}} \sim 10^6 \text{ meters} \times \gamma \left(\frac{m'/m}{0.25} \right) \left(\frac{300 \text{ GeV}}{m} \right)$$

Decays could be seen in detectors.

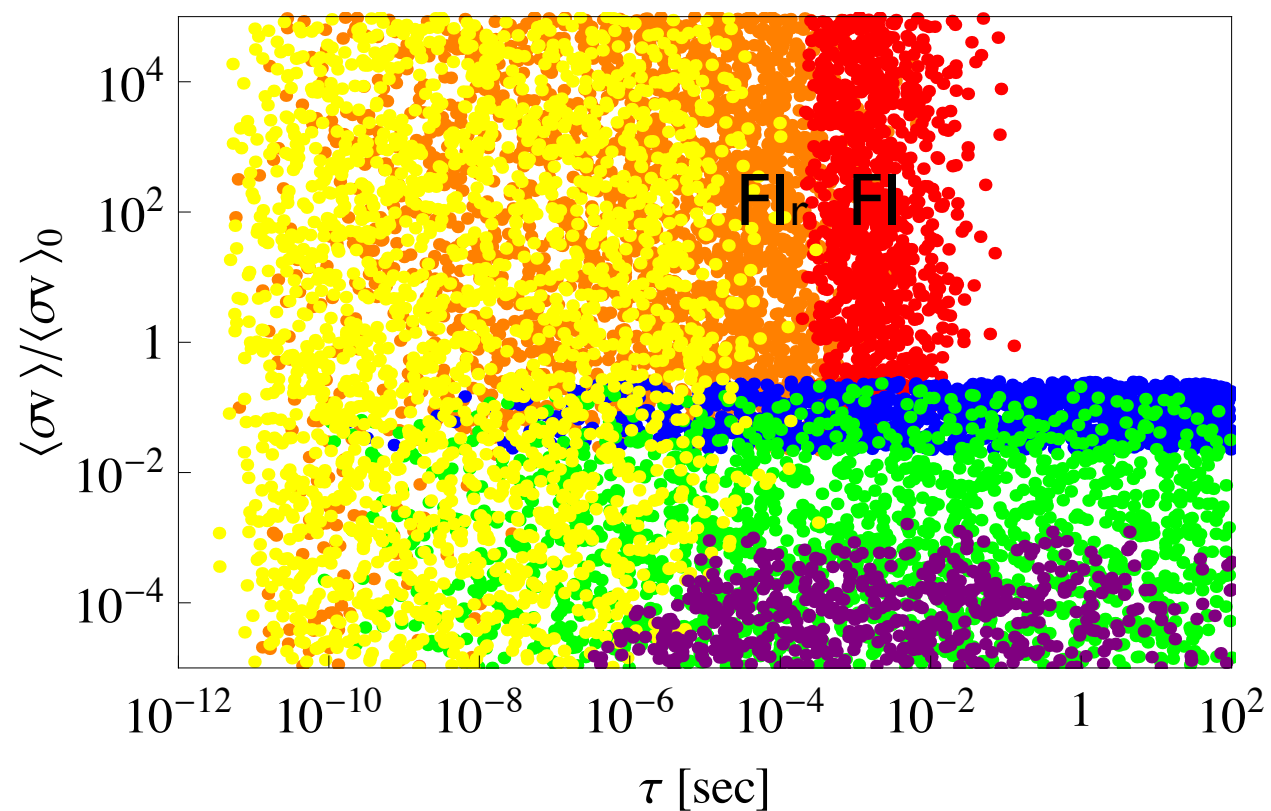
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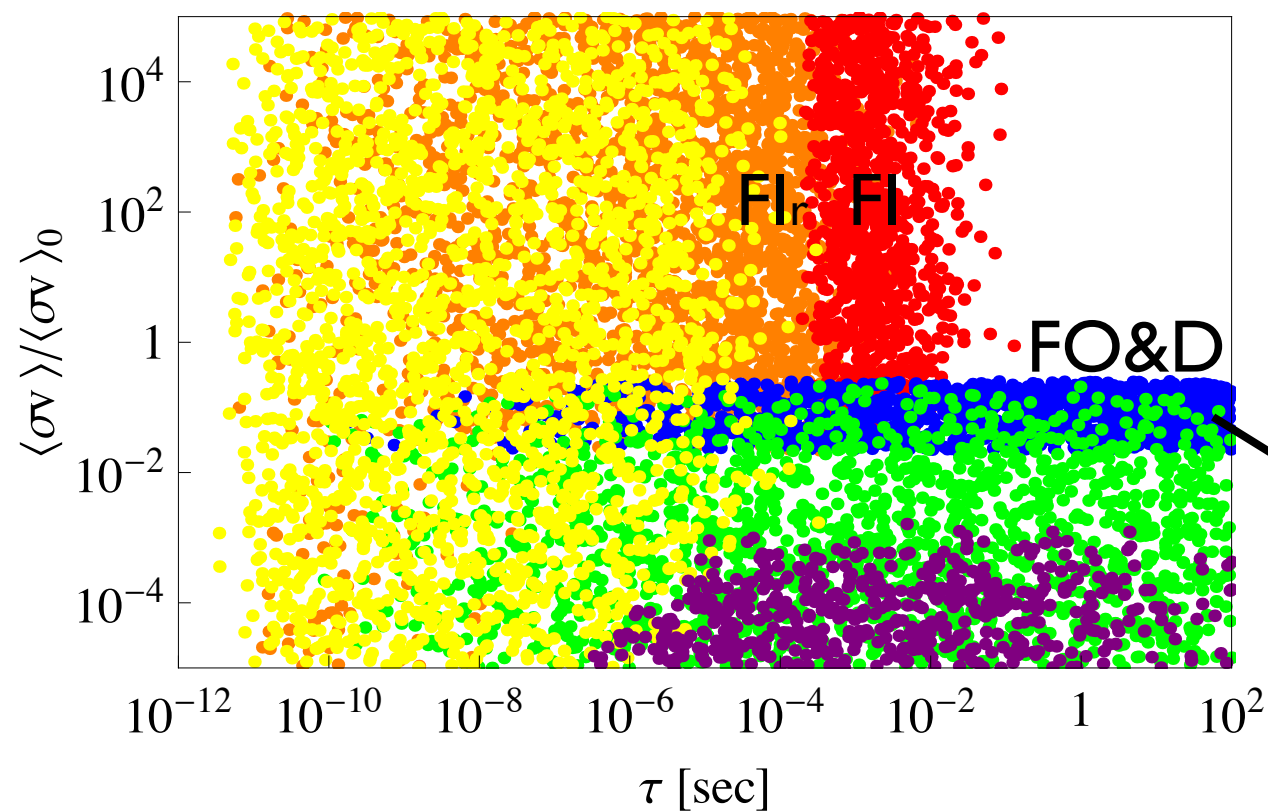
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$$\frac{\langle\sigma v\rangle m}{m'} \sim \frac{4 \times 10^{10}}{M_{\text{Pl}} \sqrt{g_\star}} \sim \frac{2 \times 10^{-25} \text{ cm}^3 \text{ sec}^{-1}}{\sqrt{g_\star}}$$

$$L_{\text{FO\&D}} \sim (10^{10} - 10^{-5} \text{ meters}) \gamma$$

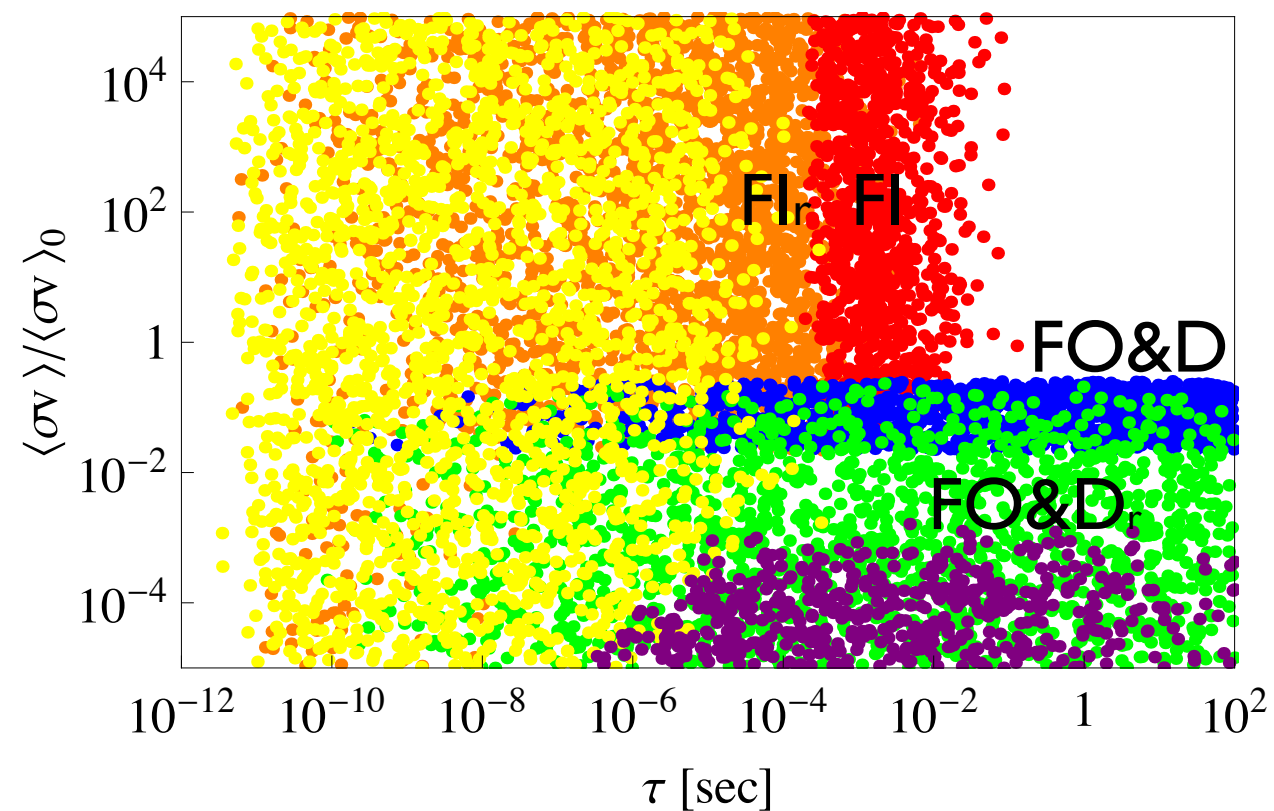
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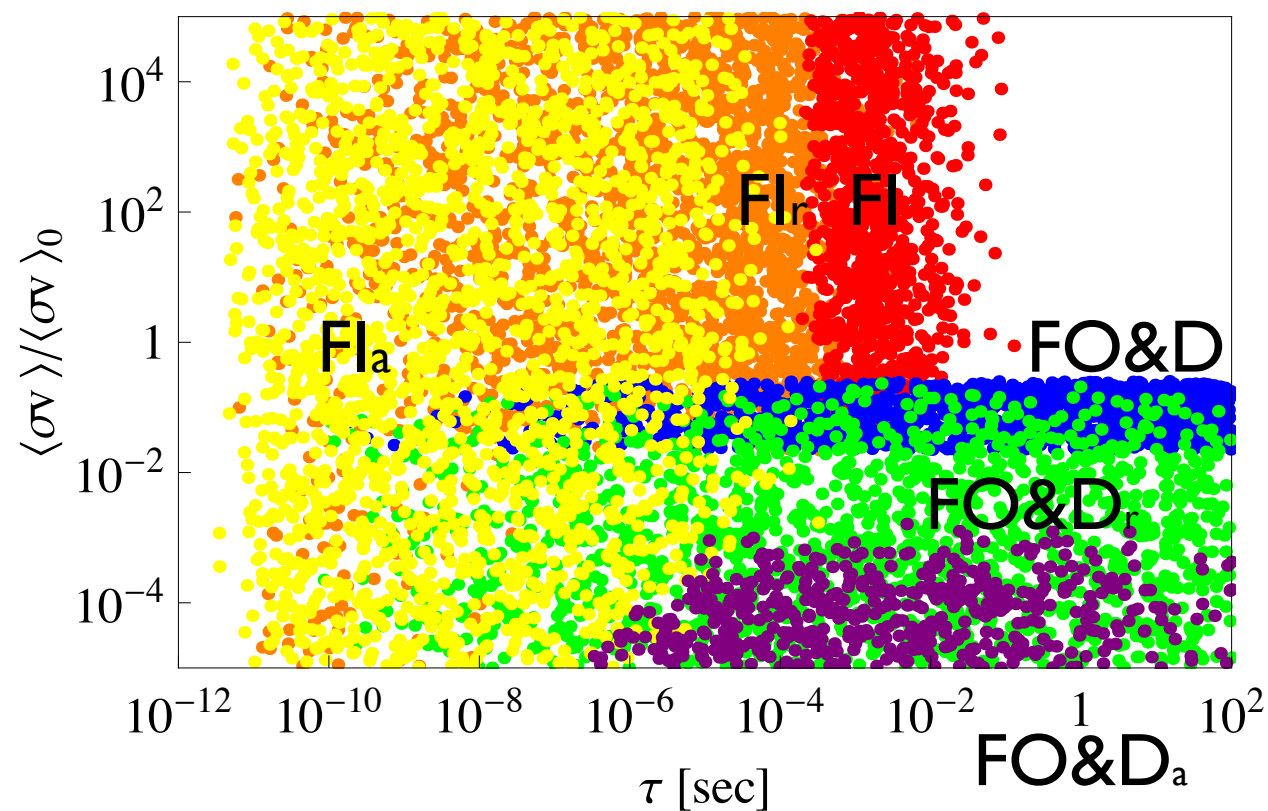
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Production mechanisms map to distinct window in parameter



$$10 \text{ GeV} < m < 1 \text{ TeV}$$

$$1/20 < m'/m < 1/2$$

Generating Dark Matter
particle asym

$$10^{-8} < \epsilon$$

Yellow and Purple coor to getting the right DM abundance via particle anti-particle asym, which unlike FO and FO' you can do with FI and FO&D since sectors are thermally decoupled and

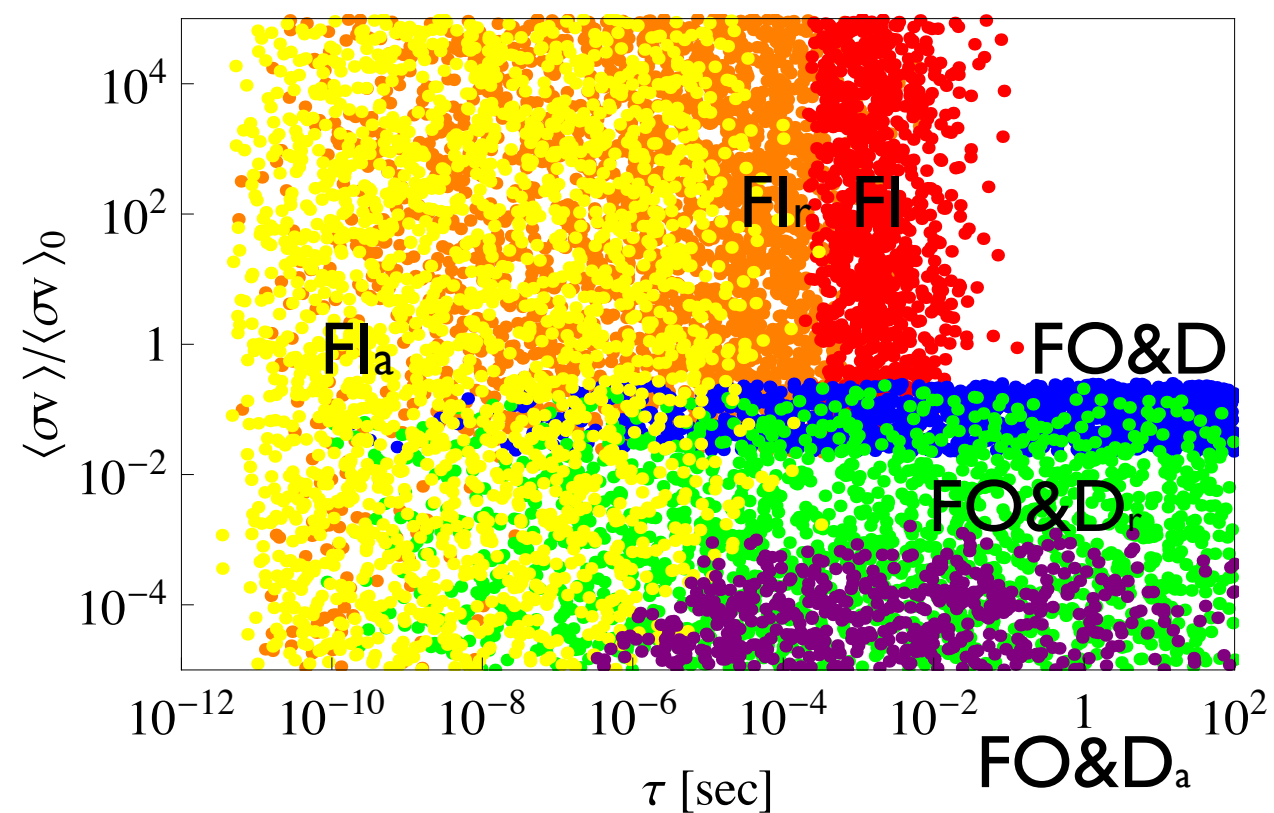
thus connector operators are not in TE. As usual we need to get rid of the symmetric part of the yield (since it is larger by a factor of $1/\epsilon$) which can happen if re-anhh are active to get rid

of symm component. Here we have scanned over epsilon the CP violation paramter.

Getting the Right Relic Abundance

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Production mechanisms map to distinct window in parameter space:



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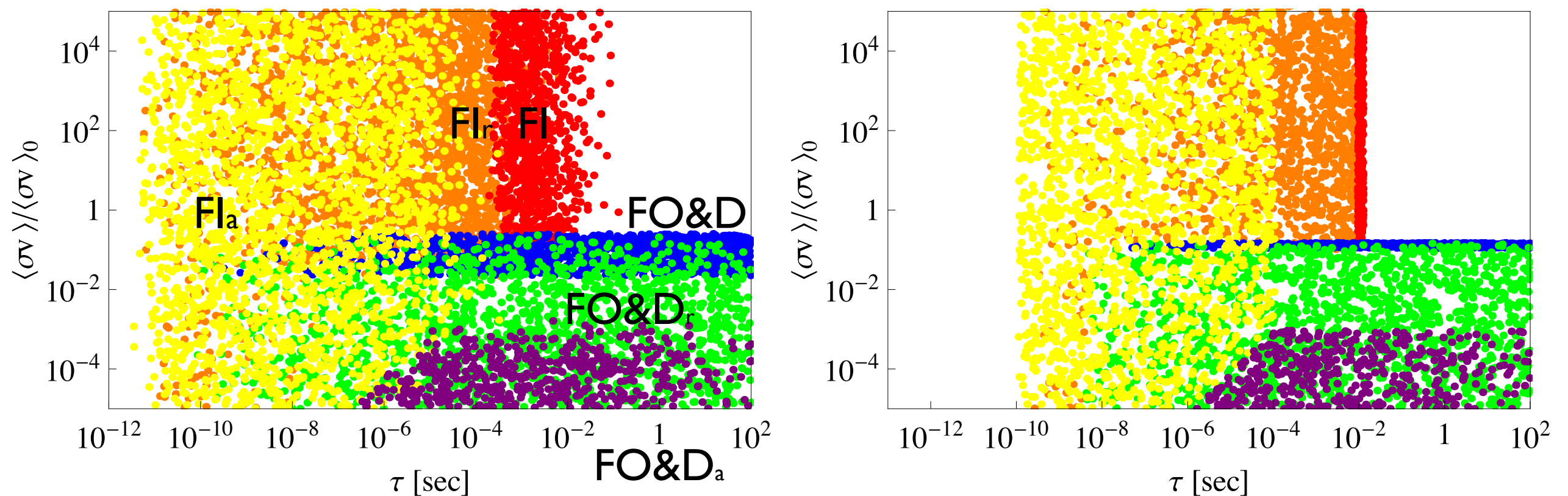
measure masses



Getting the Right Relic Abundance

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 $1/20 < m'/m < 1/2$

measure masses

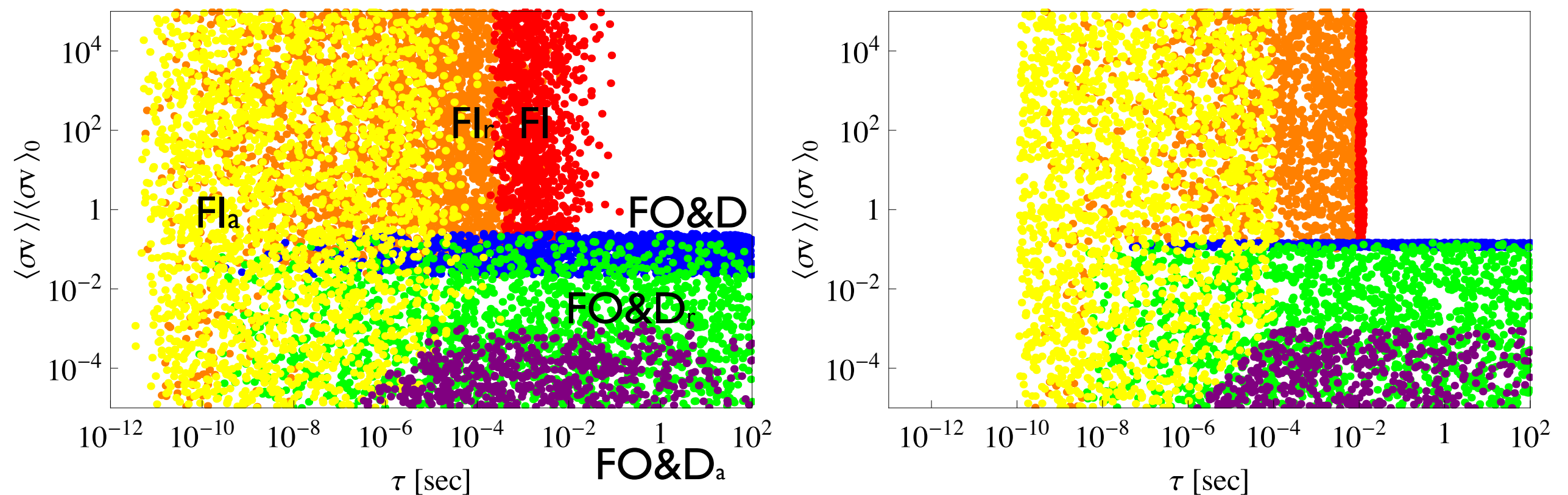


$m = 100 \text{ GeV}$
 $1/4 < m'/m < 1/3$

Getting the Right Relic Abundance

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$m = 100 \text{ GeV}$
 $1/4 < m'/m < 1/3$

Lifetime ranges are promising for seeing X decays within detectors.
 To address “reconstruction” we must choose a more specific model.

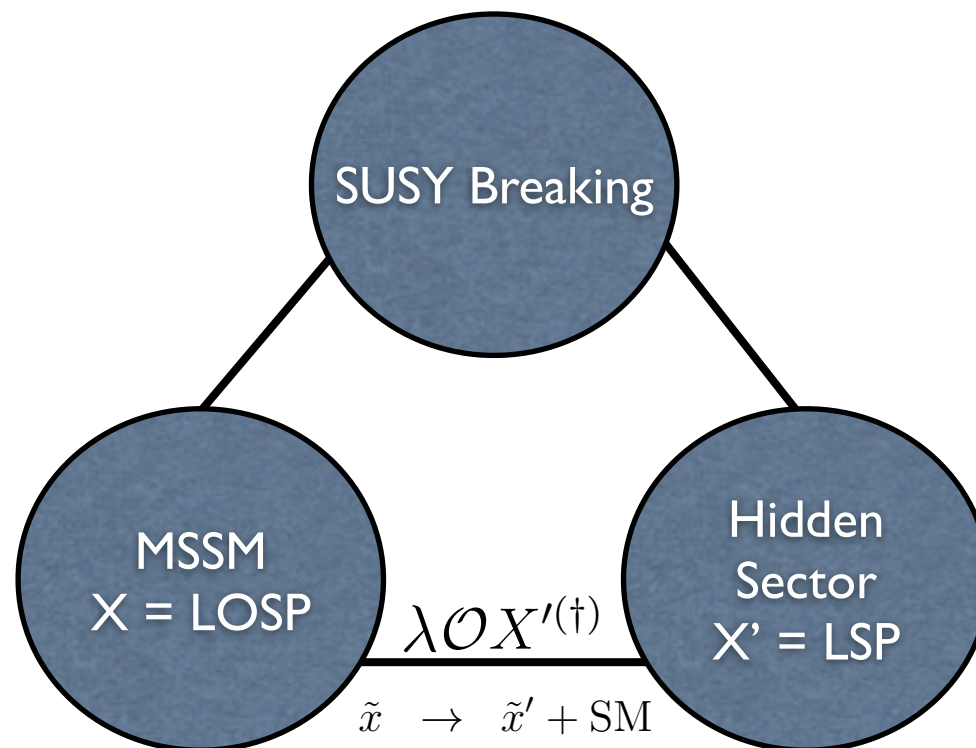
Collider Signals arXiv:1010.0024

II.Collider Physics

Supersymmetric Model

Assumptions:

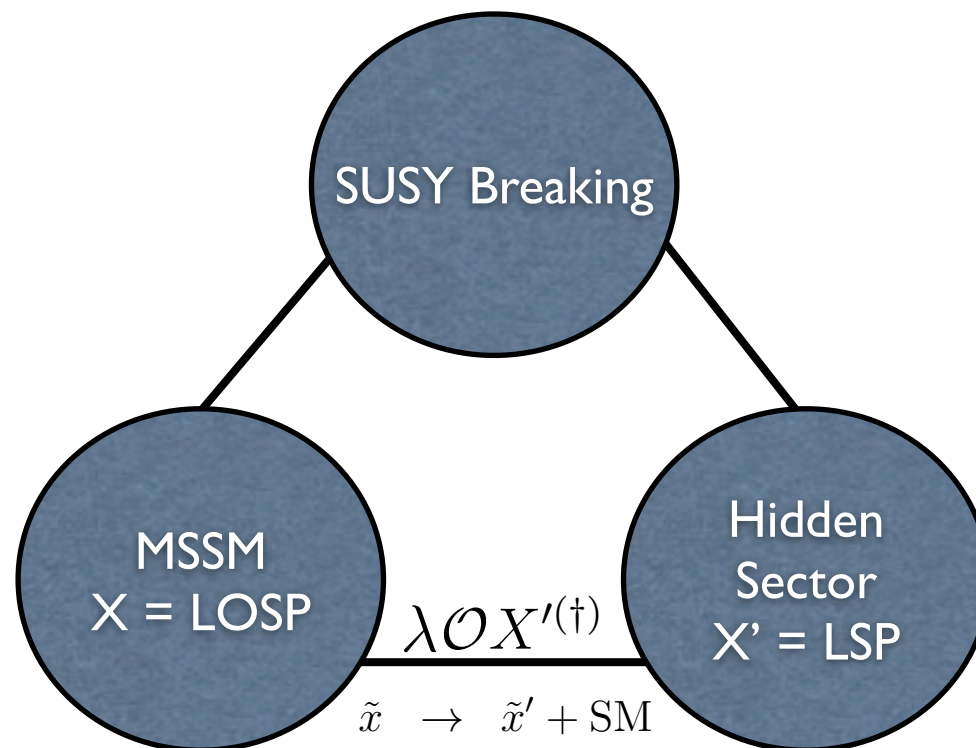
- Visible sector is the MSSM, and X is the LOSP $X \in \{Q, U, D, L, E, H_u, H_d, B^\alpha, W^\alpha, G^\alpha\}$
- X' is the LSP and is stabilized by R-Parity
- X' is a SM gauge singlet.
- Hidden and visible sectors are connected by gauge invariant dimension five or lower operators $\mathcal{O}X'^{(\dagger)}$



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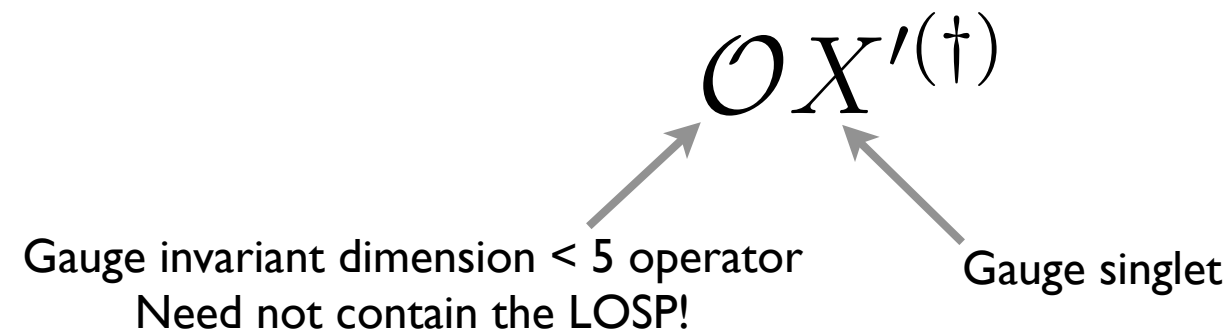
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What are the possible Portal Operators?

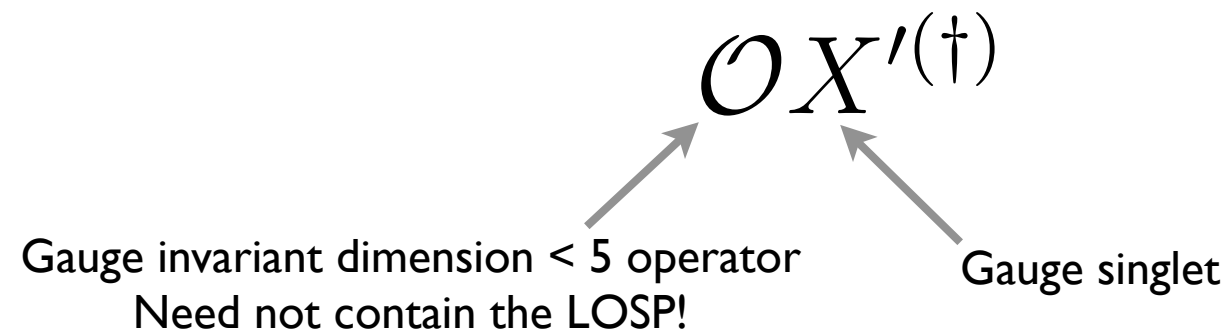
Portal Operators

Choice of R-parity and R-charge of X' dictates which portal operators are allowed.



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R-parity	+	+	+	−	−	−	−	−
R-charge	0	2	R_1	1	R_2	$R_2 - R_1$	$2 + R_2 - R_1$	R_3

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Present in the MSSM

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Higgs Portal (mass mixing)

Bino Portal (Kinetic Mixing)

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X' with odd R parity can couple to RPV operators.



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Could be fixed if we want see-saw neutrino masses.

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Out of these which operators give the best hope of reconstruction for FO&D and for FI?

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What are the possible LOSP candidates that are allowed and have the best hope of reconstruction at the LHC?

Reconstructing FO&D

To reconstruct need: $m, m', \langle \sigma v \rangle$

LOSP Candidates:

FO abundance of LOSP must be large enough:

$$\Omega \propto \frac{m'}{m \langle \sigma v \rangle} \quad \longrightarrow \quad \text{LOSP must overproduce by } m/m'$$

Two LOSP candidates in the MSSM:

- Bino with $m_{\tilde{b}} < 250 \text{ GeV}$ $m'/m_{\tilde{b}} > 1/20$
- Slepton with $m_{\tilde{l}_R} > 700 \text{ GeV}$ $m'/m_{\tilde{l}_R} < 1/2$.

$$X \in \{\cancel{Q}, \cancel{U}, \cancel{D}, \cancel{L}, E, \cancel{H}_u, \cancel{H}_d, B^\alpha, \cancel{W}^\alpha, \cancel{G}^\alpha\}$$

Portal Operators:

No restrictions:

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		$\tilde{\chi}_0 \rightarrow y' \tilde{y}'$	$\theta_{\tilde{\chi} \tilde{h}}^2 \lambda'^2$		
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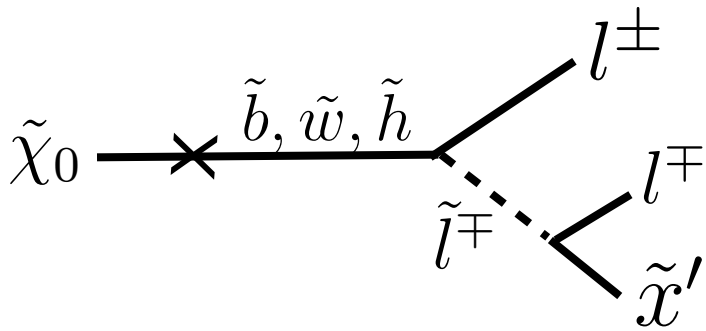
$$\Gamma(\tilde{x} \rightarrow \tilde{x}' + \text{SM}) = \left(\frac{1}{8\pi} \lambda^2 m\right) k(\tilde{x} \rightarrow \tilde{x}' + \text{SM})$$

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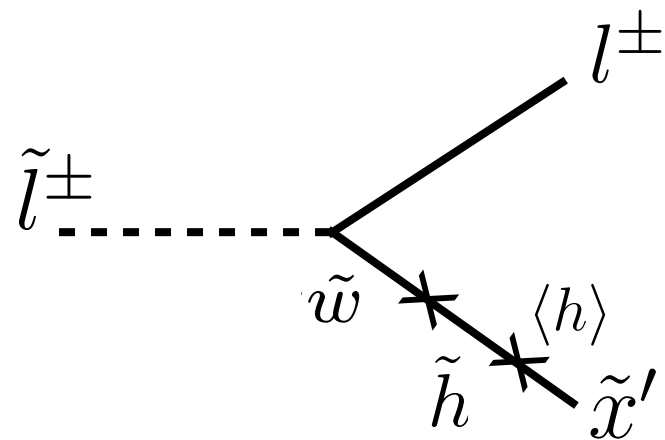
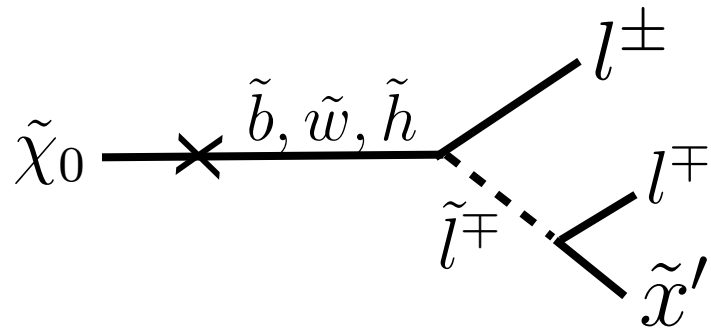
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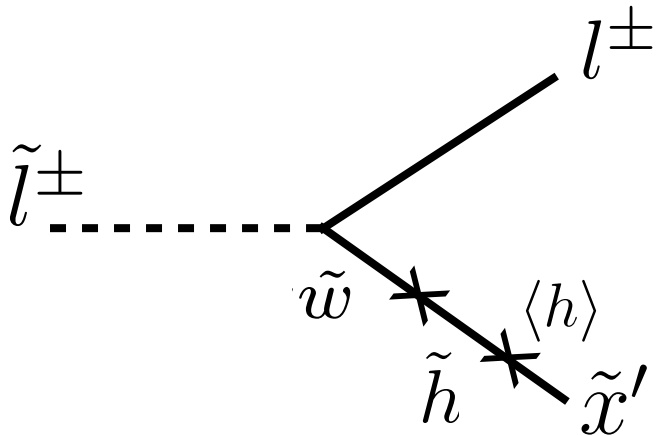
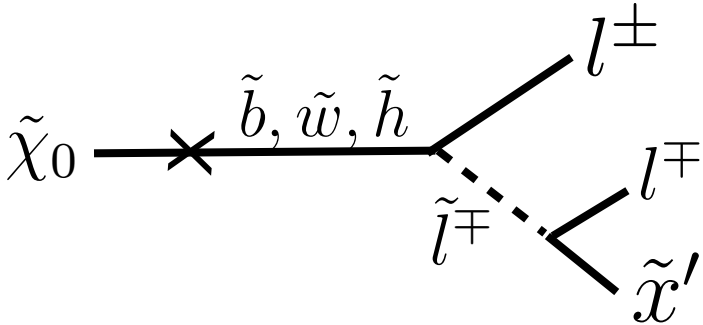
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Portal coupling need not contain the LOSP!

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Reconstructing FI

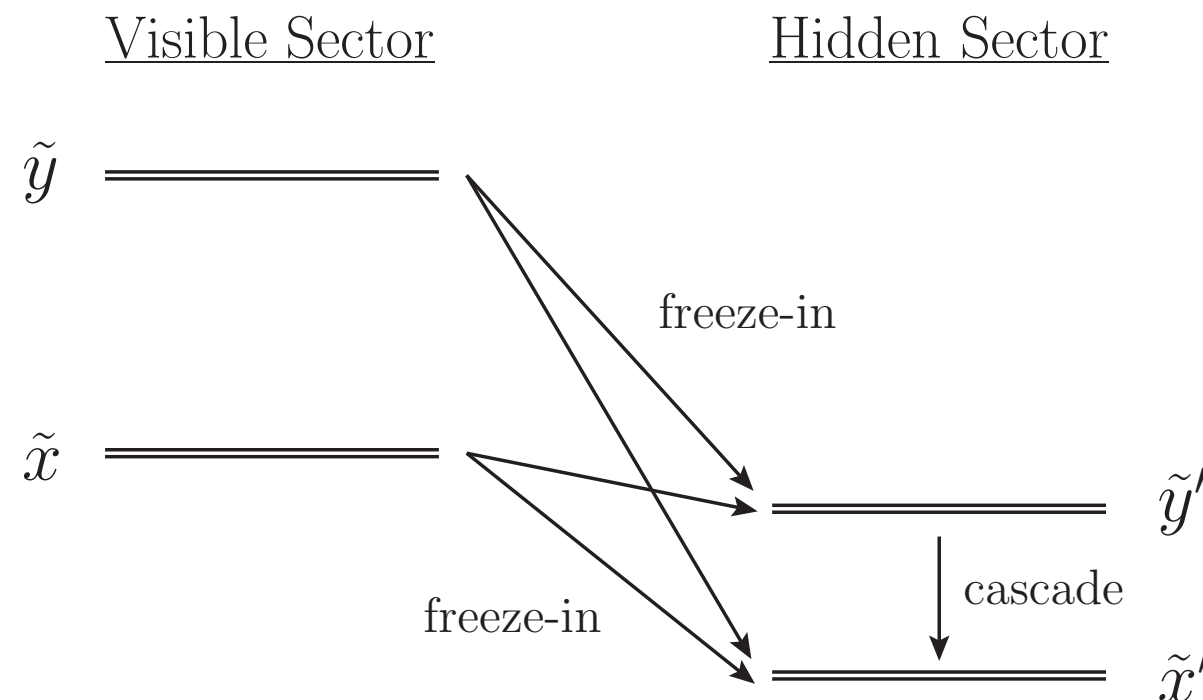
To reconstruct: m, m', τ * Unlike FO&D it is conceivable to directly measure all three at colliders

LOSP Candidates:

FO abundance must be small  Only bino excluded

Portal Operators:

Hidden Sector is rich, additional fields can give a FI contribution to X $\Omega \propto \frac{m'}{m^2 \tau}$



Reconstructing FI

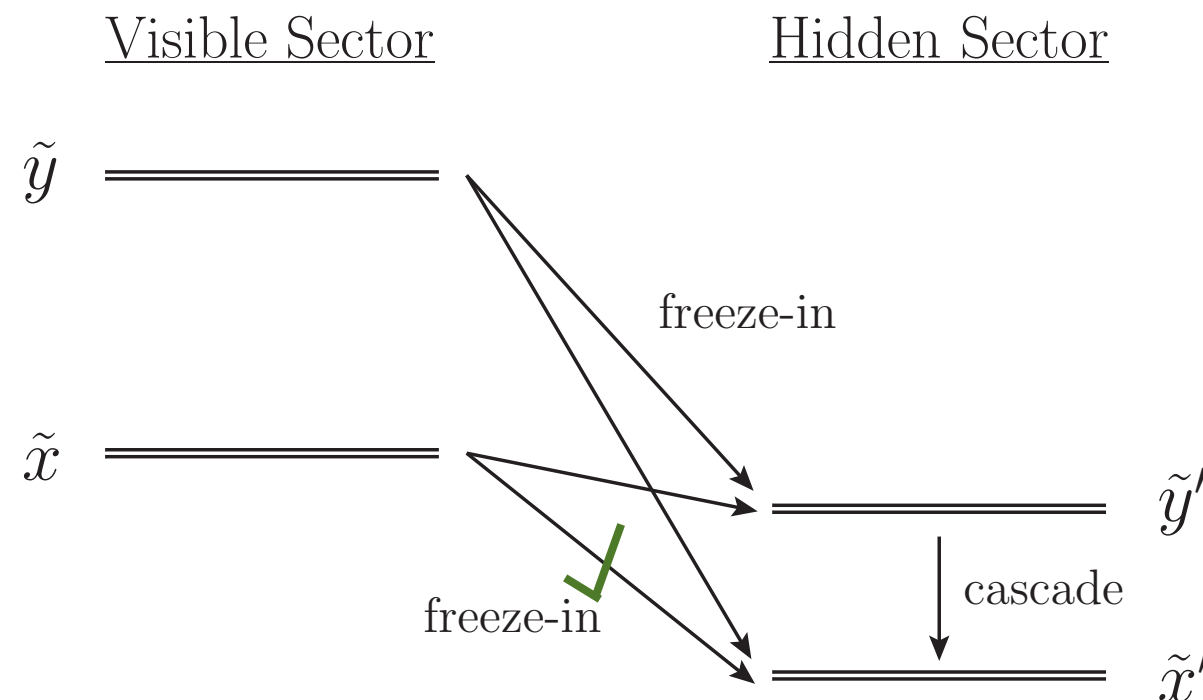
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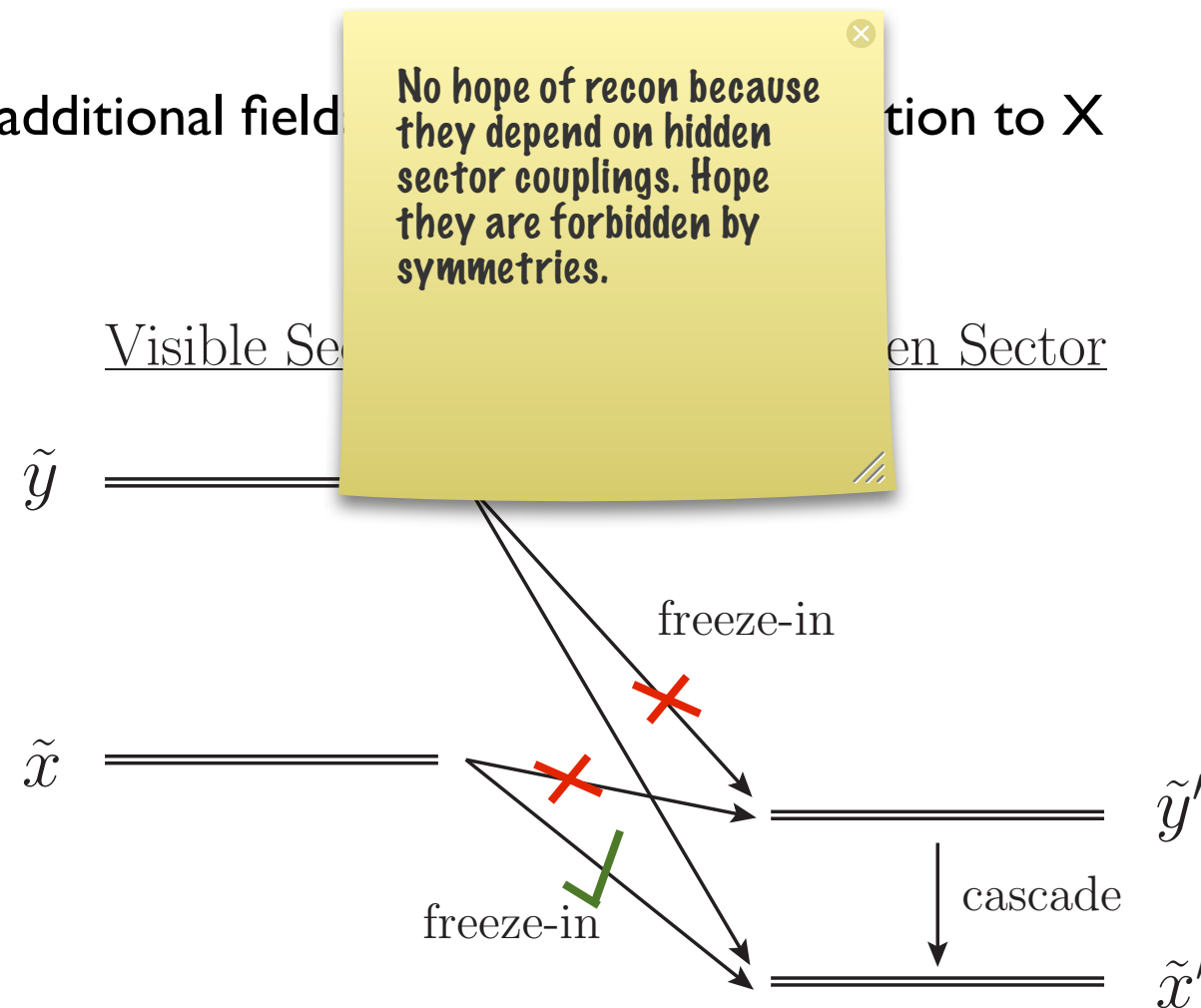
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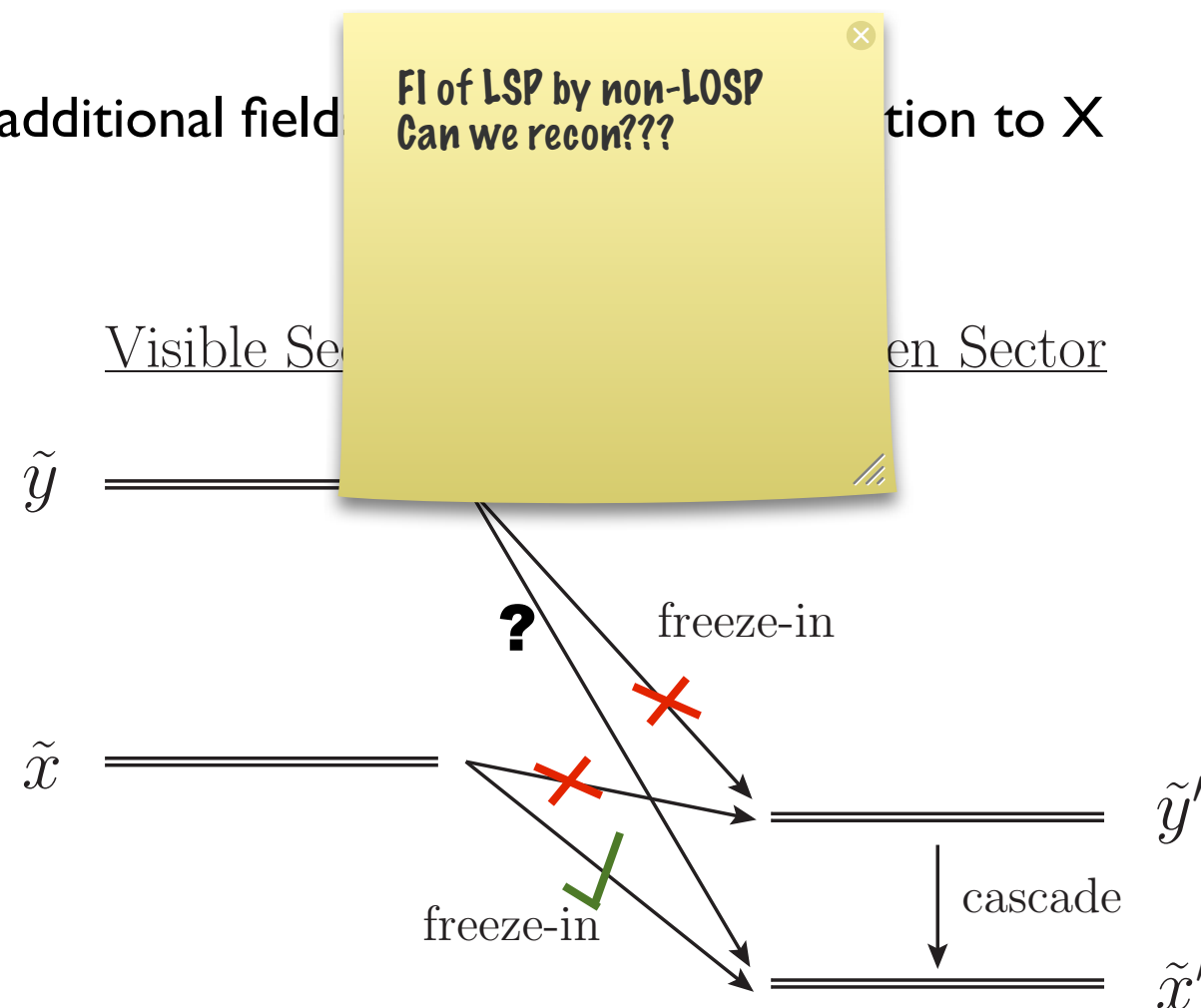
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coupling to X

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Any hope? $\tilde{y} \rightarrow \tilde{x}' + \text{SM}$

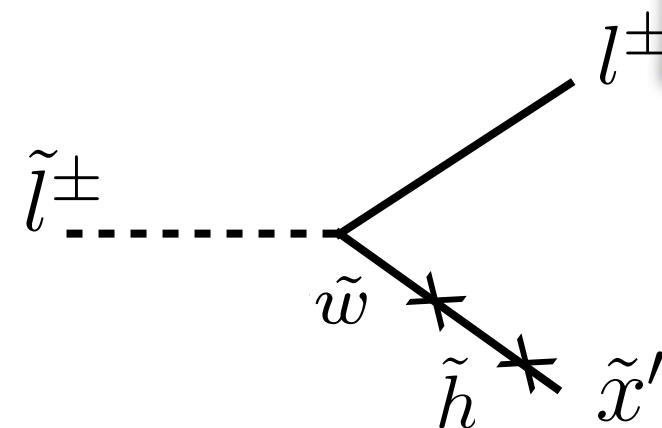
If only one operator couples the visible and hidden sectors then the coupling for FI of non-LOSPs can be inferred from the FI on the LOSP.

$$\tilde{x} \rightarrow \tilde{x}' + \text{SM}$$

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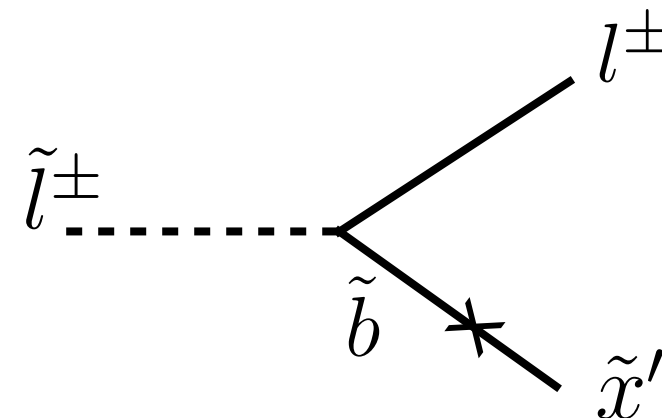
True also for LH, however L carries flavor index so that amount of couplings we would have to measure is considerably more so we don't consider this here

- Higgs Portal: $\lambda \int d^2\theta H_u H_d X'$



Mixing higgsino and dark matter through Higgs VEV.

- Bino Portal: $\lambda \int d^2\theta B^\alpha X'_\alpha$



Kinetic Mixing of bino and dark matter

Need to measure everything...

- * The portal coupling may be extracted from the slepton lifetime and measurement of the neutralino mass matrix.
- * Measure SUSY spectrum and compute the yield of DM from FI from decays of other superpartners.
- * These yields will differ for the Higgs and Bino portals.

Conclusions

- A thermally decoupled hidden sector provides seven dark matter production mechanisms:

FO' FO&D FO&D_r FO&D_a FI FI_r FI_a

- Freeze-out and Decay and Freeze-In have correspond to distinctive windows in parameter space and depend only on quantities that could in principle be measured at colliders.

	Freeze-Out and Decay (FO&D)	Freeze-In (FI)
LOSP	$\tilde{\chi}_0, \tilde{\ell}$	$\tilde{q}, \tilde{\ell}, \tilde{\nu}, \tilde{g}, \tilde{\chi}_0, \tilde{\chi}_{\pm}$
Operators	$\mathcal{O}X'$	$H_u H_d X', B^{\alpha} X'_{\alpha}$
Observables	$m, m', \langle \sigma v \rangle$	m, m', τ
Range	$10^{-27} \text{ cm}^3/\text{s} < \langle \sigma v \rangle < 10^{-26} \text{ cm}^3/\text{s}$	$10^{-4} \text{ s} < \tau < 10^{-1} \text{ s}$
Predicted Relation	$\frac{m' \langle \sigma v \rangle_0}{m \langle \sigma v \rangle} = 1$	$\frac{m'}{m\tau} \left(\frac{100 \text{ GeV}}{m} \right) = 25 \text{ s}^{-1}$

Back Up Slides

Asymmetric FI_a and FO&D_a

We have been assuming that DM abundance arises from the symmetric yield: $Y' = (n' + \bar{n}')/s$ since $\bar{n} = n$

Given no asymmetry at high temperature what conditions are necessary for DM to arise from a particle anti-particle asymmetry? $\eta' = \frac{n' - \bar{n}'}{s}$

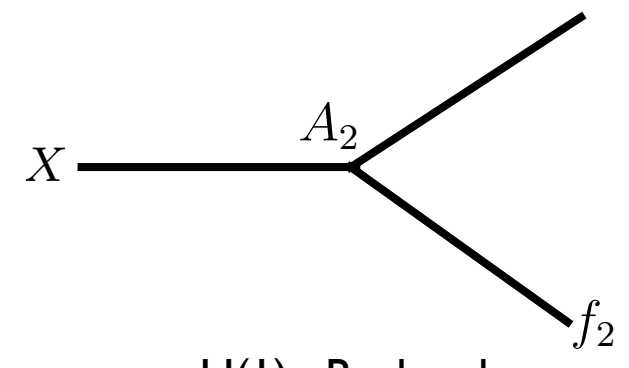
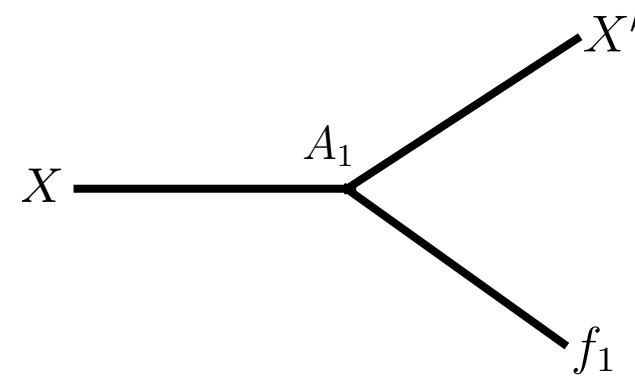
- X number violation requires hidden sector to contain a global U(1)_X
- X decays must be CP violating requires multiple X decay channels
- • Loss of thermal equilibrium

Asymmetry cannot be generated via FO or FO' since the total annihilation cross section is the same for particles and anti-particles by CPT.

Is it possible generate a non-zero asymmetry via FI and FO&D?

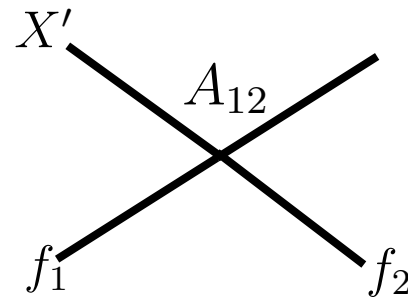
Yes! Sectors are at different temperatures so processes mediated by connector interactions are NOT in thermal equilibrium.

To violate CP requires multiple decay modes for X:



$U(1)_X$ Broken by
connector operator

As well as a re-scattering vertex:



A non-zero CP violation in X decays results from the interference between tree and loop contributions to decays:

$$\epsilon \simeq \frac{1}{16\pi} \frac{\text{Im}(A_1 A_2^* A_{12})}{|A_1|^2 + |A_2|^2}$$

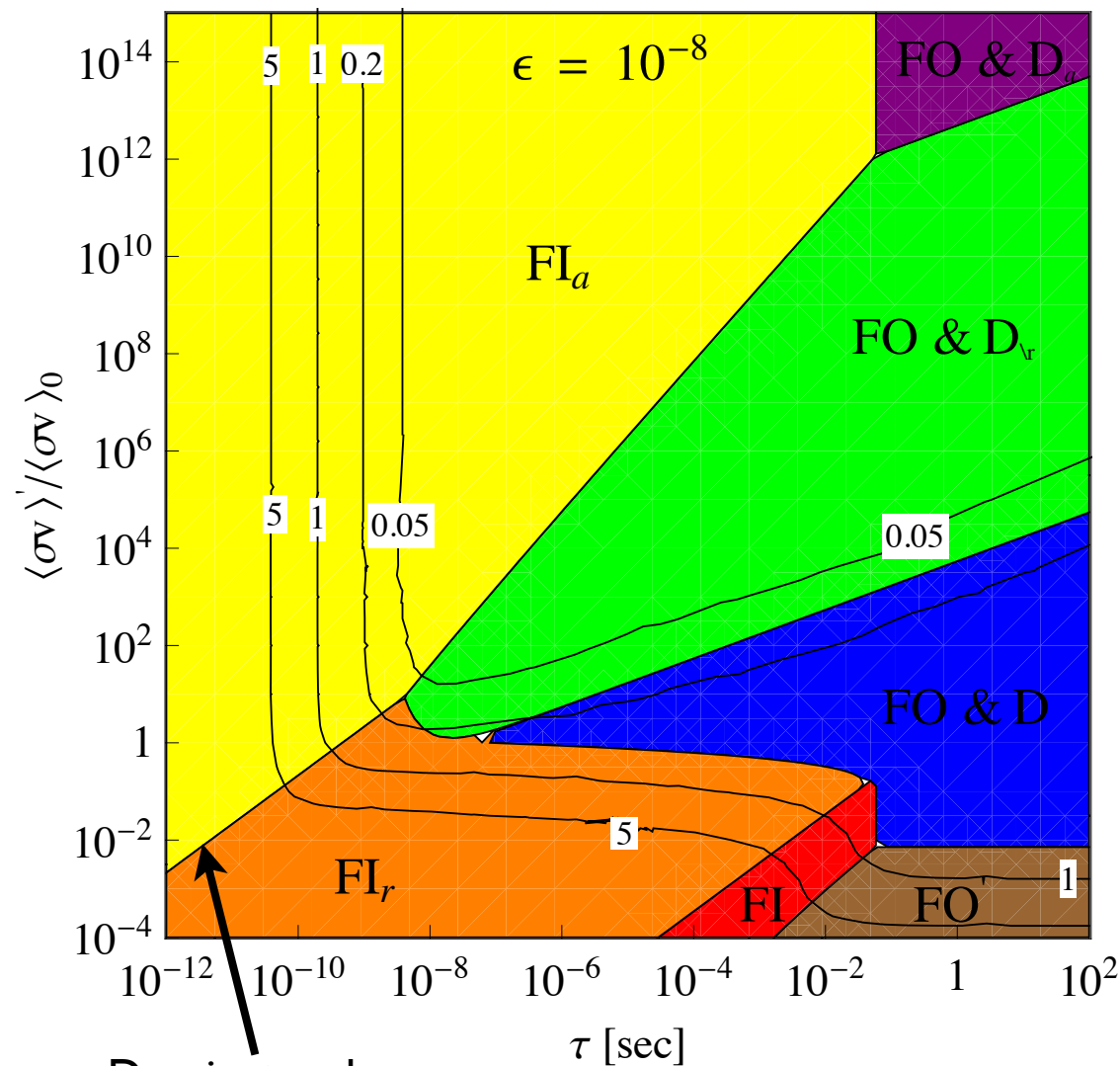
From the Boltzmann equations: $\eta' = \epsilon Y'$

Since the asymmetric yield is suppressed relative to the symmetric yield in order for the asymmetric yield to dominate the Dark Matter re-annihilations must be active in order to diminish the symmetric yield.

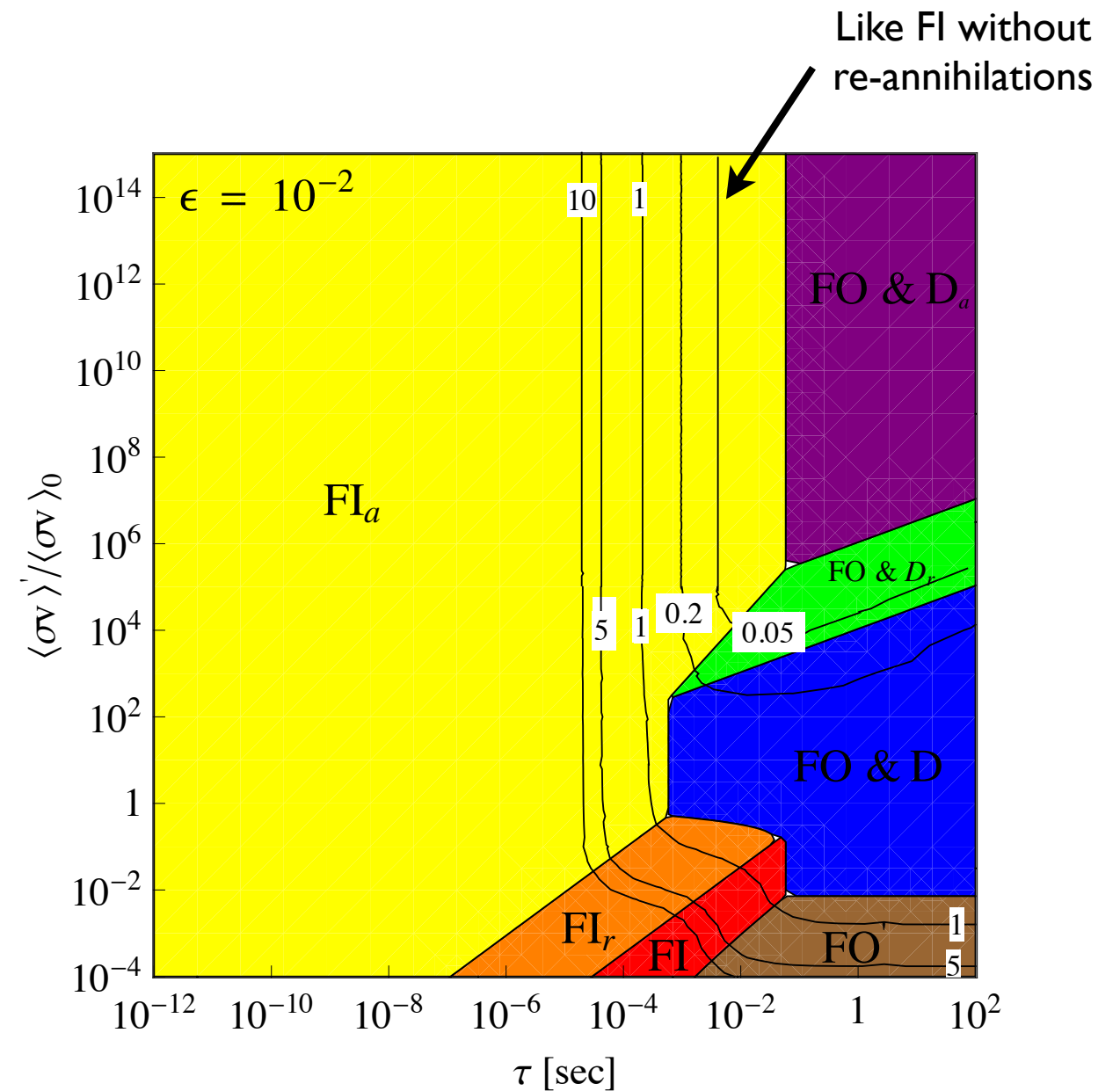
To get the right relic abundance: $m' \eta' = 4 \times 10^{-10} \text{ GeV}$

Asymmetric Phase Diagrams

Contours of symmetric + asymmetric contributions:



Dominate when
re-annihilations
is maximal



Like FI without
re-annihilations

$$Y'_{FO\&D} \propto \frac{1}{m\langle\sigma v\rangle}$$

$$Y'_{FI} \propto \frac{1}{\tau m^2}$$

$$\begin{aligned} \langle\sigma v\rangle &= \langle\sigma v\rangle_0 = 3 \times 10^{-26} \text{ cm}^3/\text{s} \\ m &= 100 \text{ GeV}, m' = 50 \text{ GeV} \\ \xi_{UV} &= 0.01 \end{aligned}$$

Collider Signatures of FO&D:

- Higgs or Bino Portals: The dominant decay will be 2-body into hidden sector states.

$$\lambda \int d^2\theta B^\alpha X'_\alpha$$

$$\mathcal{L}_{\text{int}} \approx \lambda (\tilde{x}' \tilde{J} + \tilde{b} \tilde{J}')$$

$$\tilde{J}' = \sum_{i=\text{hidden}} g'_i \phi'_i \psi'_i$$

 $\tilde{\chi}^0 \rightarrow y' \tilde{y}'$

So LSP mass must be reconstructed from subdominant visible decay modes.

- LSP Multiplicities: Hidden sector states will cascade down and can produce an odd number of LSPs.

$$y' \rightarrow \tilde{x}' \tilde{x}'$$

X' is R-Parity Even

FO&D					
Operator	Charges (X')	$\tilde{\chi}_0$		$\tilde{\ell}^\pm$	
		Decay	k	Decay	k
$\mathcal{O}_K X'$	$(+, 0)$	$\tilde{\chi}_0 \rightarrow \ell^+ \ell^- \tilde{x}'$ $\tilde{\chi}_0 \rightarrow (h^0, Z) \tilde{x}'$	$\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\ell}^2 \frac{m^4}{m_{\tilde{\ell}}^4}$ $\theta_{\tilde{\chi}\tilde{h}}^2, \theta_{\tilde{\chi}\tilde{h}}^2 g_2^2$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \tilde{x}'$	1
$\mathcal{O}_W X'$	$(+, 0)$	$\chi_0 \rightarrow (\gamma, Z) \tilde{x}'$ $\tilde{\chi}_0 \rightarrow \ell^+ \ell^- \tilde{x}'$	$\theta_{\tilde{\chi}\tilde{b}}^2, \theta_{\tilde{\chi}\tilde{w}}^2$ $\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\ell}^2 \frac{m^4}{m_{\tilde{\ell}}^4}$	$\tilde{\ell}^\pm \rightarrow \ell^\pm (\gamma, Z) \tilde{x}'$ $\tilde{\ell}^\pm \rightarrow \ell^\pm \tilde{x}'$	$\frac{1}{(4\pi)^2} m^2 (\frac{g_{1\ell}^2}{m_b^2}, \frac{g_2^2}{m_w^2})$ 1
$H_u H_d X' (X'^\dagger)$	$(+, 2 - R_1)$ or $(+, R_1)$	$\tilde{\chi}_0 \rightarrow (h^0, Z) \tilde{x}'$ $\tilde{\chi}_0 \rightarrow y' \tilde{y}'$ $\tilde{\chi}_0 \rightarrow \ell^+ \ell^- \tilde{x}'$	$\theta_{\tilde{\chi}\tilde{h}}^2, \theta_{\tilde{\chi}\tilde{h}}^2 g_2^2$ $\theta_{\tilde{\chi}\tilde{h}}^2 \lambda'^2$ $\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\ell}^2 g_{1\ell}^2 \frac{m^4}{m_{\tilde{\ell}}^4}$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \tilde{x}'$	$g_{h\tilde{\ell}\ell}^2$

X' is R-Parity Odd

FO&D					
Operator	Charges (X')	$\tilde{\chi}_0$		$\tilde{\ell}^\pm$	
		Decay	k	Decay	k
$B^\alpha X'_\alpha$	$(-, 1)$	$\tilde{\chi}_0 \rightarrow y' \tilde{y}'$ $\tilde{\chi}_0 \rightarrow \ell^+ \ell^- \tilde{x}'$ $\tilde{\chi}_0 \rightarrow (h^0, Z) \tilde{x}'$	$\theta_{\tilde{\chi}\tilde{b}}^2 g'^2$ $\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\ell}^2 g_{1\ell}^2 \frac{m^4}{m_{\tilde{\ell}}^4}$ $\theta_{\tilde{\chi}\tilde{h}}^2, \theta_{\tilde{\chi}\tilde{h}}^2 g_2^2$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \tilde{x}'$	$g_{1\ell}^2$
$LH_u X'$	$(-, 2 - R_2)$	$\tilde{\chi}_0 \rightarrow \nu \tilde{x}'$ $\tilde{\chi}_0 \rightarrow \ell^\pm (h^\mp, W^\mp) \tilde{x}'$	$\theta_{\tilde{\chi}\tilde{h}}^2$ $\frac{1}{(4\pi)^2} g_2^2 \frac{m^2}{m_h^2} (\theta_{\tilde{\chi}\tilde{w}}^2, \theta_{\tilde{\chi}\tilde{h}}^2)$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \nu \tilde{x}'$ $\tilde{\ell}^\pm \rightarrow (h^\pm, W^\pm) \tilde{x}'$	$\frac{1}{(4\pi)^2} g_{h\tilde{\ell}\ell}^2 \frac{m^2}{m_h^2}$ $\theta_{\tilde{\ell}\tilde{\ell}_L}^2 (1, g_2^2)$
$LH_u X'^\dagger$	$(-, R_2)$	"	"	"	"
$LH_d^\dagger X'^\dagger$	$(-, R_2 - R_1)$	"	"	"	"
$LH_d^\dagger X'$	$(-, R_1 - R_2)$	"	"	"	"
$LLEX', QLDX'$	$(-, R_1 - R_2)$	$\tilde{\chi}_0 \rightarrow l^+ l^- \nu \tilde{x}'$	$\frac{1}{(4\pi)^4} g_{\tilde{\chi}\tilde{\ell}\ell}^2 \frac{m^4}{m_{\tilde{\ell}}^4}$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \nu \tilde{x}'$	$\frac{1}{(4\pi)^2}$

Collider Signatures of FI:

FI				
	Higgs Portal: $H_u H_d X'$		Bino Portal: $B^\alpha X'_\alpha$	
LOSP	Decay	k	Decay	k
\tilde{g}	$\tilde{g} \rightarrow qq\tilde{x}'$	$\frac{1}{(4\pi)^2} g_{h\tilde{q}q}^2 \frac{m^4}{m_{\tilde{q}}^4}$	$\tilde{g} \rightarrow qq\tilde{x}'$	$\frac{1}{(4\pi)^2} g_{1q}^2 \frac{m^4}{m_{\tilde{q}}^4}$
$\tilde{\nu}$	$\tilde{\nu} \rightarrow \ell^\pm (h^\mp, W^\mp) \tilde{x}'$ $\tilde{\nu} \rightarrow \tilde{\nu} \tilde{x}'$	$\frac{1}{(4\pi)^2} g_{h\tilde{\nu}\ell}^2 \frac{m^2}{m_{\tilde{h}}^2} (1, g_2^2)$ $g_{h\tilde{\nu}\nu}^2$	$\tilde{\nu} \rightarrow \ell^\pm (h^\mp, W^\mp) \tilde{x}'$ $\nu \rightarrow \nu \tilde{x}'$	$\frac{1}{(4\pi)^2} g_{1h}^2 g_{h\tilde{\nu}\ell}^2 \frac{m^2}{m_{\tilde{h}}^2} (1, g_2^2)$ $g_{1\nu}^2$
\tilde{q}	$\tilde{q} \rightarrow q\tilde{x}'$ $\tilde{q} \rightarrow q(h^{0,\pm}, W^{0,\pm})\tilde{x}'$	$g_{h\tilde{q}q}^2$ $\frac{1}{(4\pi)^2} g_{h\tilde{q}q}^2 \frac{m^2}{m_{\tilde{h}}^2} (1, g_2^2)$	$\tilde{q} \rightarrow q\tilde{x}'$ $\tilde{q} \rightarrow q(h^{0,\pm}, W^{0,\pm})\tilde{x}'$	g_{1q}^2 $\frac{1}{(4\pi)^2} g_{1h}^2 g_{h\tilde{q}q}^2 \frac{m^2}{m_{\tilde{h}}^2} (1, g_2^2)$
$\tilde{\chi}^\pm$	$\tilde{\chi}^\pm \rightarrow (h^\pm, W^\pm) \tilde{x}'$ $\tilde{\chi}^\pm \rightarrow \ell^\pm \nu \tilde{x}'$	$g_2^2 (\theta_{\tilde{\chi}\tilde{w}}^2, \theta_{\tilde{\chi}\tilde{h}}^2)$ $\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\nu}^2 g_{h\tilde{\ell}\ell}^2 \frac{m^4}{m_{\tilde{l}}^4}$	$\tilde{\chi}^\pm \rightarrow (h^\pm, W^\pm) \tilde{x}'$ $\tilde{\chi}^\pm \rightarrow \ell^\pm \nu \tilde{x}'$	$g_{1h}^2 (\theta_{\tilde{\chi}\tilde{h}}^2, \theta_{\tilde{\chi}\tilde{w}}^2)$ $\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\nu}^2 g_{1\ell}^2 \frac{m^4}{m_{\tilde{l}}^4}$
$\tilde{\chi}_0$	$\tilde{\chi}_0 \rightarrow (h^0, Z) \tilde{x}'$ $\tilde{\chi}_0 \rightarrow y' \tilde{y}'$ $\tilde{\chi}_0 \rightarrow \ell^+ \ell^- \tilde{x}'$	$\theta_{\tilde{\chi}\tilde{h}}^2, \theta_{\tilde{\chi}\tilde{h}}^2 g_2^2$ $\theta_{\tilde{\chi}\tilde{h}}^2 \lambda'^2$ $\frac{1}{(4\pi)^2} g_{\tilde{\chi}\tilde{\ell}\ell}^2 g_{h\tilde{\ell}\ell}^2 \frac{m^4}{m_{\tilde{l}}^4}$	$\tilde{\chi}_0 \rightarrow (h^0, Z) \tilde{x}'$ $\tilde{\chi}_0 \rightarrow y' \tilde{y}'$ $\tilde{\chi}_0 \rightarrow \ell^+ \ell^- \tilde{x}'$	$\theta_{\tilde{\chi}\tilde{h}}^2 g_{1h}^2, \theta_{\tilde{\chi}\tilde{h}}^2 g_2^2 g_{1h}^2$ $\theta_{\tilde{\chi}\tilde{b}}^2 g'^2$ $\frac{1}{(4\pi)^2} g_{\chi\tilde{\ell}\ell}^2 g_{1\ell}^2 \frac{m^4}{m_{\tilde{l}}^4}$
$\tilde{\ell}^\pm$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \tilde{x}'$	$g_{h\tilde{\ell}\ell}^2$	$\tilde{\ell}^\pm \rightarrow \ell^\pm \tilde{x}'$	$g_{1\ell}^2$

Collider Signals

Note: Asymmetric FI and FO&D are harder to reconstruct due to the CP phase but the same operators and LOSPs apply

- See signal at LHC.
- Identity of LOSP candidate is now known.
- What mechanism and what operator?
- Look up corresponding portal operator(s).
- Sometimes result is unique.
- How to resolve ambiguities?

X' is R-Parity Even

	$L^\dagger L X'$ $Q^\dagger Q X'$ $H^\dagger H X'$	$W^2 X'$	$QUHX'$ $LEHX'$ $QDHX'$	$H_u H_d X'$
$\tilde{\chi}^0$	$h^0, Z, \ell^+ \ell^-$	γ, Z	$l^+ l^-$	$h^0, Z, l^+ l^-$
\tilde{l}^\pm	l^\pm	$l^\pm (\gamma, Z, h^0), \nu(W^\pm, h^\pm)$	l^\pm	l^\pm
$\tilde{\chi}^\pm$	$h^\pm, W^\pm, \ell^\pm \nu$	h^\pm, W^\pm	$l^\pm \nu$	h^\pm, W^\pm
$\tilde{\nu}$	$\nu(1, h^0, Z), l^\pm(h^\mp W^\mp)$	$\nu(\gamma, Z, h^0), \ell^\pm(W^\mp, h^\mp)$	$l^\pm(h^\mp, W^\mp)$	$\nu(1, h^0, Z), l^\pm(h^\mp W^\mp)$
\tilde{q}	$j(1, h^0, Z, h^\pm, W^\pm)$	$j(\gamma, Z, h^0, W^\pm, h^\pm)$	$j(1, h^0, Z, h^\pm, W^\pm)$	$j(1, h^0, Z, h^\pm, W^\pm)$
\tilde{g}	$jj(1, h^0, Z, h^\pm, W^\pm)$	$jj(\gamma, Z, h^0, W^\pm, h^\pm)$	$jj(1, h^0, Z, h^\pm, W^\pm)$	$jj(1, h^0, Z, h^\pm, W^\pm)$

X' is R-Parity Odd

	$B^\alpha X'_\alpha$	$LH_u X'$ $LH_u X'^\dagger$	$LH_d^\dagger X'$ $LH_d^\dagger X'^\dagger$	$LLEX'$	$QDLX'$	$UDDX'$
$\tilde{\chi}^0$	$h^0, Z, l^+ l^-$	$\nu(1, h^0, Z), l^\pm(h^\mp, W^\mp)$	$\nu(1, h^0, Z), l^\pm(h^\mp, W^\mp)$	$l^+ l^- \nu$	$jj(l^\pm, \nu)$	jjj
\tilde{l}^\pm	l^\pm	h^\pm, W^\pm	h^\pm, W^\pm	$l^\pm \nu$	jj	$jjj(l^\pm, \nu)$
$\tilde{\chi}^\pm$	$h^\pm W^\pm$	l^\pm	l^\pm	$l^\pm l^+ l^-, l^\pm \nu \nu$	$jj(l^\pm, \nu)$	jjj
$\tilde{\nu}$	$\nu(1, h^0, Z), l^\pm(h^\mp W^\mp)$	h^0, Z	h^0, Z	$l^+ l^-$	jj	$jjj(l^\pm, \nu)$
\tilde{q}	$j(1, h^0, Z, h^\pm, W^\pm)$	$j(l^\pm, \nu)$	$j(l^\pm, \nu)$	$j(l^+ l^- \nu, l^\pm l^+ l^-, l^\pm \nu \nu)$	$j(l^\pm, \nu)$	jj
\tilde{g}	$jj(1, h^0, Z, h^\pm, W^\pm)$	$jj(l^\pm, \nu)$	$jj(l^\pm, \nu)$	$jj(l^+ l^- \nu, l^\pm l^+ l^-, l^\pm \nu \nu)$	$jj(l^\pm, \nu)$	jjj

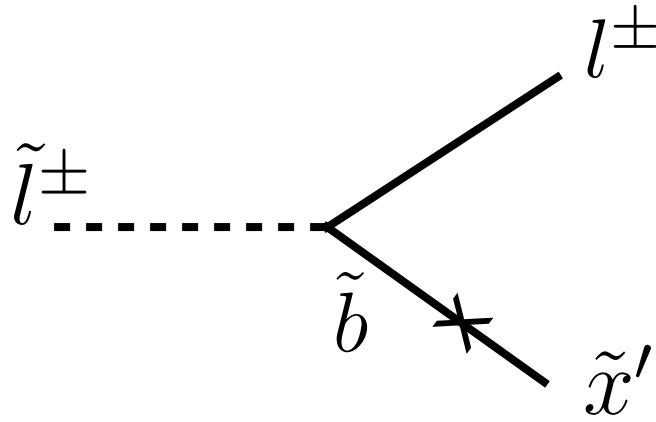
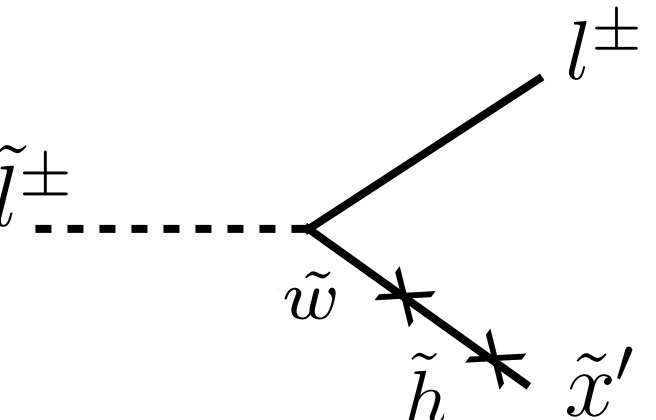
An Example: $\tilde{l}^\pm \rightarrow l^\pm \tilde{x}'$

- Suppose LHC discovers a charged slepton LOSP with mass of 200GeV.
- Suppose slepton decays to lepton + missing energy.
- Suppose lifetime is measured to be 0.1sec, and m' is reconstructed to be 100GeV.

Production Mechanism:

Low slepton mass \rightarrow Cosmological Phase space chooses FI rather than FO&D

Portal:

- Bino Portal: 
 - Higgs Portal: 
- } Same signal but with different branching fraction.
Which portal?

To get correct relic abundance from FI: $\frac{m'}{m\tau} \left(\frac{100 \text{ GeV}}{m} \right) = 25 \text{ s}^{-1}$

So reconstructed lifetime 0.1 sec is a factor of ten too big

→ Only 10% of DM abundance arises from FI of LOSP decays

Could other measurements reveal that the remaining 90% arose from FI of non-LOSPs?

Measure the superpartner spectrum:

- The Portal coupling can be extracted from the slepton lifetime and measurement of the neutralino mass matrix.
- Compute the yield of DM from FI from decays of other superpartners. These yields will differ for the Higgs and Bino portals.

→ Then we could see if the yield from non-LOSP decays in one of these portals accounts for the remaining 90% of DM.

Freeze-In

L. Hall, K. Jedamzik, J. March-Russel, S. West [0911.1120]

FI via decay of bath particle to the FIMP: $B_1 \rightarrow B_2 X$

$$\dot{n}_X + 3Hn_X = \int d\Pi_X d\Pi_{B_1} d\Pi_{B_2} (2\pi)^4 \delta^4(p_X + p_{B_2} - p_{B_1}) \\ \times \left[|M|_{B_1 \rightarrow B_2 + X}^2 f_{B_1} (1 \pm f_{B_2})(1 \pm f_X) - |M|_{B_2 + X \rightarrow B_1}^2 f_{B_2} f_X (1 \pm f_{B_1}) \right]$$

$$\dot{n}_X + 3n_X H \approx g_{B_1} \int \frac{d^3 p_{B_1}}{(2\pi)^3} \frac{f_{B_1} \Gamma_{B_1}}{\gamma_{B_1}} = g_{B_1} \int_{m_{B_1}}^{\infty} \frac{m_{B_1} \Gamma_{B_1}}{2\pi^2} (E_{B_1}^2 - m_{B_1}^2)^{1/2} e^{-E_{B_1}/T} dE_{B_1} \\ = \frac{g_{B_1} m_{B_1}^2 \Gamma_{B_1}}{2\pi^2} T K_1(m_{B_1}/T)$$

$$Y_{1 \rightarrow 2}(T) \propto \frac{M_{Pl} m_{B_1} \Gamma_{B_1}}{T^3}$$

Bino Portal

X' is the gauge field of a $U(1)'$ in the hidden sector:

$$\mathcal{L} = \lambda \int d^2\theta B^\alpha X'_\alpha + \tilde{\lambda} \int d^2\theta B^\alpha X'_\alpha \Phi \supset i\lambda \tilde{b} \bar{\sigma}^\mu \partial_\mu \tilde{x}' + \tilde{\lambda} m_{3/2} \tilde{b} \tilde{x}'$$

Coupling depends on UV theory and can be made small enough for FI

$$\lambda = \sum_i \frac{g_i g'_i}{16\pi^2} \text{Log} \left(\frac{\Lambda}{m_i} \right)$$

Shift to remove gaugino kinetic mixing: $\tilde{B}_\alpha \rightarrow \tilde{B}_\alpha + \lambda \tilde{X}'_\alpha$

Hidden-Visible sector coupling induced in the interaction Lagrangian:

$$\begin{aligned} \mathcal{L}_{\text{int}} &= \int d^4\theta \left(\Phi_i^\dagger e^{2g_i B_\alpha} \Phi_i + \Phi_j'^\dagger e^{2g'_j X'_\alpha} \Phi_j' \right) \\ &\rightarrow \left(\Phi_i^\dagger e^{2g_i (B_\alpha + \lambda \tilde{X}'_\alpha)} \Phi_i + \Phi_j'^\dagger e^{2g'_j X'_\alpha} \Phi_j' \right) \\ &\supset g_i \phi_i^* \psi_i \tilde{b} + \text{h.c.} + g_i \lambda \phi_i^* \psi_i \tilde{x}' + \dots \end{aligned}$$

As well as mass mixing: $m_{\tilde{b}} \tilde{b} \tilde{b} \rightarrow m_{\tilde{b}} \tilde{b} \tilde{b} + \lambda m_{\tilde{b}} (\tilde{b} \tilde{x}' + \text{h.c.})$

$$\mathcal{L}_{\text{int}} \approx \lambda \left(\tilde{x}' \tilde{J} + \tilde{b} \tilde{J}' \right)$$

$$\tilde{J}' = \sum_{i=\text{hidden}} g'_i \phi_i' \psi_i'$$

Detection at the LHC

Depends on the nature of the LOSP

Charged/Colored LOSP: K. Hamaguchi, Y. Hundo, T. Nakaya M. M. Nojiri hep-ph/0409248
J.L. Feng, B.T. Smith hep-ph/0409278 ...

- Lifetime and decay products can be measured for a large range of lifetimes 10^{-12} sec to 10^{-6} sec.
- Electrically charged sleptons and charginos will produce charge tracks which can be used to measure LOSP mass
- LOSPs emitted with small velocities will lose their kinetic energy by ionization and stop inside the calorimeter.
- Proposals for stopper detectors to be built outside the main detector.

Neutral LOSP:

- Prospects are highly dependent on LOSP lifetime
- For FI the lifetime $\sim 10^{-2}$ sec gives a decay length $L_{FI} \sim 10^6 \text{ meters} \times \gamma \left(\frac{m'/m}{0.25} \right) \left(\frac{300 \text{ GeV}}{m} \right) \frac{1}{N_{\text{eff}}}$